



Fitting GBM Gamma-Ray Burst Spectra with Physical Emission Models

J. Michael Burgess

Rob Preece, Matthew Baring, Michael Briggs, Valerie Connaughton, Sylvain Guiriec
on behalf of the Fermi GBM Team

What We Know...

- * Band's GRB function fits most GRB spectra well.
- * Synchrotron spectrum appears to be inconsistent with some fitted Band indices (Preece (1998)).
- * Multi-component spectra (Gonzalez et al. (2003), Fermi LAT Team (2009-2011), Ryde (2009) Guiriec et al. (2011))
- * Electron distributions from relativistic shock acceleration are well known (Baring (2011), Spikovsky (2008)).

Electron Distributions

SHOCK ACCELERATION

BARING AND BRABY (2004)

$$n_e(\gamma) = n_0 \left(\frac{\gamma}{\gamma_{th}} \right)^2 e^{-\frac{\gamma}{\gamma_{th}}} \Theta \left(\eta - \frac{\gamma}{\gamma_{th}} \right) + \epsilon \left(\frac{\gamma}{\gamma_{th}} \right)^{-\delta} \Theta \left(\frac{\gamma}{\gamma_{th}} - \eta \right)$$

FAST COOLING

BLUMENTHAL & GOULD (1971)

$$\frac{\partial}{\partial t} n_e(\gamma, t) + \frac{\partial}{\partial \gamma} (\dot{\gamma} n_e(\gamma, t)) = Q_{inj}(\gamma) - \frac{n_e(\gamma, t)}{t_{esc}}$$

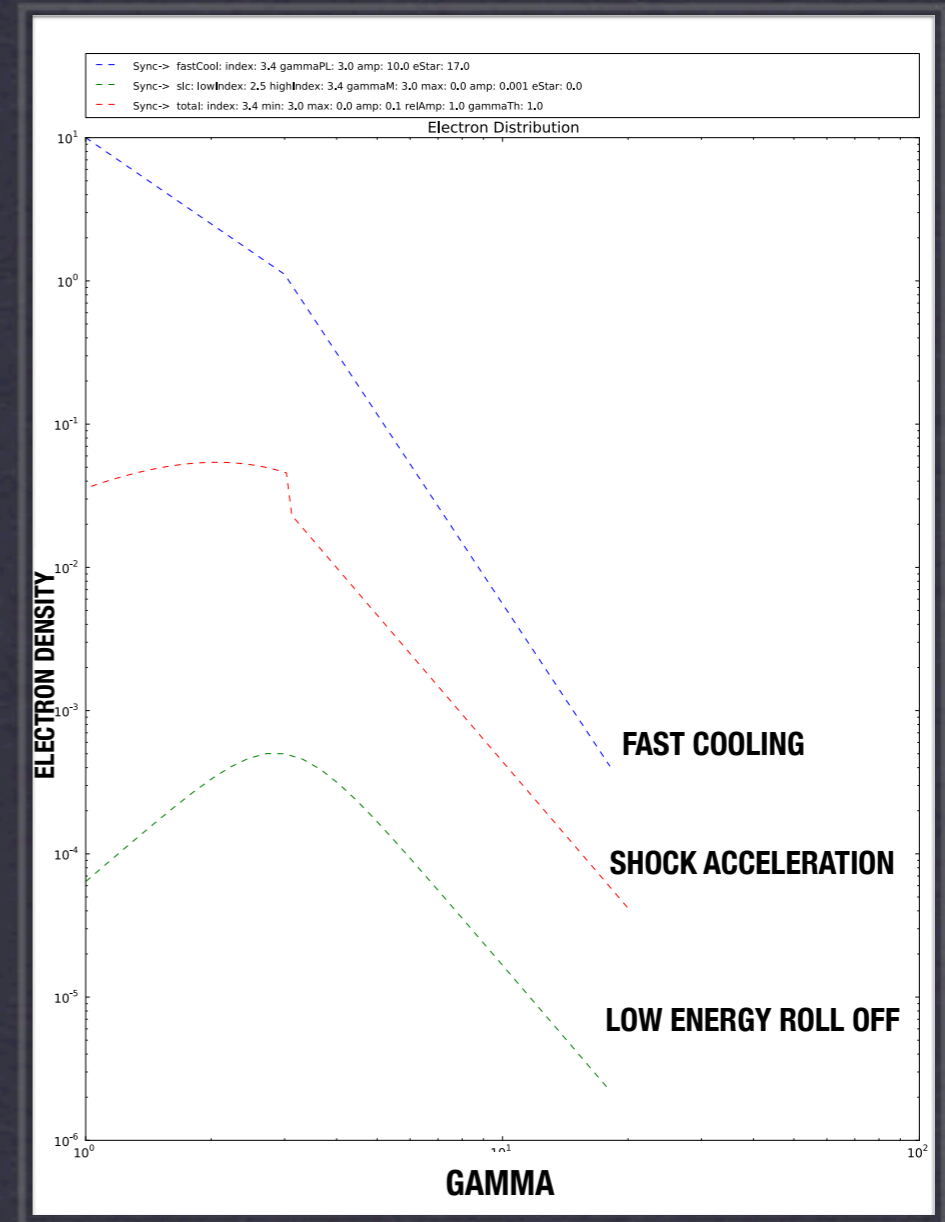
$$Q_{inj}(\gamma) = n_0 (\delta - 1) \gamma_{pl}^{\delta-1} \gamma^{-\delta} \Theta(\gamma - \gamma_{pl}) \quad \dot{\gamma} = -\frac{2}{3} \frac{r_0 c}{r_g^2} \gamma^2 \sin^2 \theta$$

$$n_e^{cool}(\gamma) = n_0 \frac{3}{2} \frac{n_0 r_g^2}{r_0 c \sin^2 \theta} \gamma^{-2} \left[\left(\frac{\gamma}{\gamma_{pl}} \right)^{-(\delta-1)} \Theta(\gamma - \gamma_{pl}) - \Theta(\gamma_{pl} - \gamma) \right]$$

LOW-ENERGY ROLL OFF

LLOYD & PETROSIAN (2002)

$$n_e^{rolloff}(\gamma) = n_0 \frac{(\gamma/\gamma_m)^q}{1 + (\gamma/\gamma_m)^{p+q}}$$



Electron Distributions

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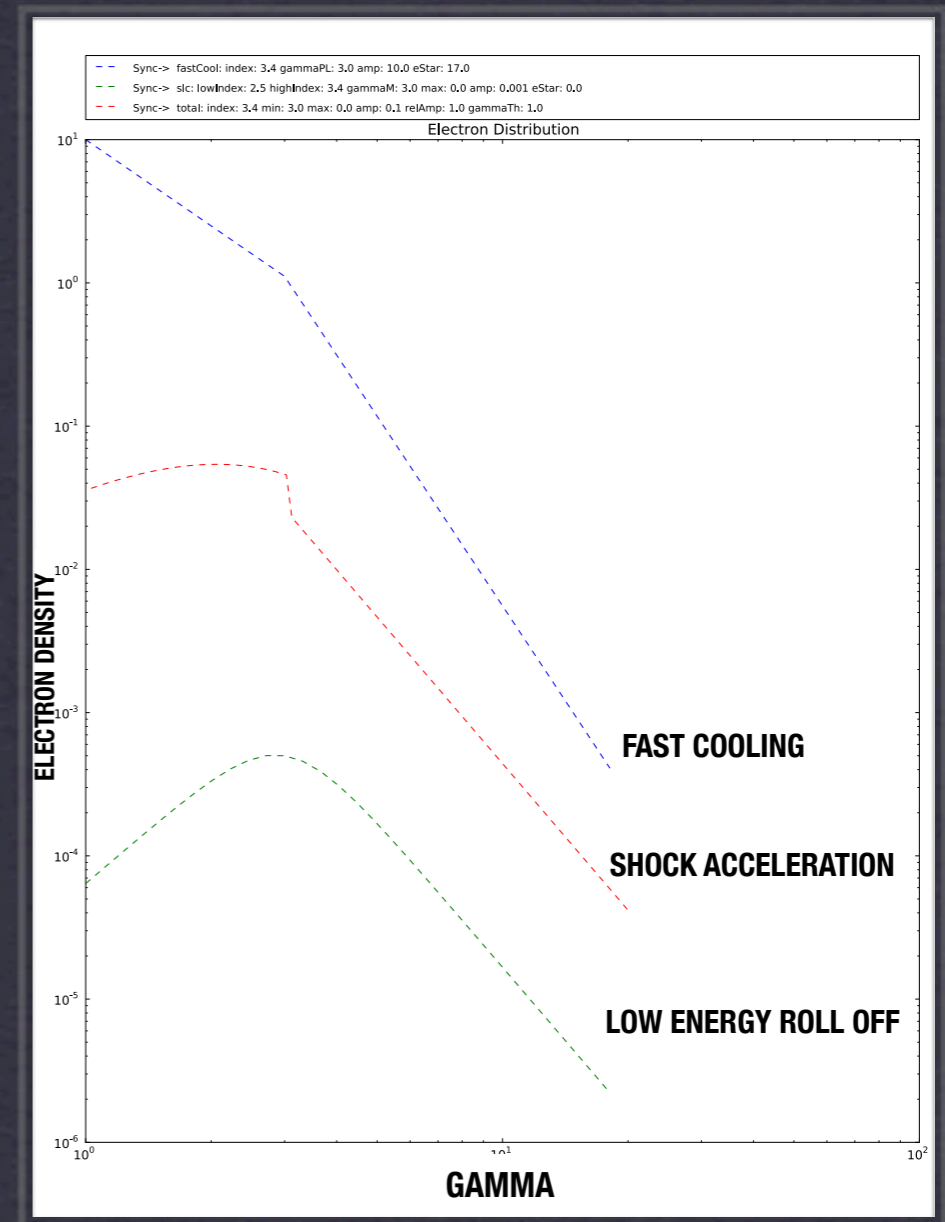
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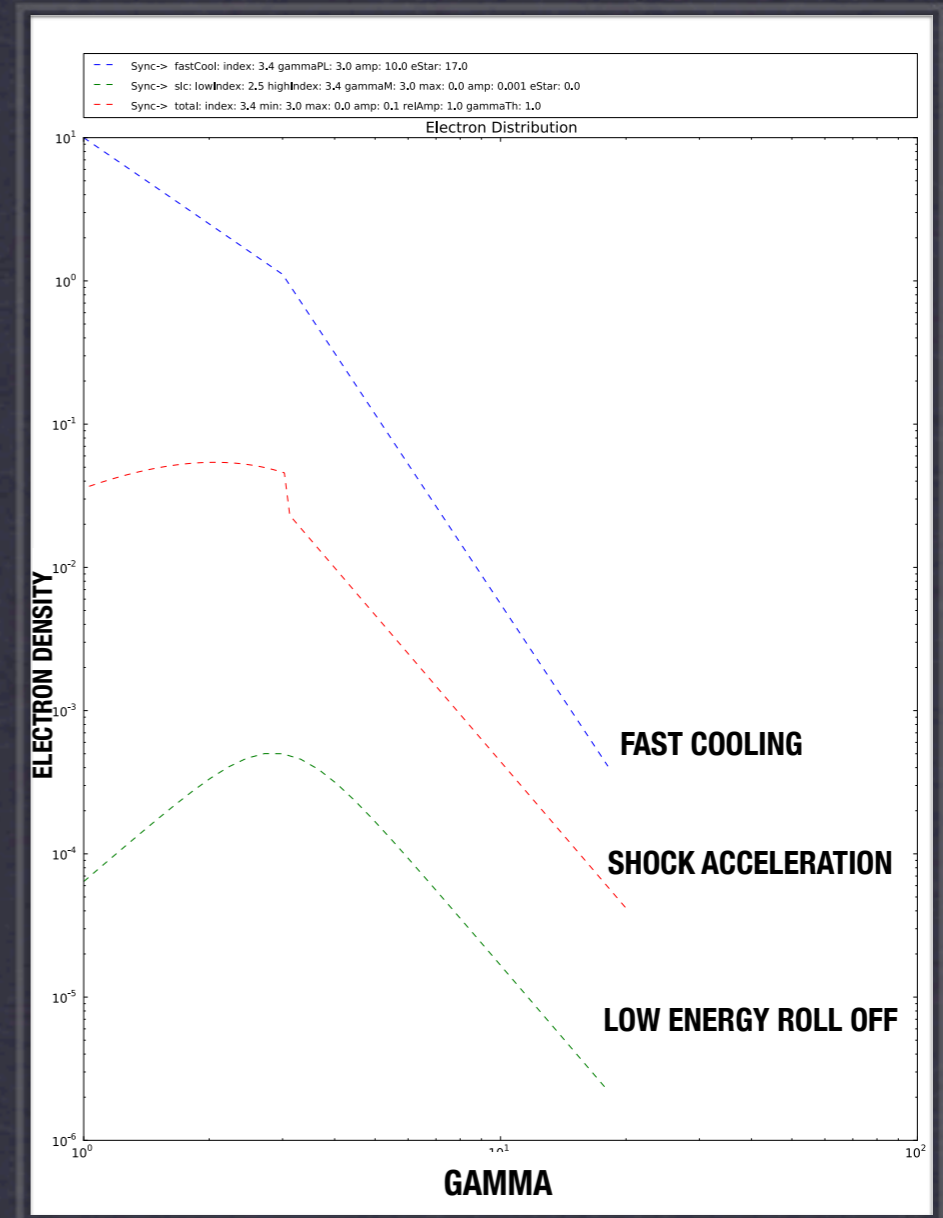
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$$\frac{\mathcal{E}_\gamma}{\mathcal{E}_* \gamma^2} \quad \mathcal{E}_* = \frac{3}{2} \frac{B}{B_{cr}} \Gamma \gamma_{th}^2 m_e c^2$$

Electron Distributions

SHOCK ACCELERATION

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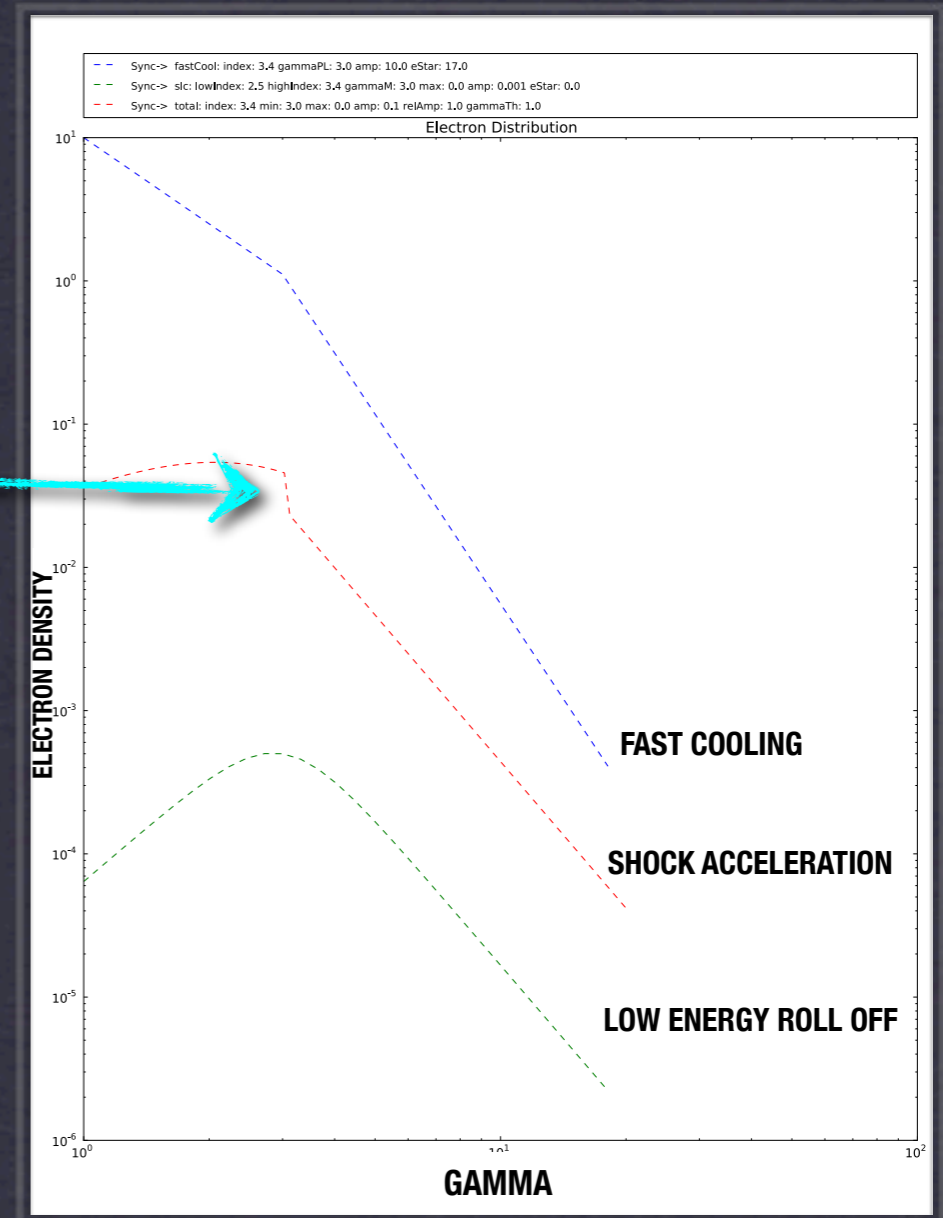
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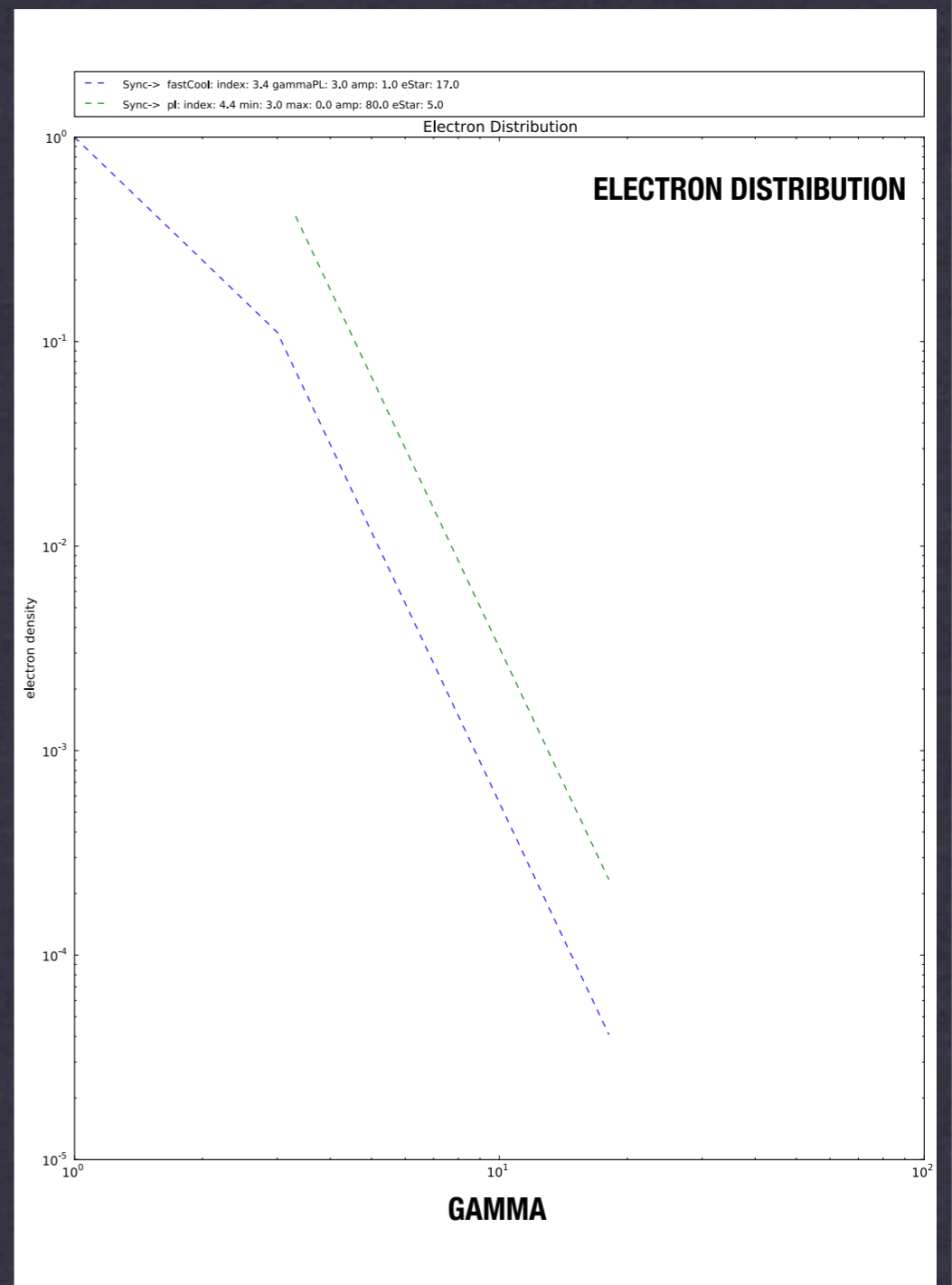
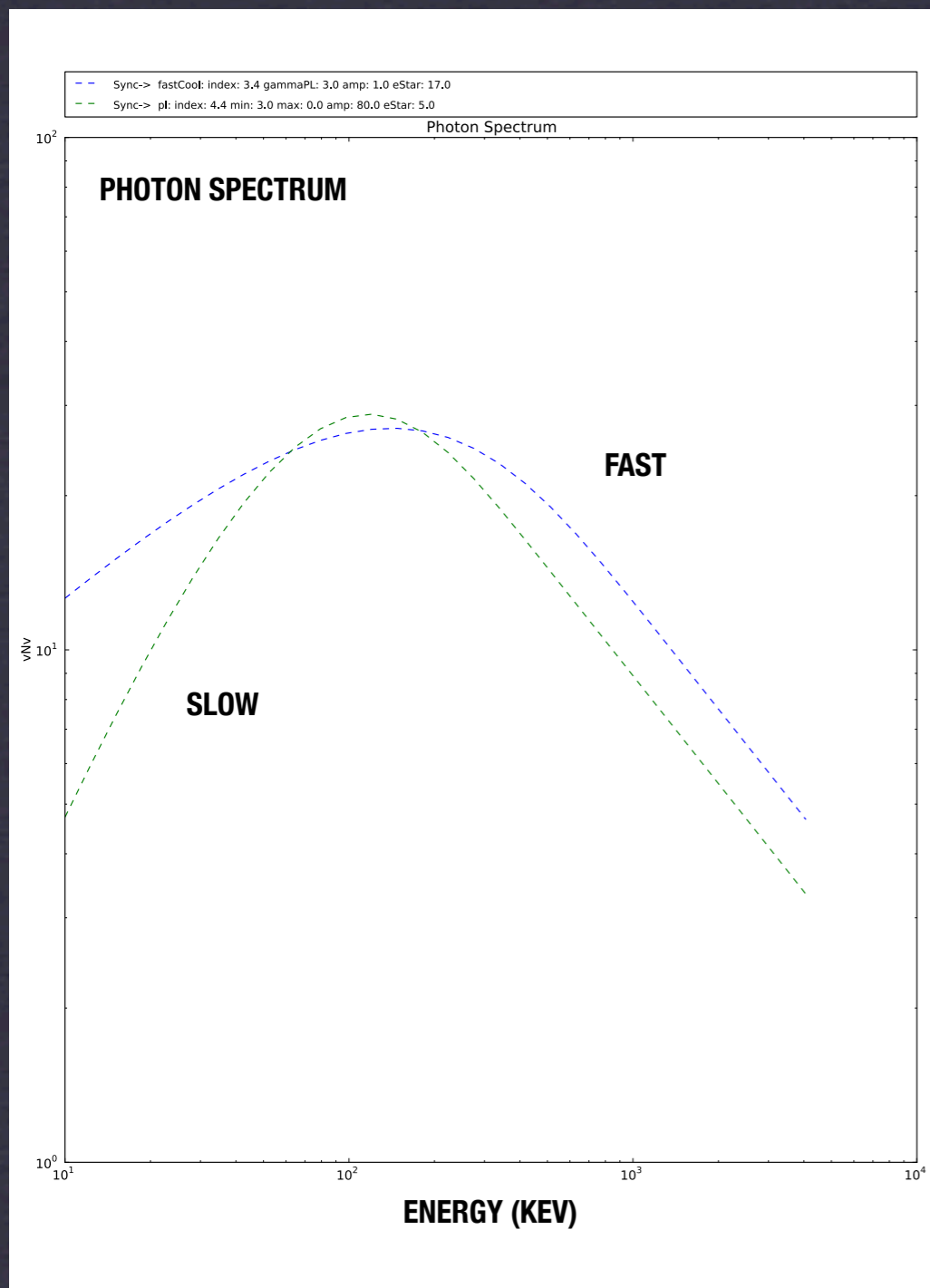
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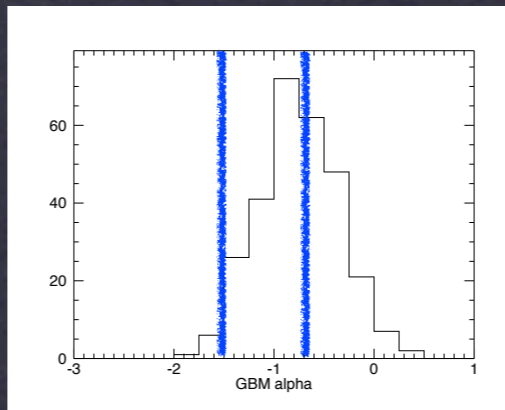
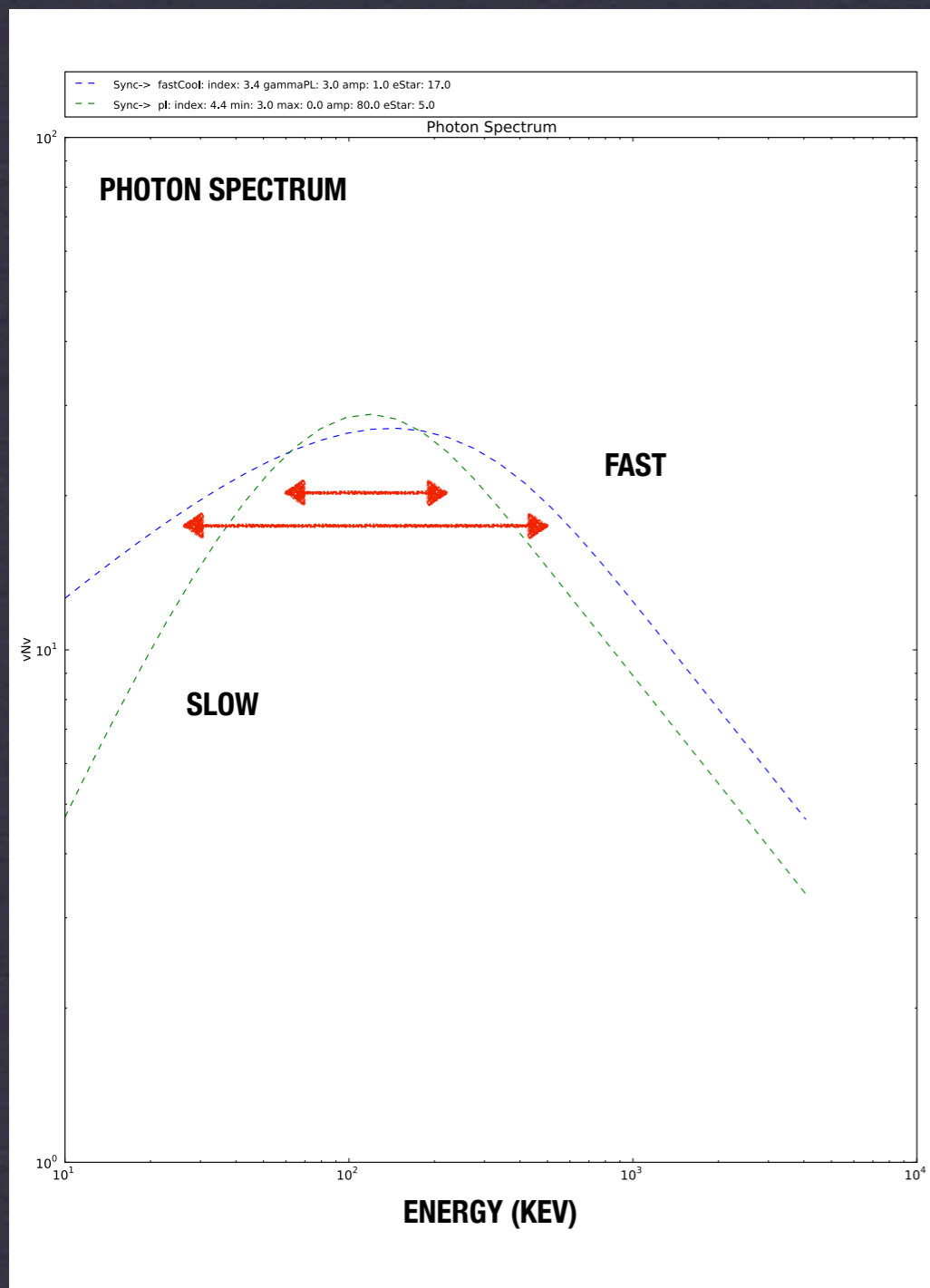
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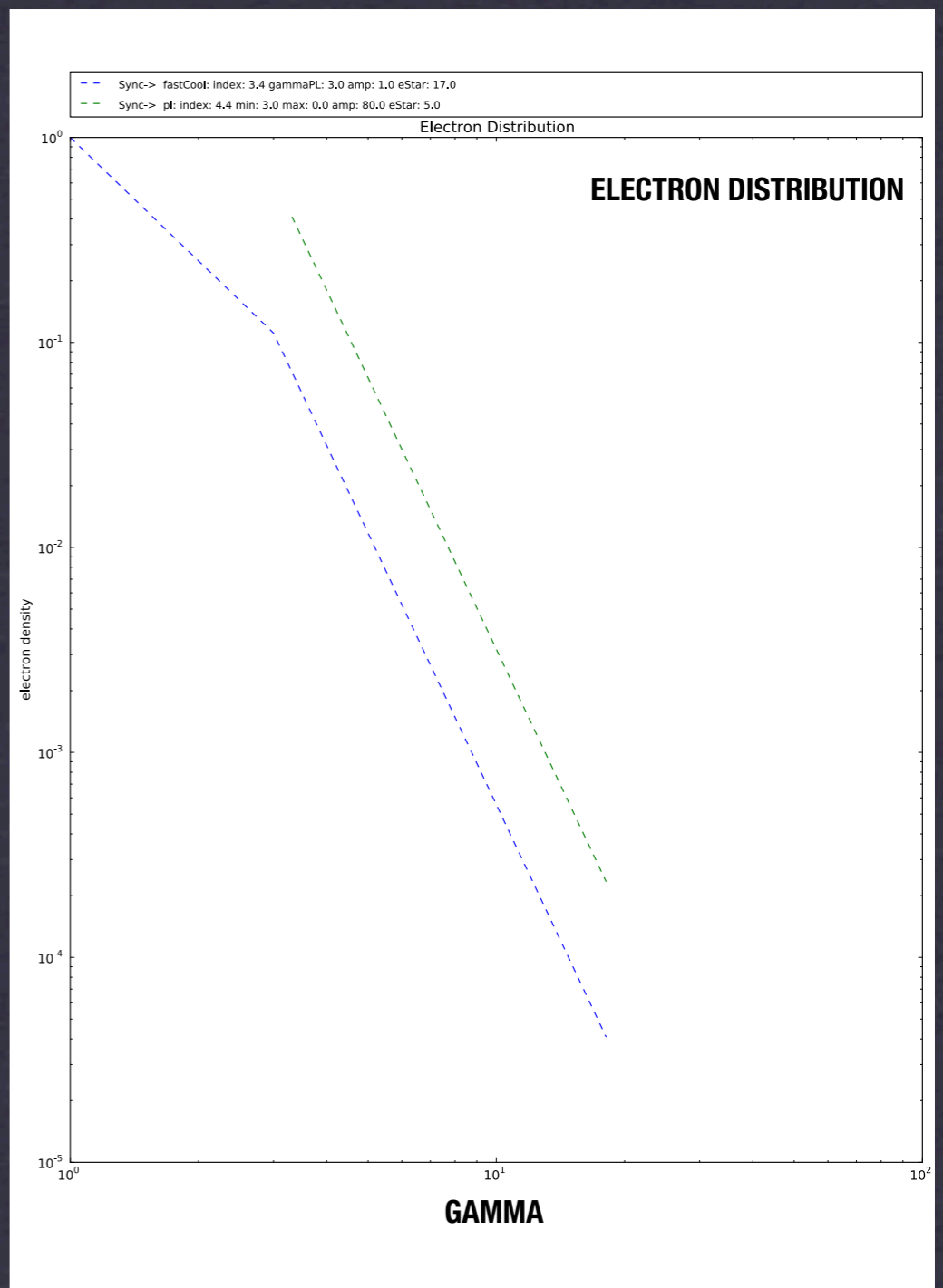
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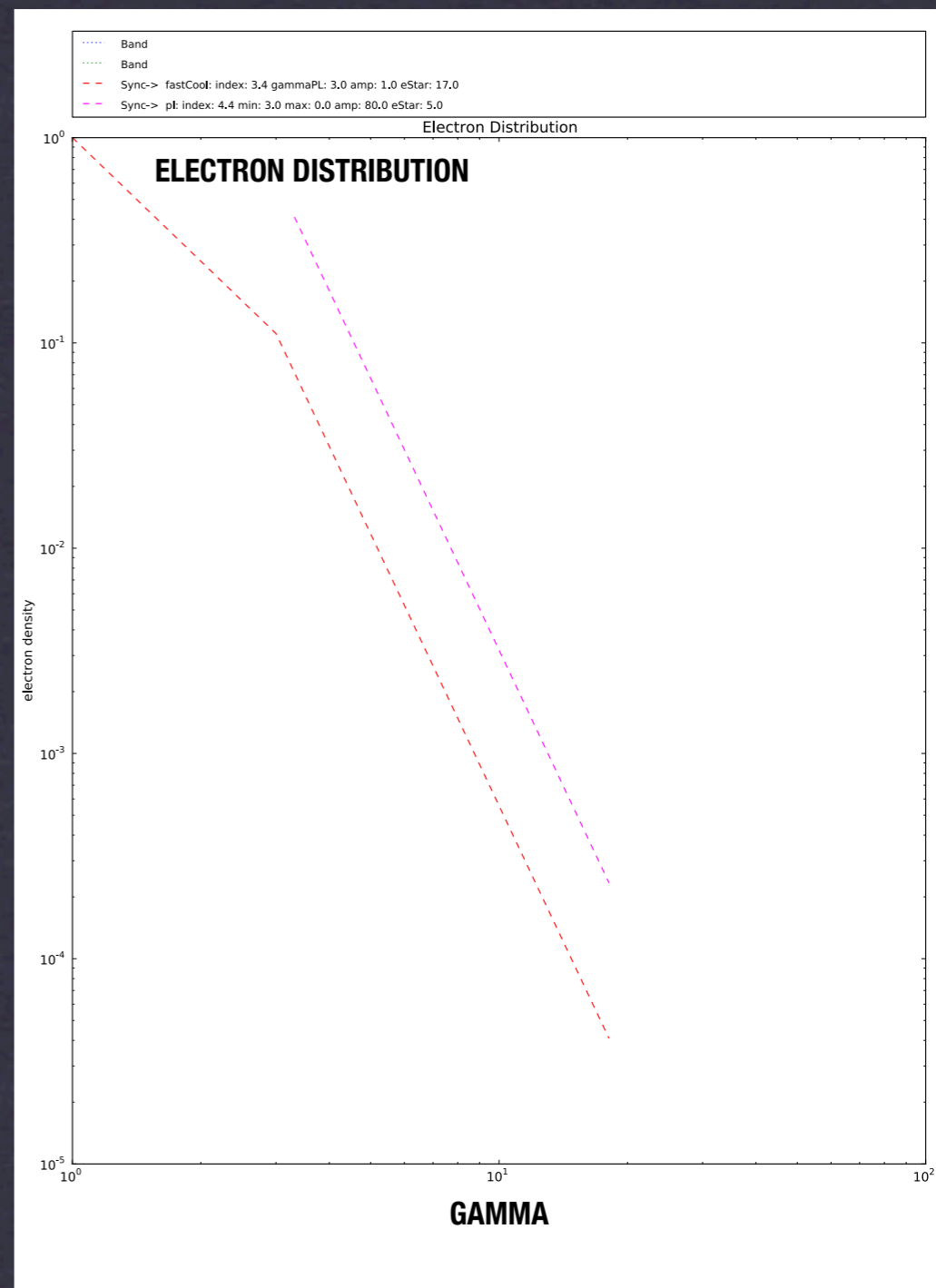
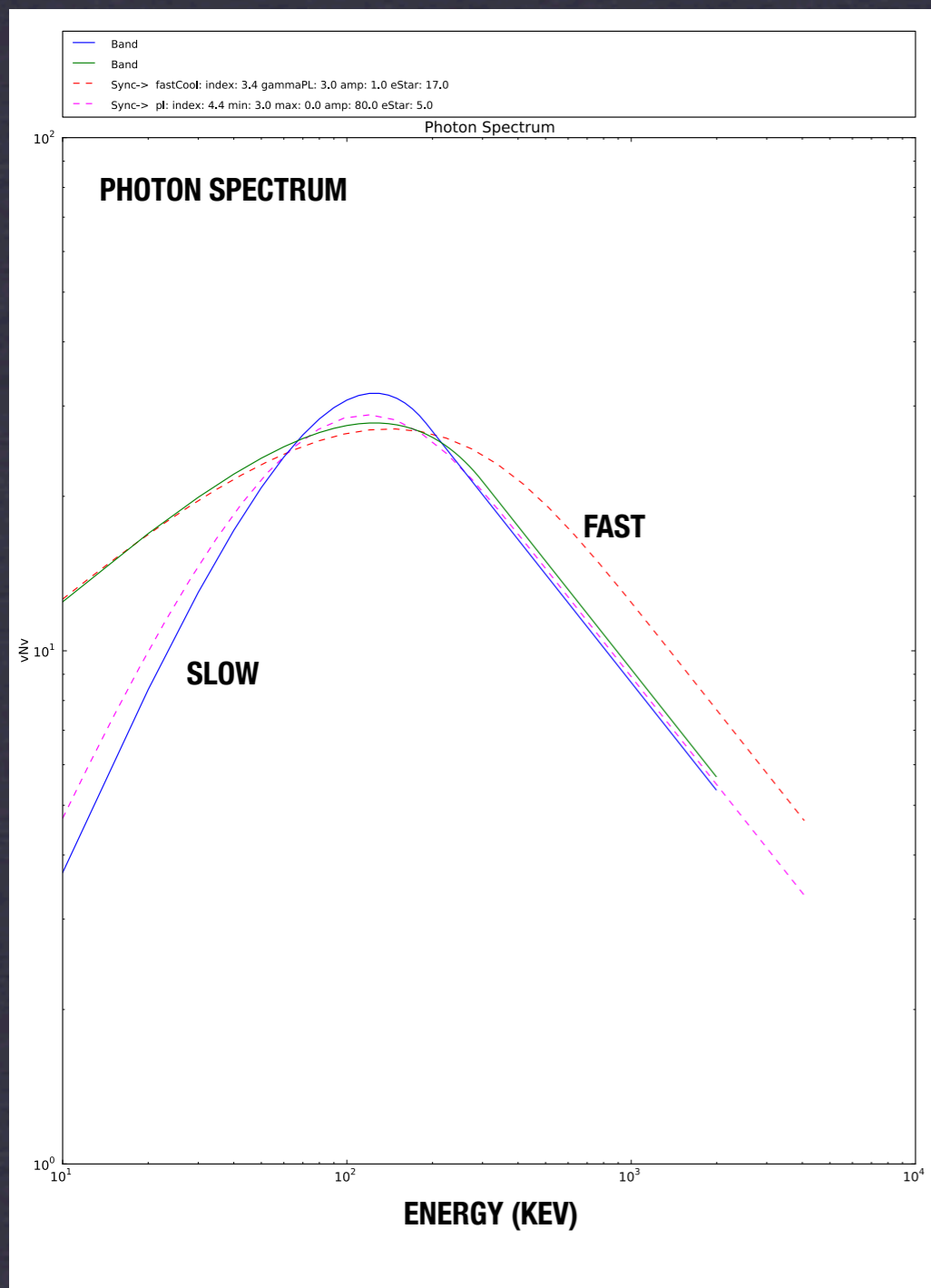
FAST OR SLOW?



GOLDSTEIN ET. AL. (IN PREP)



FAST OR SLOW?

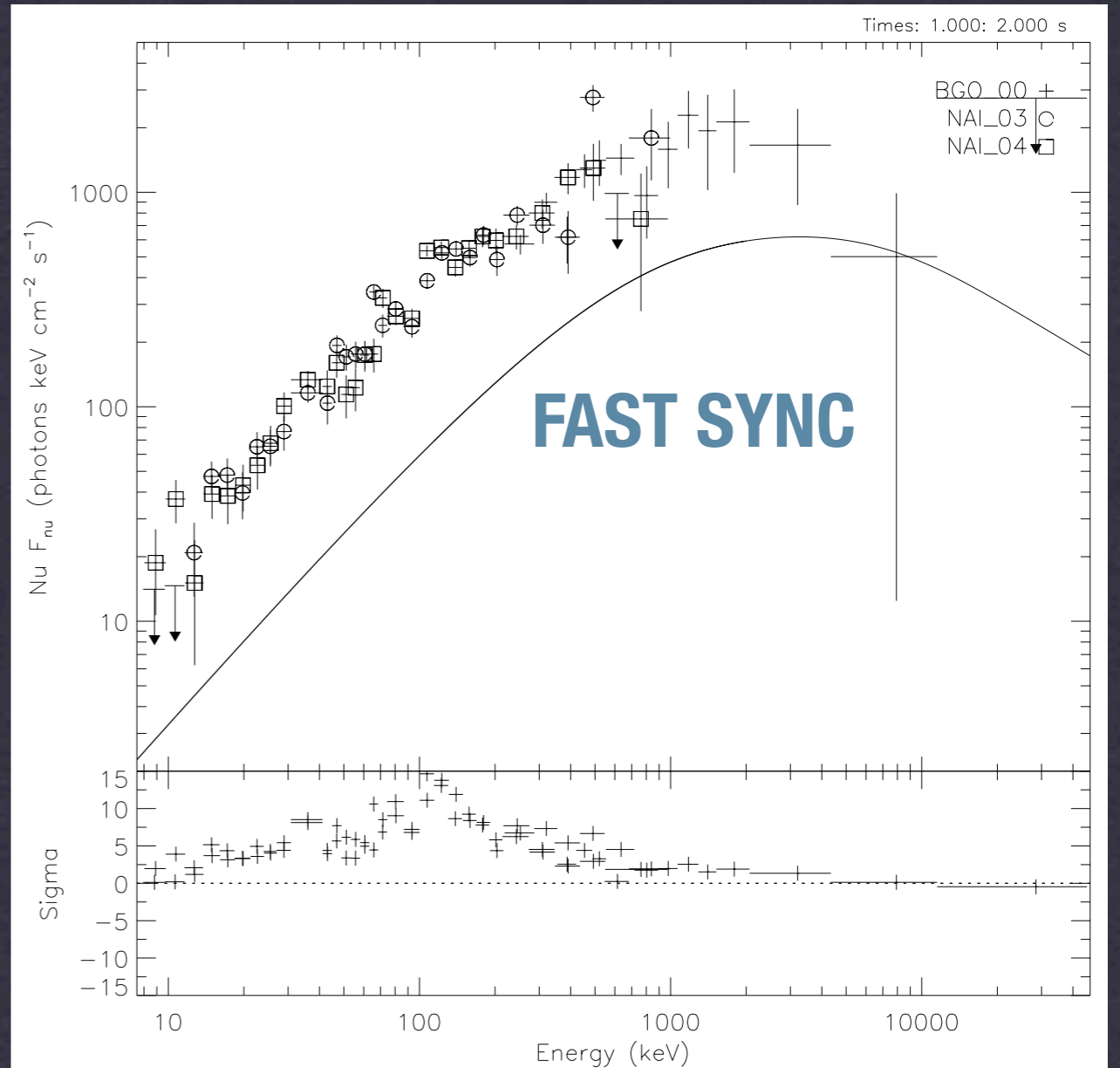


FAST OR SLOW?

FAST SYNCHROTRON IS MUCH BROADER THAN BAND AT THE PEAK

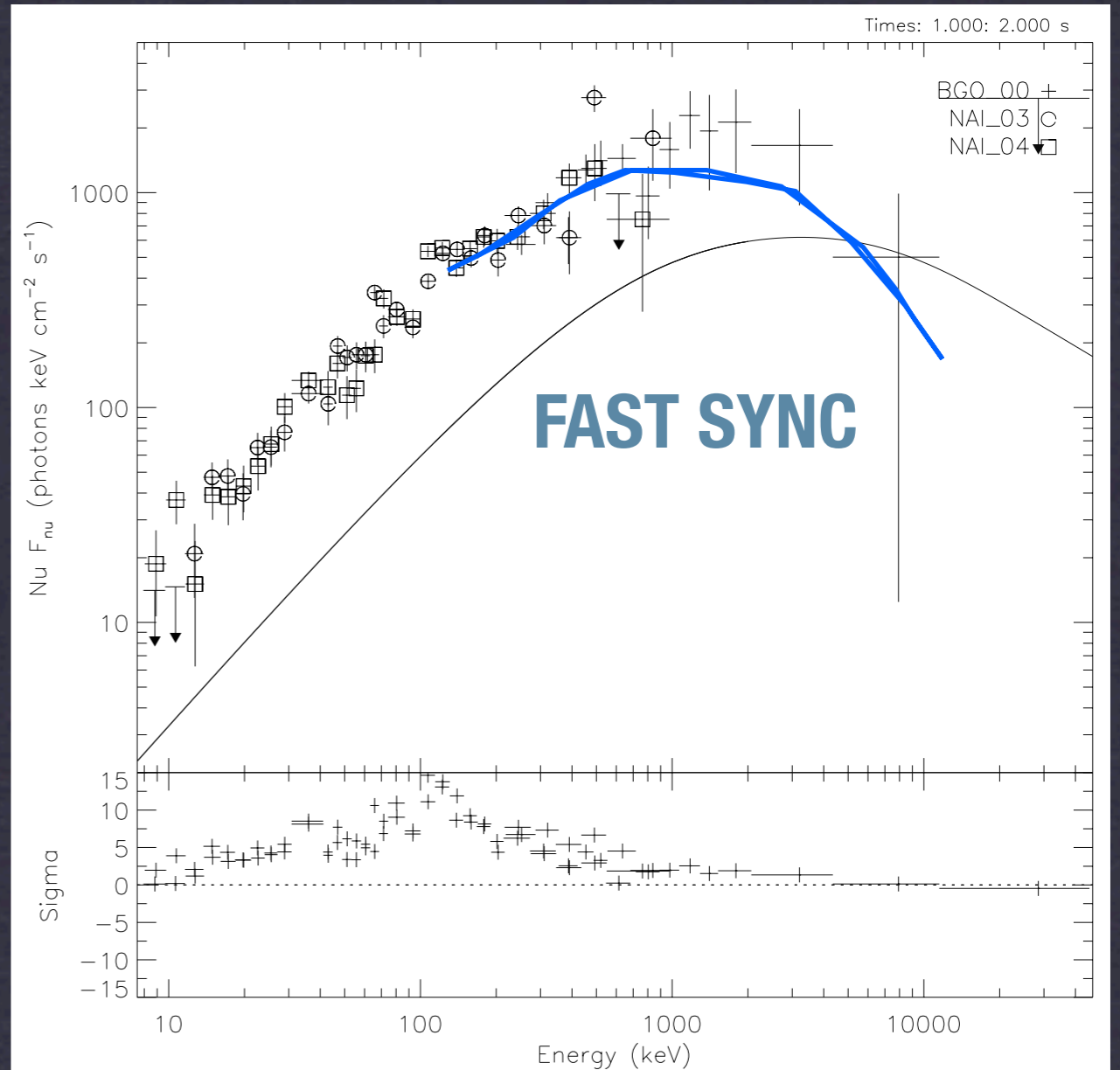
The Fast Conundrum

- Curvature is too broad to fit the prompt emission spectrum regardless of low-energy index for all bursts tried.
- Slow cooling spectrum implies electrons are being re-energized.



The Fast Conundrum

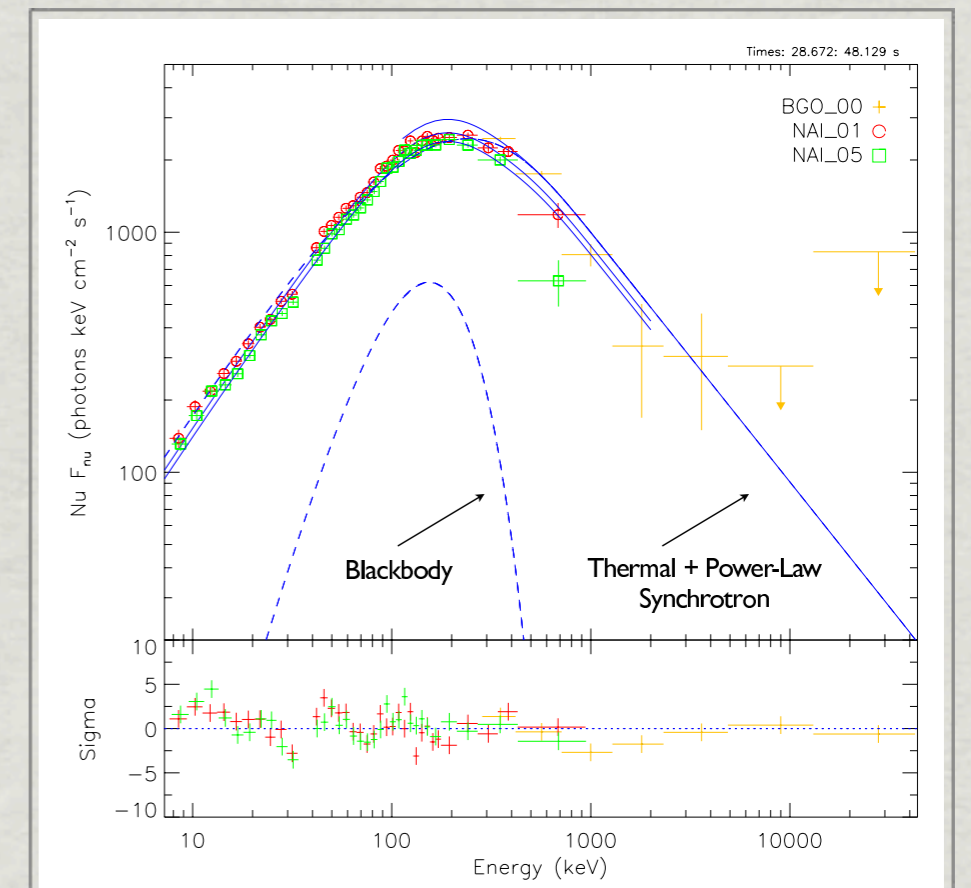
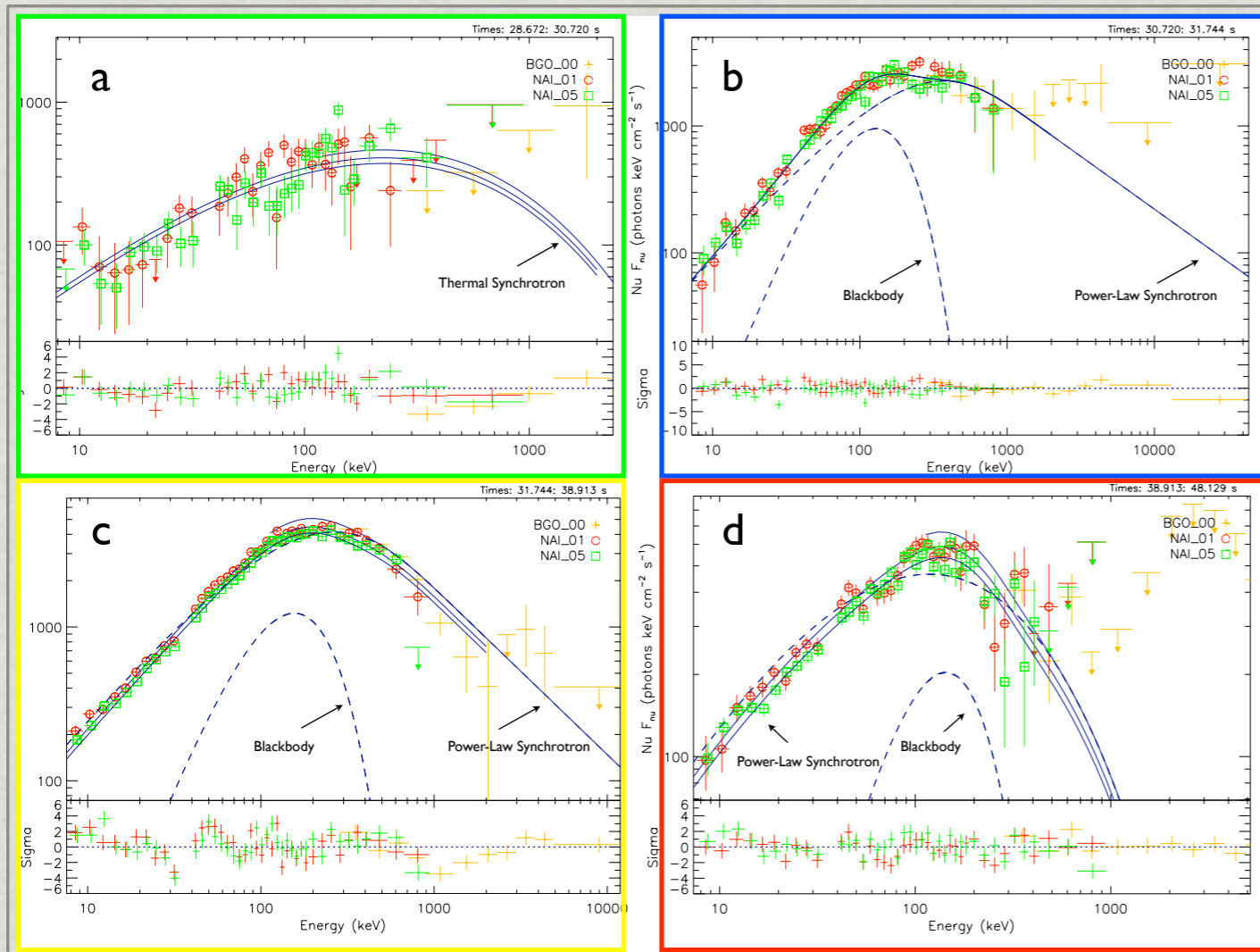
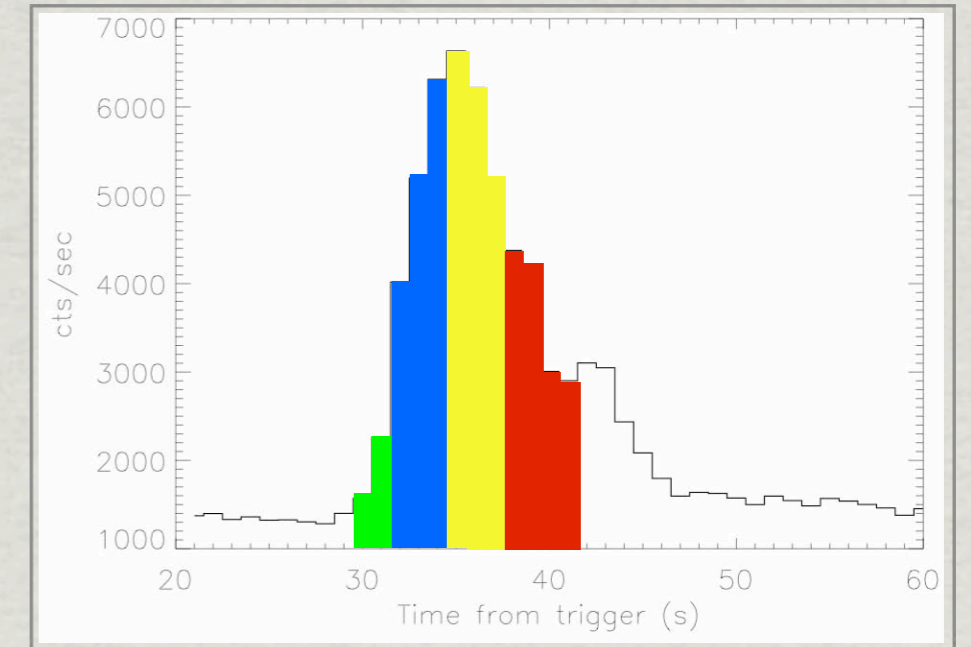
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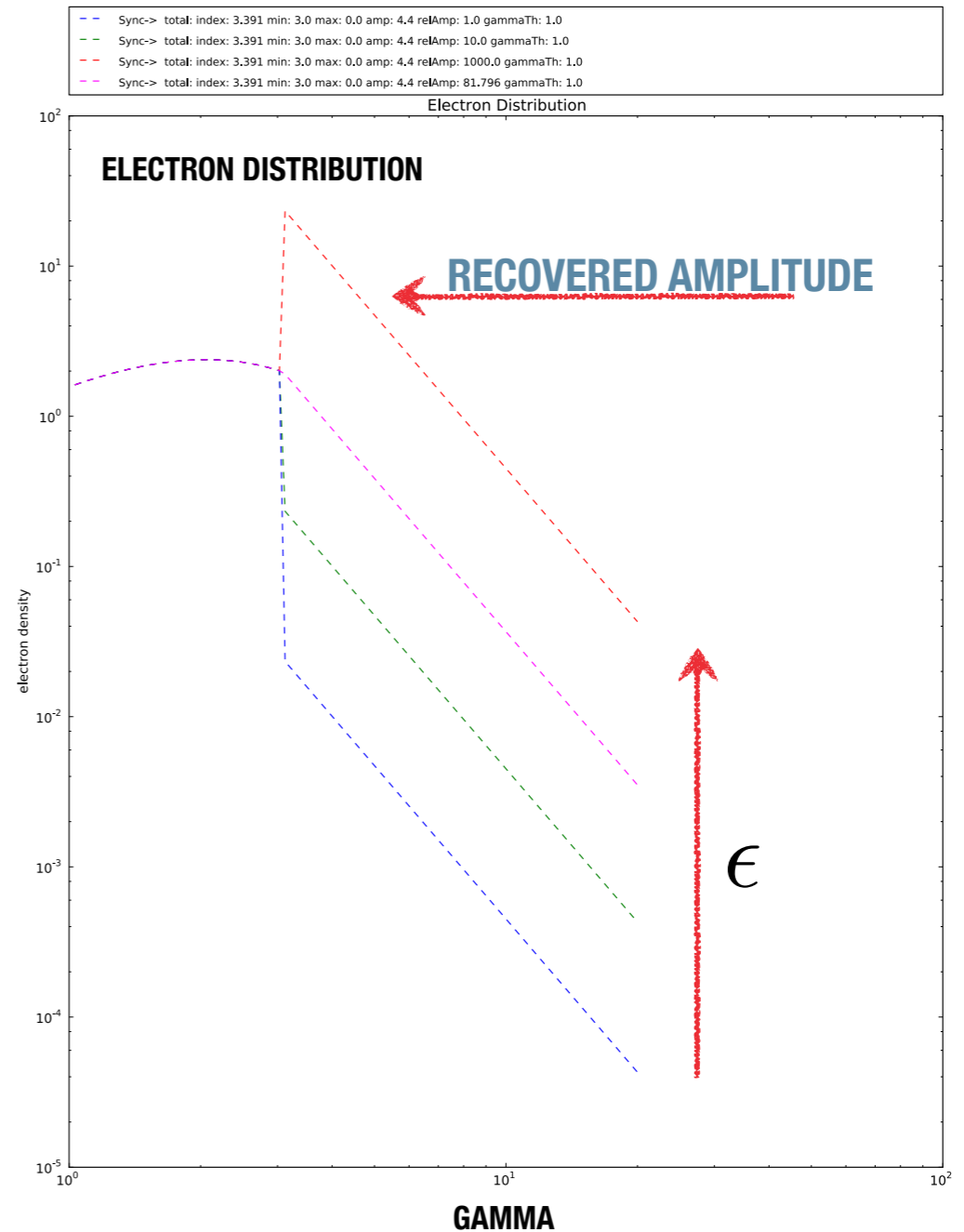
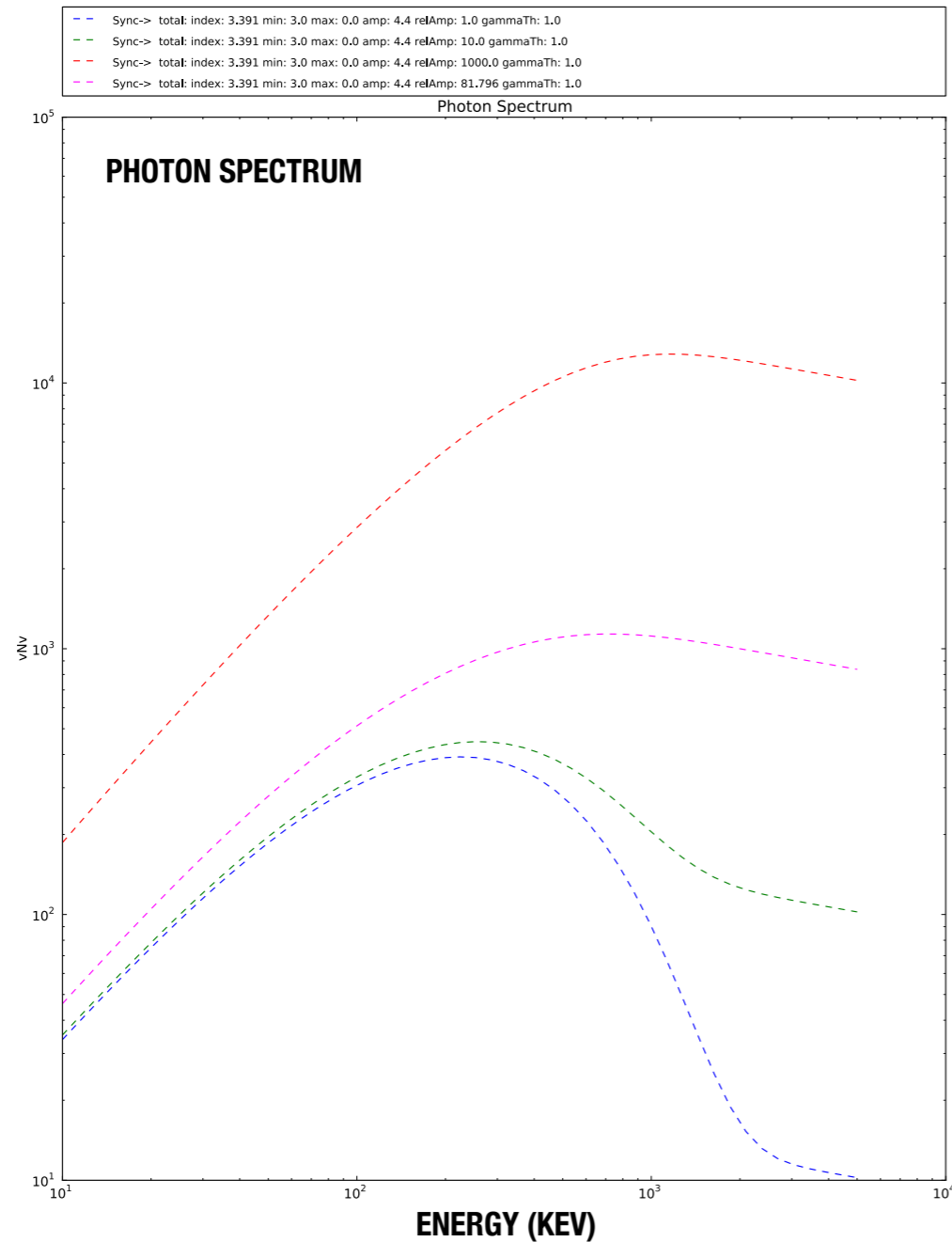


GRB090820A

- SPECTRUM STATISTICALLY BEST DESCRIBED BY SYNCHROTRON AND AN ADDITIONAL BLACKBODY
- EXCESS OF POWER-LAW ELECTRONS IN THE DISTRIBUTION
- TIME EVOLUTION OF THE ELECTRON DISTRIBUTION

BURGESS ET AL (SUBMITTED)

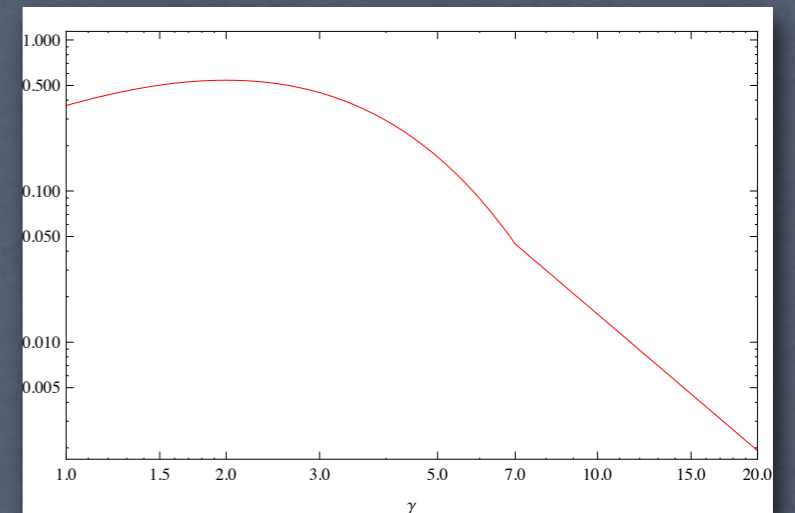
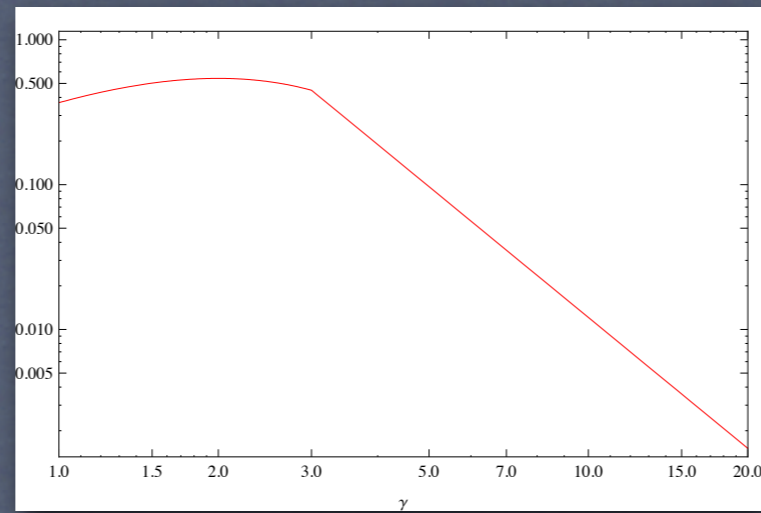
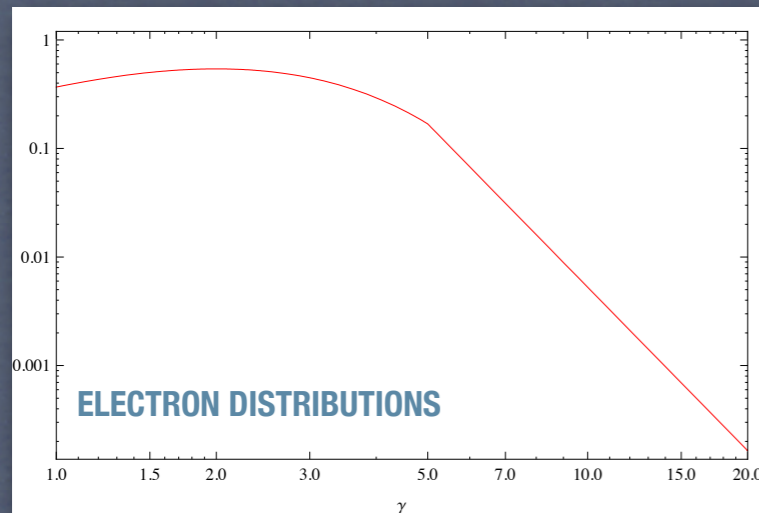




WHERE IS THE MAXWELLIAN?

Fixing the Amplitude

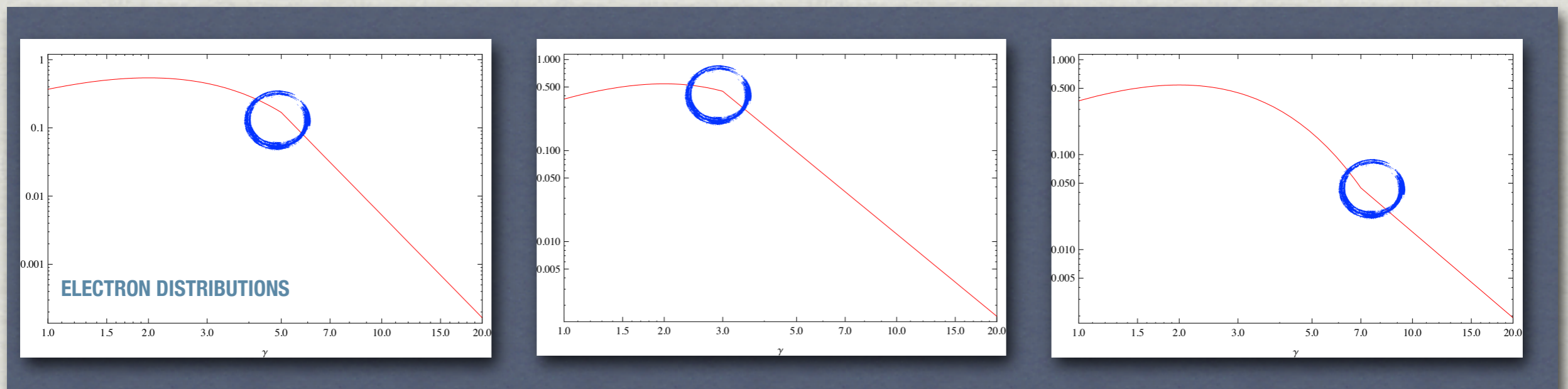
$$\epsilon = \eta^{2+\delta} e^{-\eta}$$



BY FIXING THE AMPLITUDE WE ELIMINATE A PARAMETER AND RECOVER A MORE PHYSICALLY MOTIVATED SPECTRUM

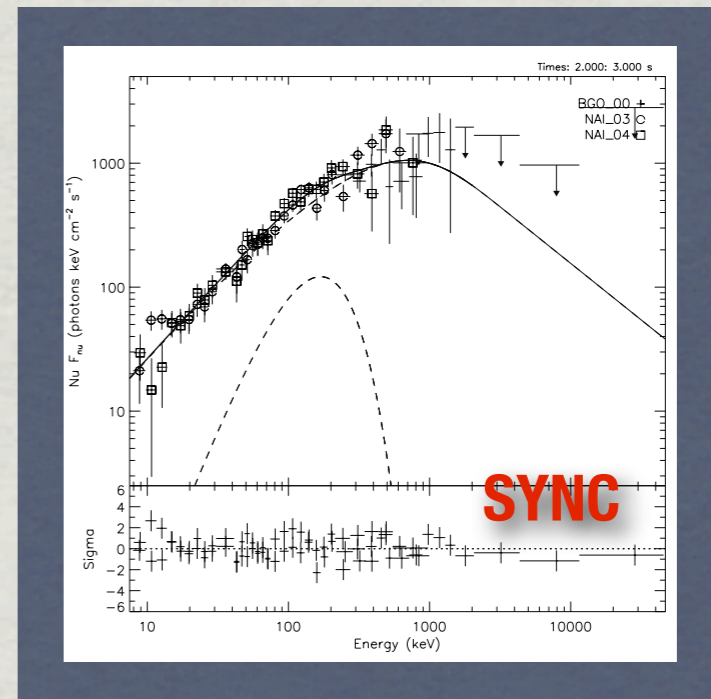
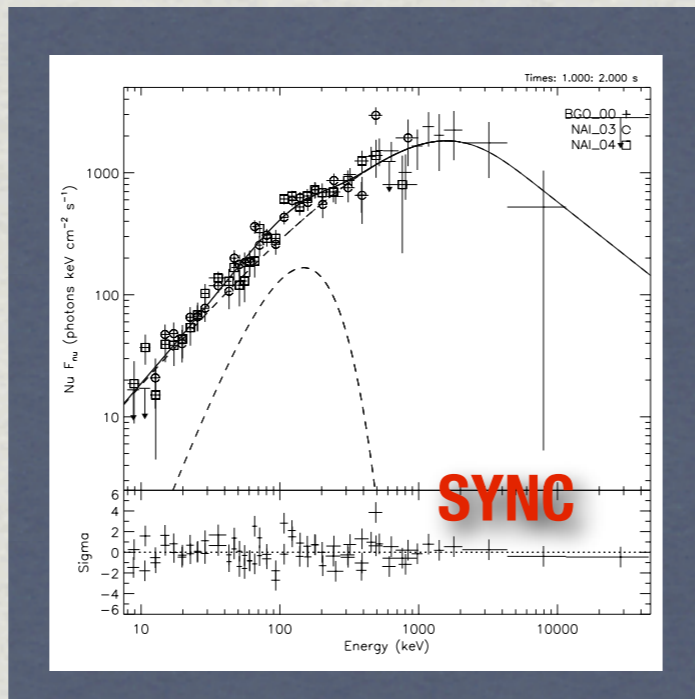
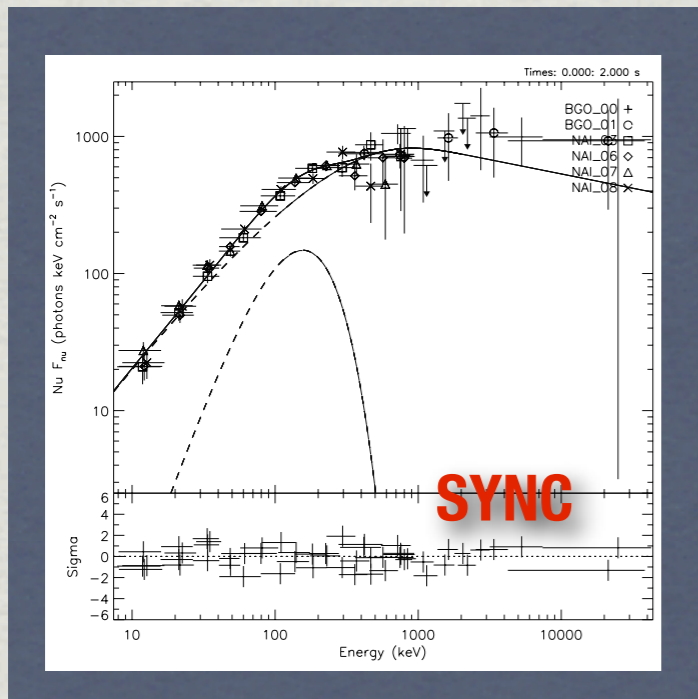
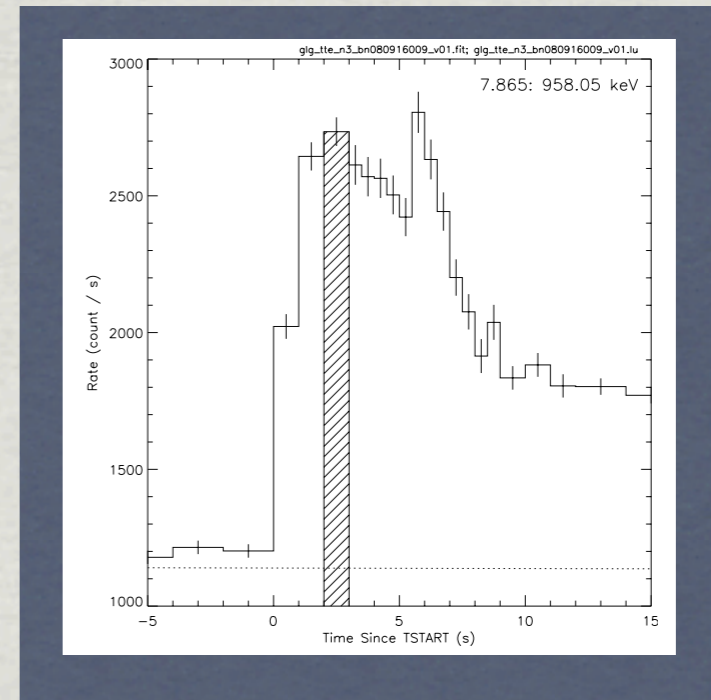
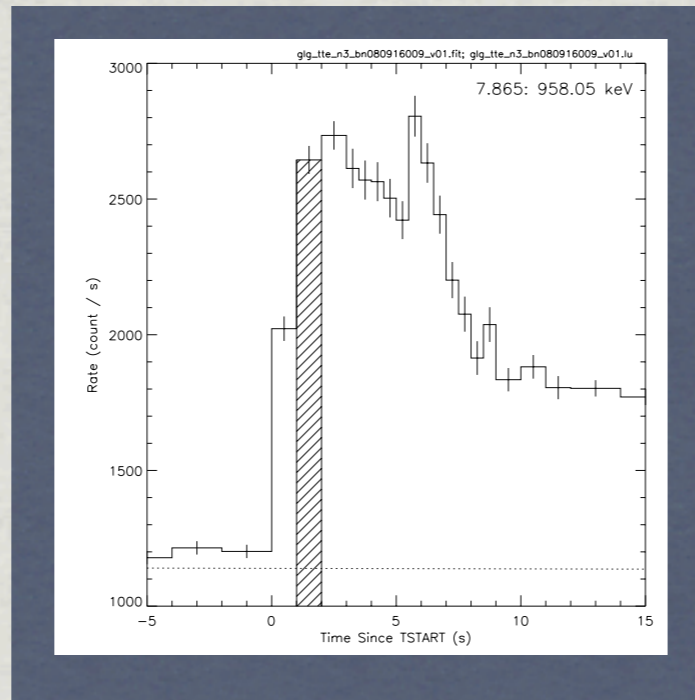
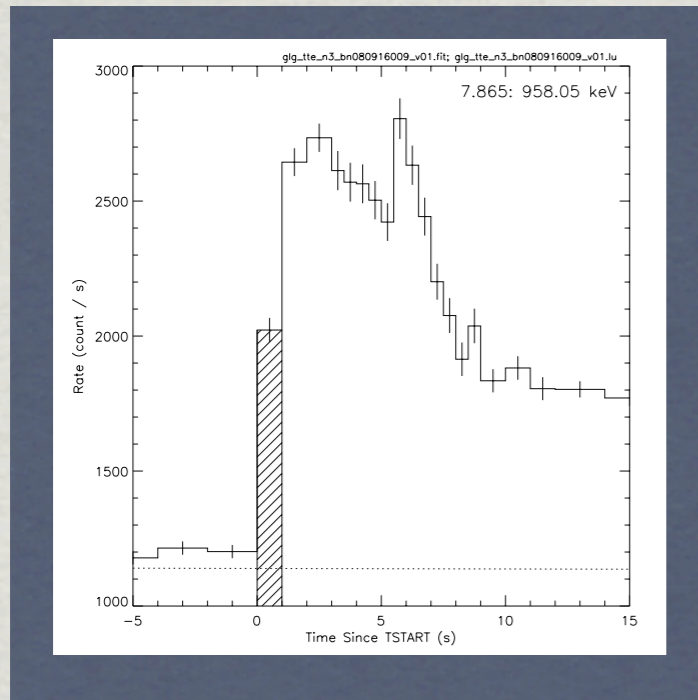
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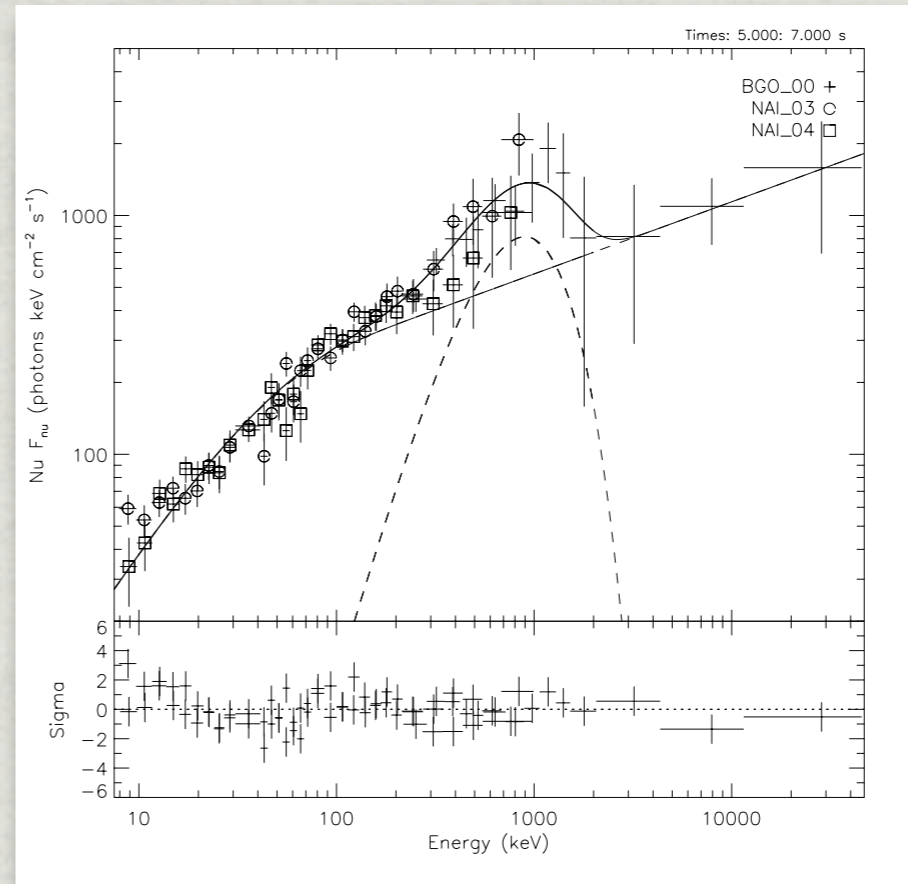
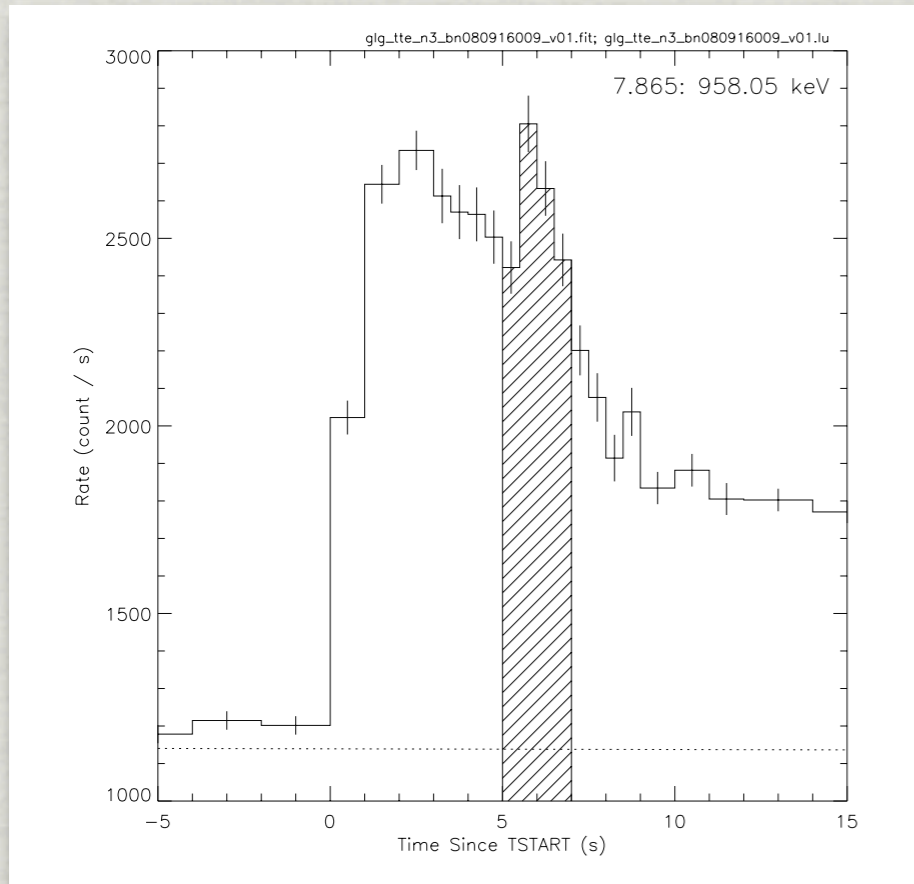
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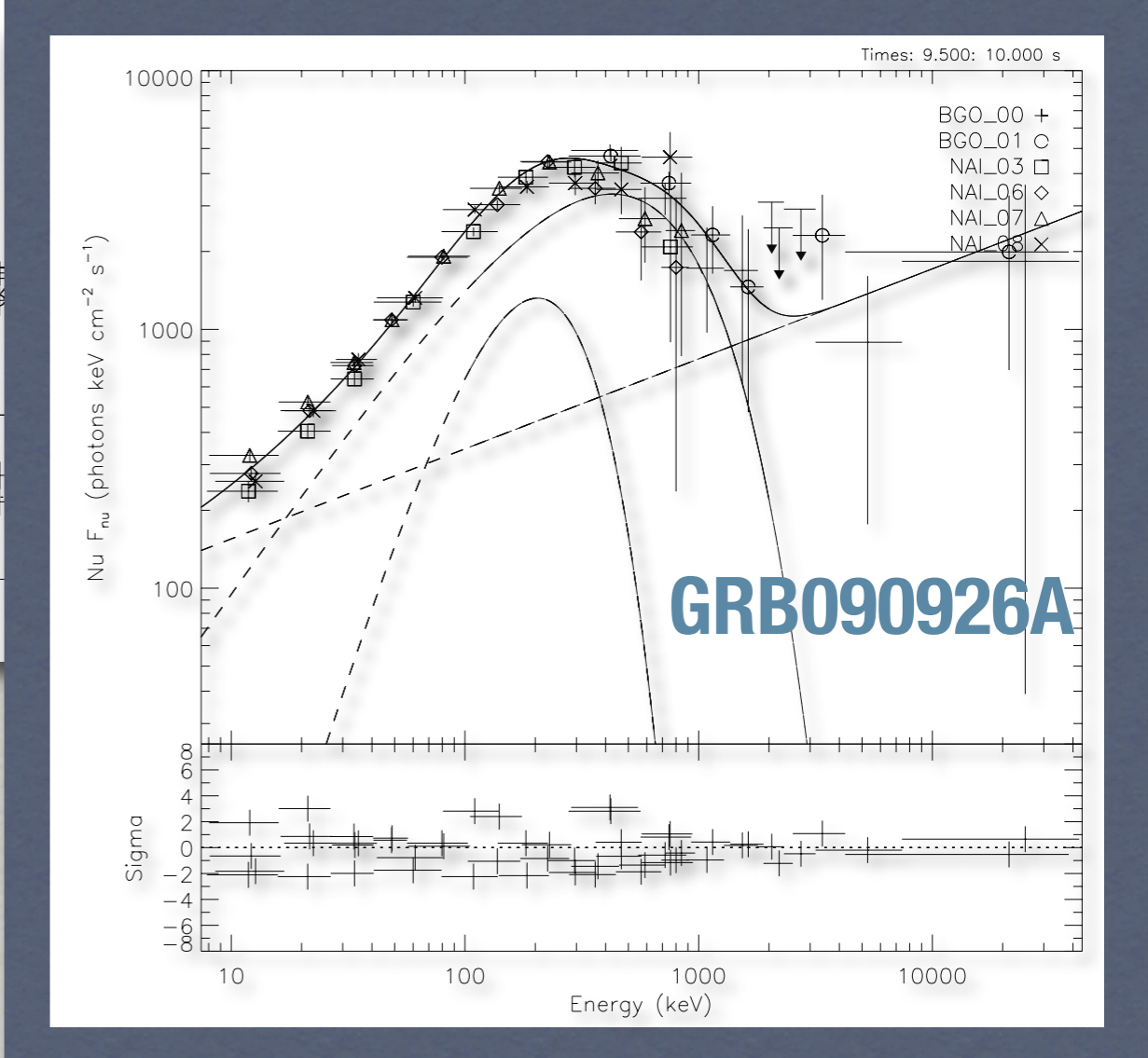
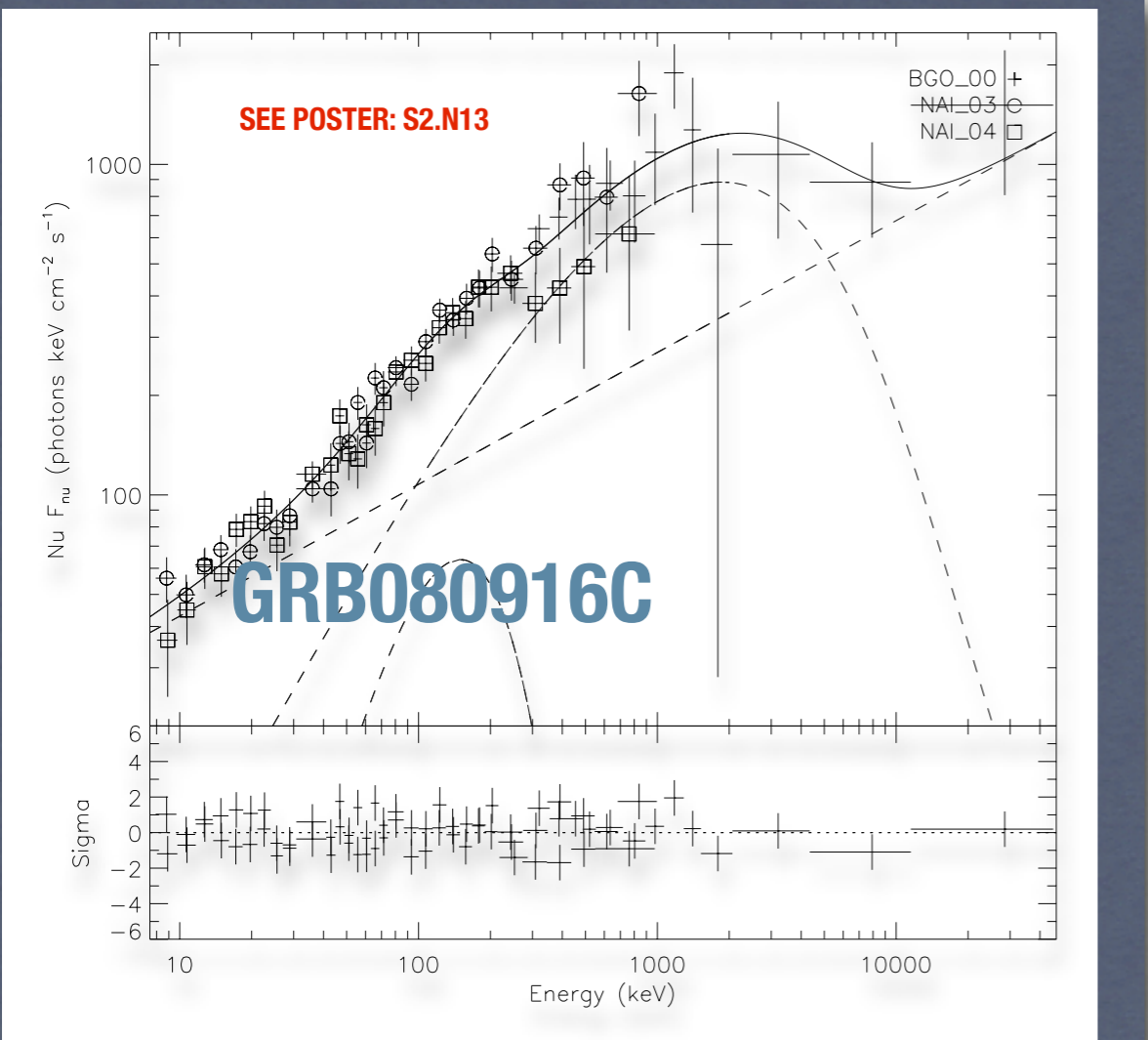
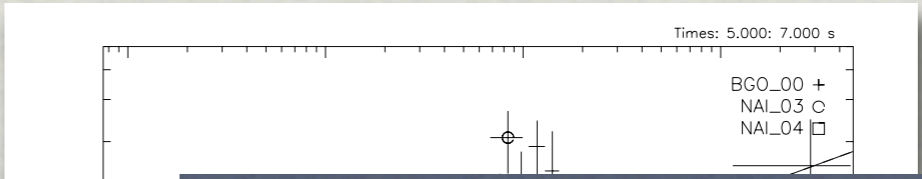
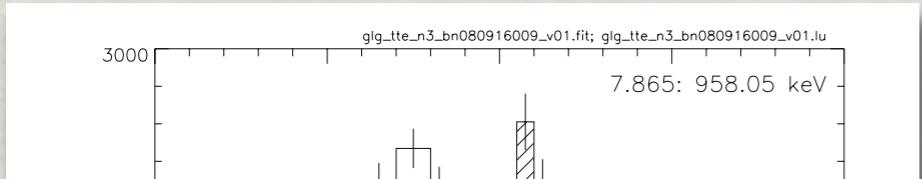
- SYNCHROTRON CEASES TO DESCRIBE THE NON-THERMAL SPECTRUM WELL.
- HIGH-ENERGY POWER-LAW CHANGES IN A NON-PHYSICAL WAY.
- INDICATION OF AN EXTRA-COMPONENT.

SYNCHROTRON + BB

CASTOR C-STAT = 394.07, DOF = 366

BAND + BB

CASTOR C-STAT = 375.00, DOF = 365



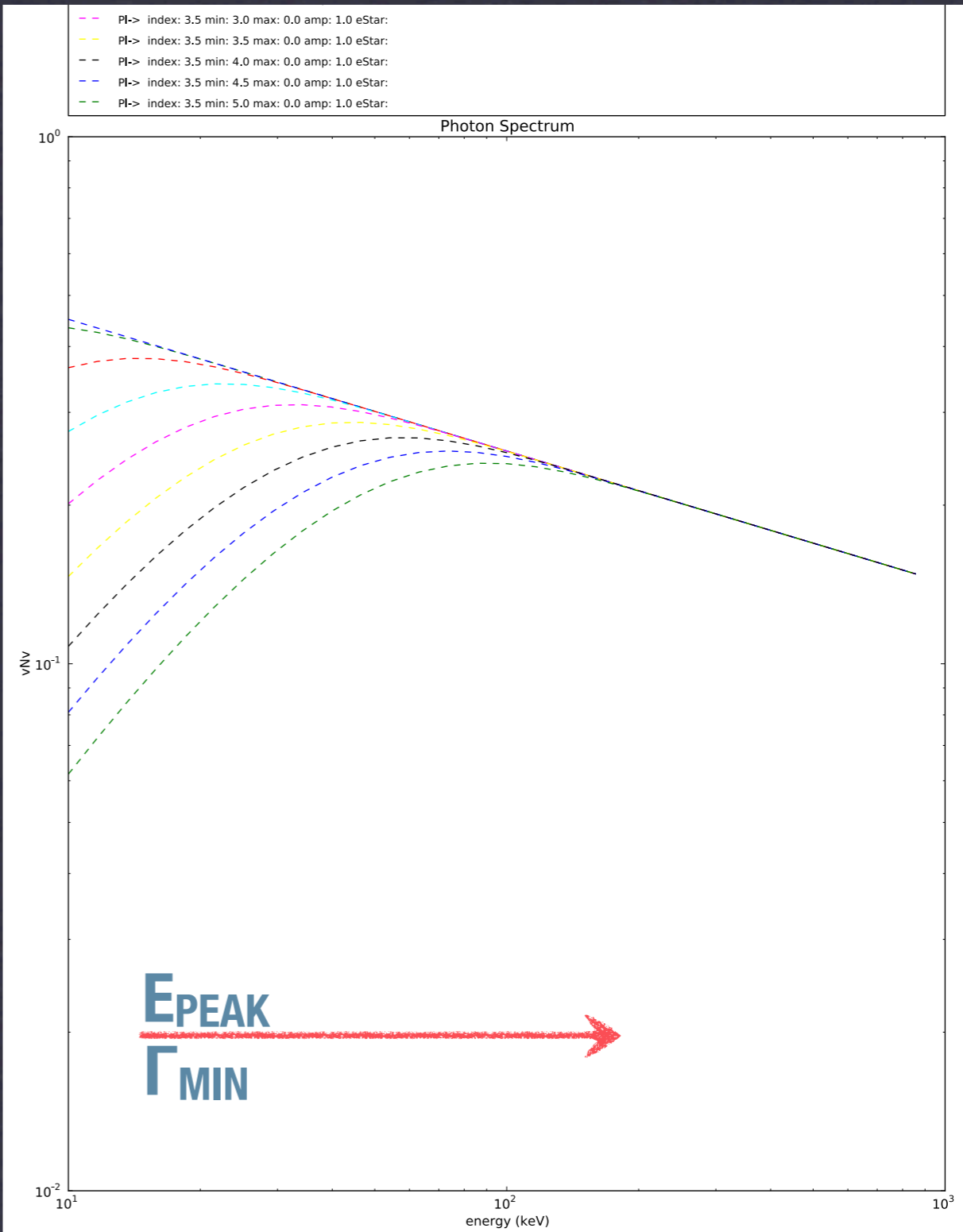
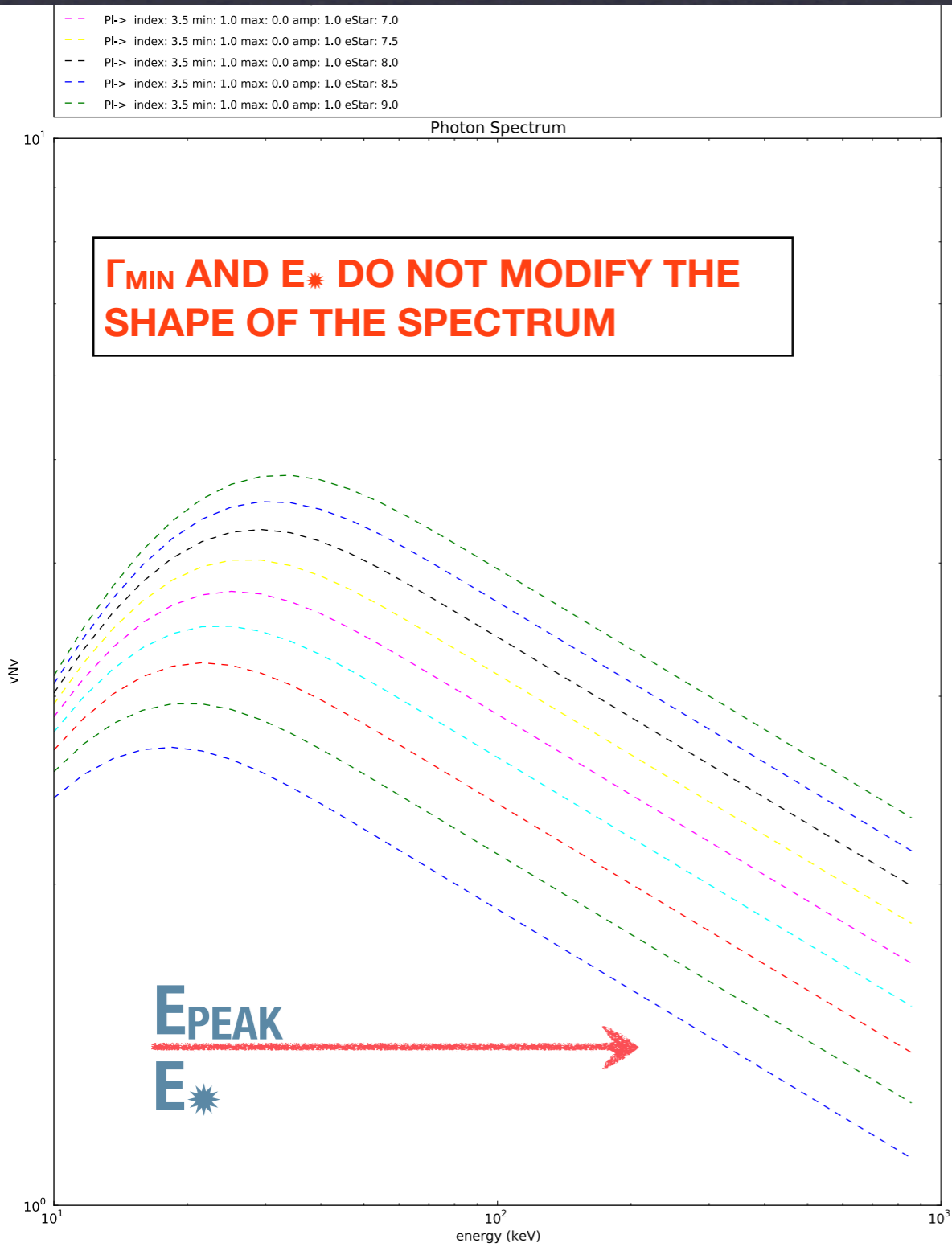
NON-PHYSICAL WAY.

- **INDICATION OF AN EXTRA-COMPONENT.**

Conclusions

- * Band function can be replaced by synchrotron in many cases.
- * Can resolve the Maxwellian peak if we assume that the electron distribution is continuous.
- * Curvature of the νF_{ν} peak is important when modeling spectra.
- * Fast cooling synchrotron is far too broad to be the main non-thermal emission component in GRB prompt emission.
- * Synchrotron fits consistent with multi-component fits attempted.
- * Physical fits with other models and the high-energy component coming soon...

Backup slides

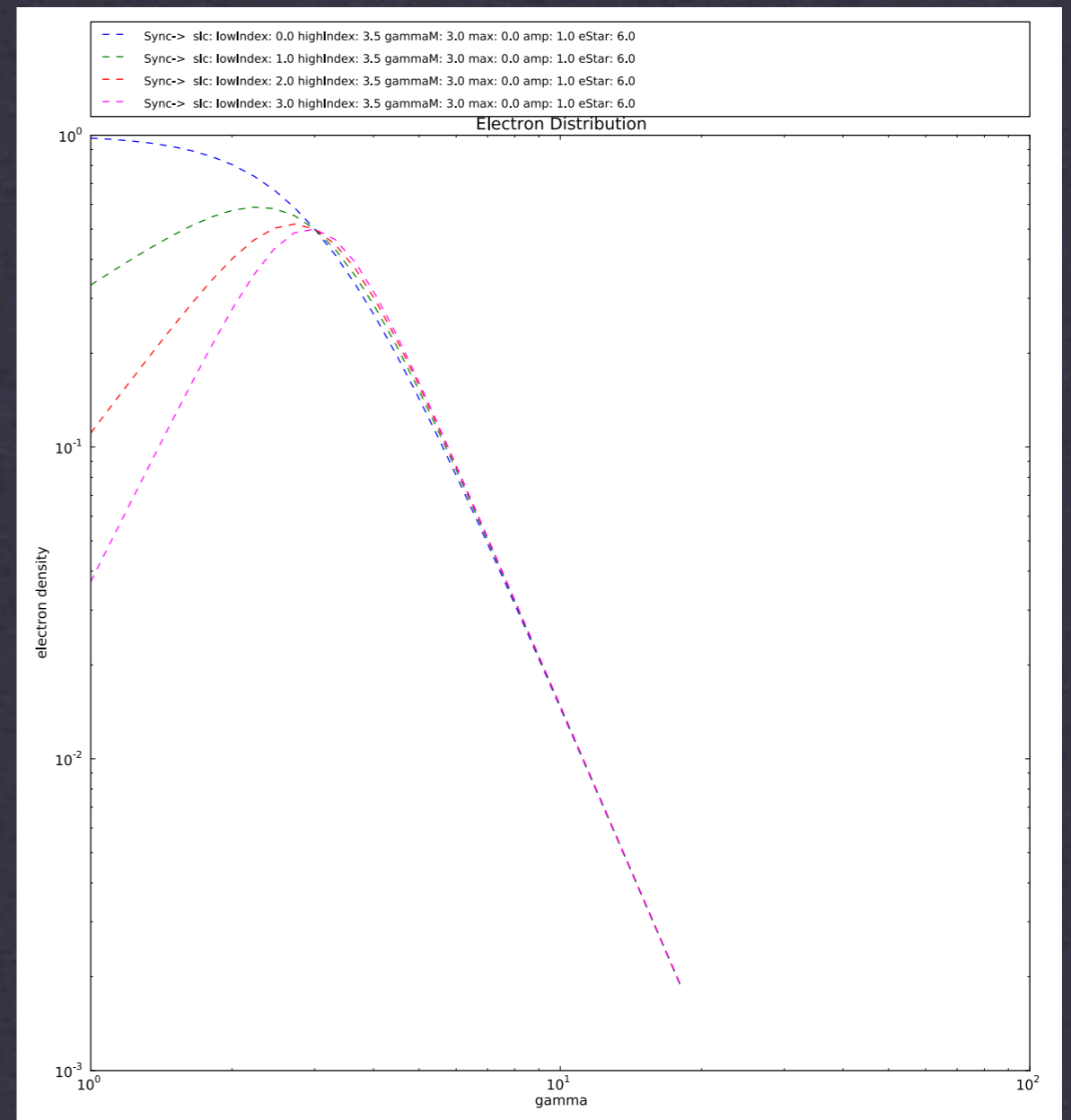


CORRELATIONS

UNABLE TO RESOLVE MINIMUM LORENTZ FACTOR AND E_{star} SIMULTANEOUSLY

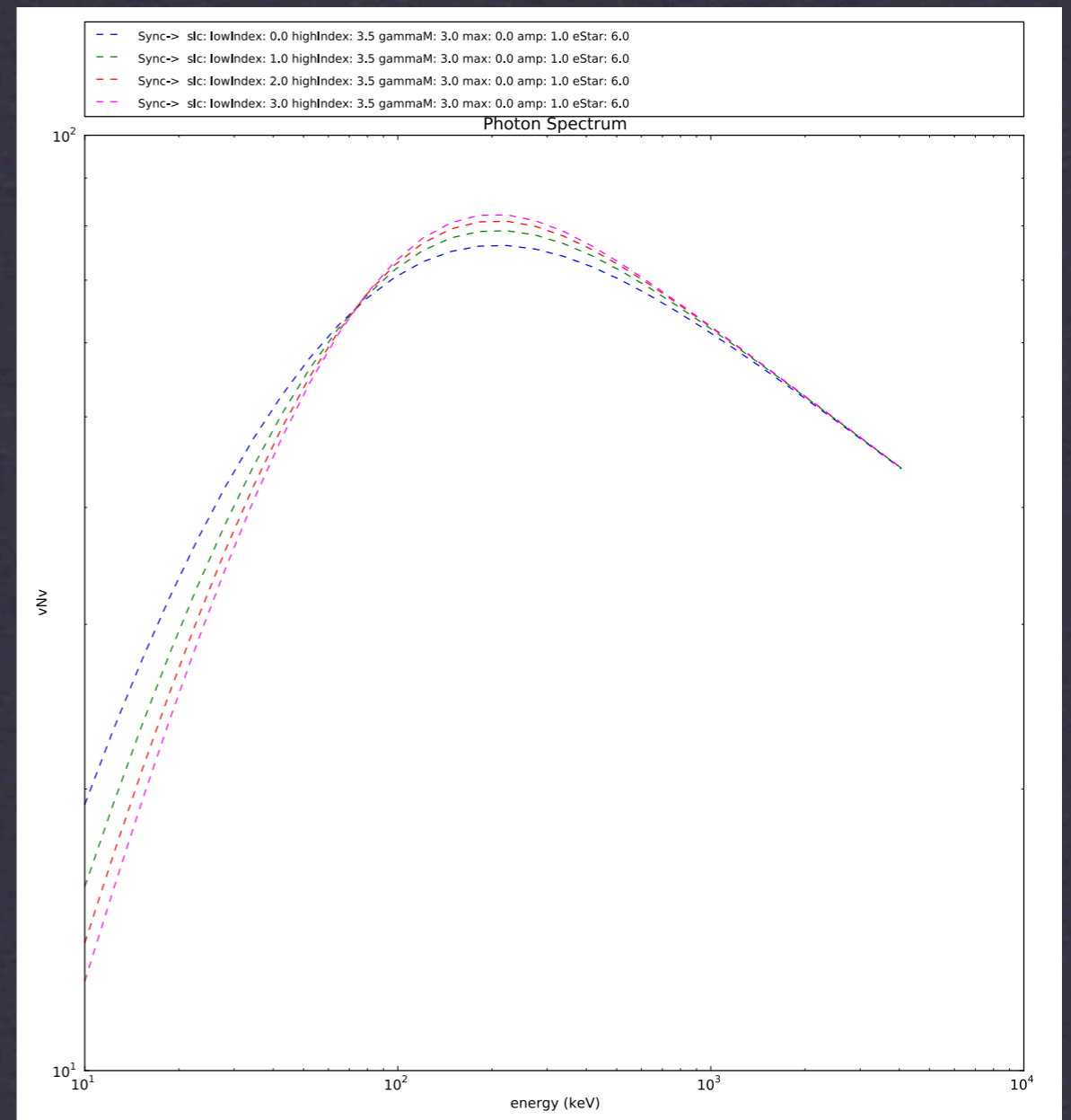
The Low-Energy Index

- Adding an extra parameter helps improve the fit however not significantly ($\Delta C\text{-Stat} \sim 1$)
- Most parameters must be fixed to have constrained fits.

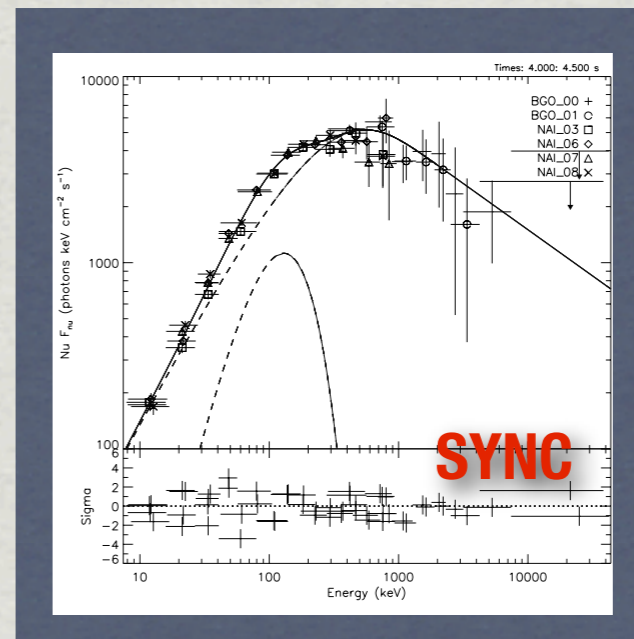
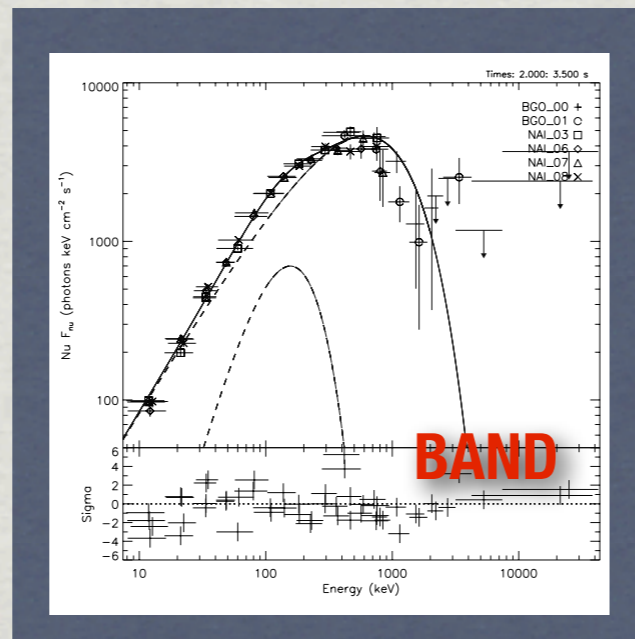
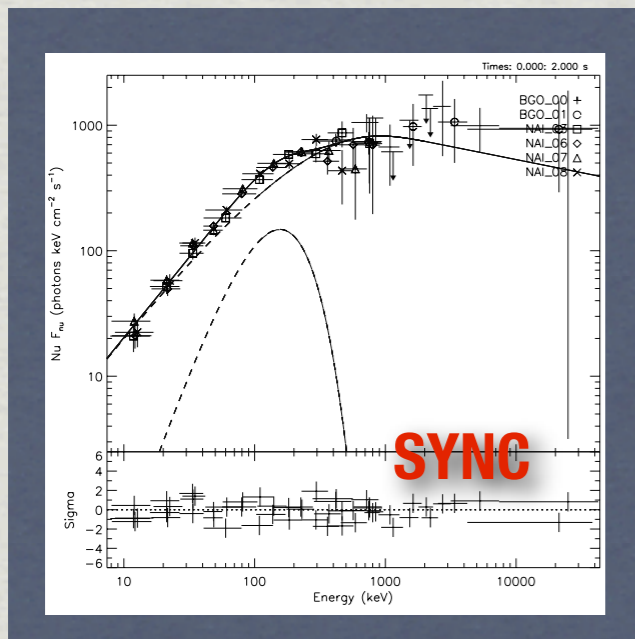
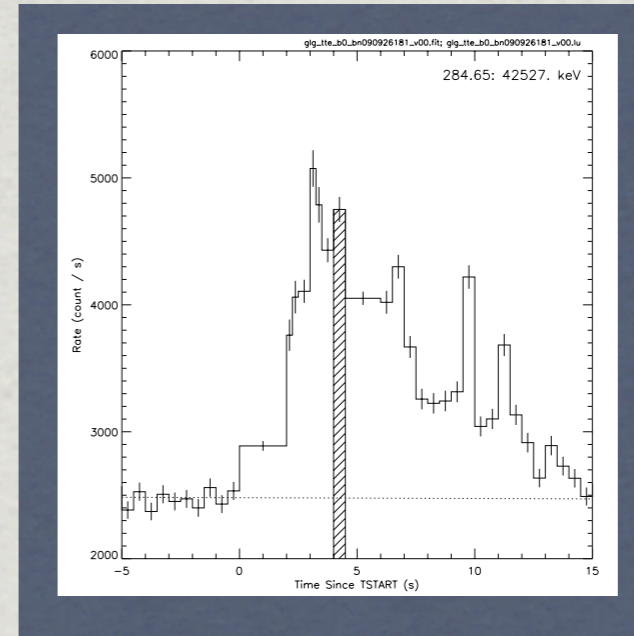
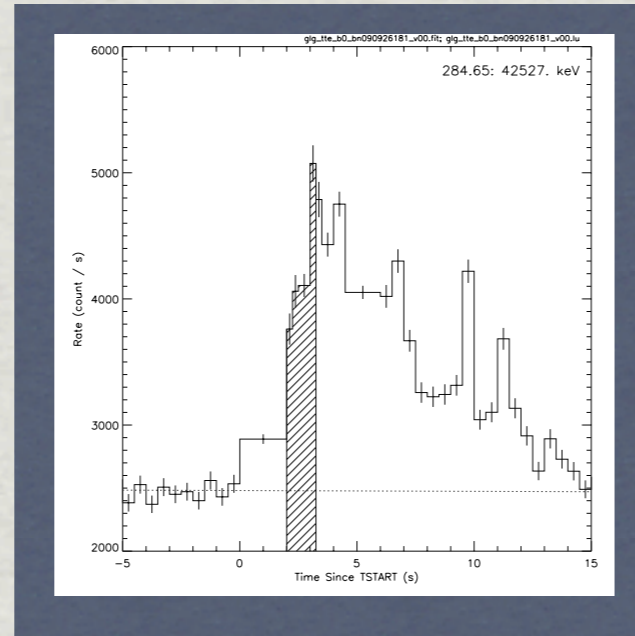
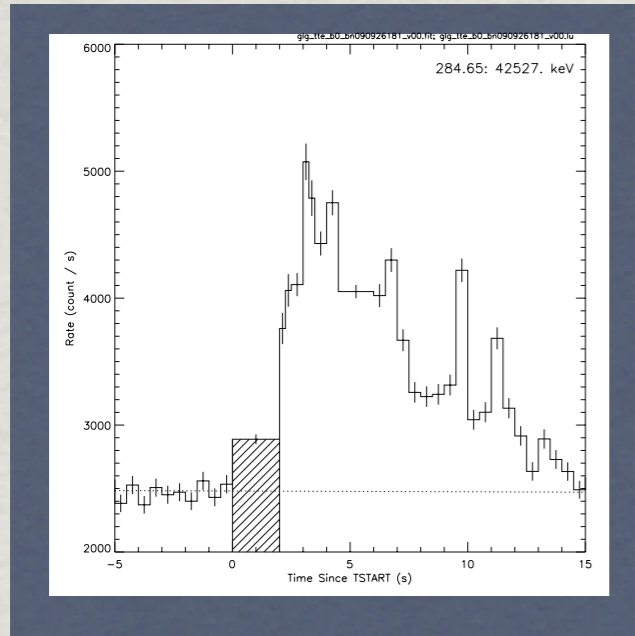


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GRB090926A



FIT VALUES: GRB 090926A

TERM: BAND'S GRB, EPEAK

AMPLITUDE	0.03141 +/-	0.00541 P/S-CM2-KEV
EPEAK	600.0 +/-	153. KEV
ALPHA	-0.8176 +/-	0.101
BETA	-2.143 +/-	0.131

TERM: BLACK BODY

AMPLITUDE	1.735E-05 +/-	6.20E-06 P/S-CM2-KEV
KT	35.55 +/-	4.31 KEV

==> CASTOR C-STAT = 783.07, DOF = 724

--
TERM: BLACK BODY

AMPLITUDE	1.234E-05 +/-	4.41E-06 P/S-CM2-KEV
KT	39.93 +/-	3.90 KEV

TERM: TOTAL TEST SYNCHROTRON

AMPLITUDE	4.004 +/-	0.200 P/S-CM2-KEV
ENERGY CRIT	28.74 +/-	5.78 KEV
ETA	3.000 +/-	0.00
PL INDEX	3.382 +/-	0.311

==> CASTOR C-STAT = 783.19, DOF = 725

TERM: BAND'S GRB, EPEAK

AMPLITUDE	0.1809 +/-	0.00683 P/S-CM2-KEV
EPEAK	514.5 +/-	18.6 KEV
ALPHA	-0.5280 +/-	0.0310
BETA	-3.593 +/-	0.487

TERM: BLACK BODY

AMPLITUDE	0.0001476 +/-	3.74E-05 P/S-CM2-KEV
KT	26.85 +/-	2.03 KEV

==> CASTOR C-STAT = 784.10, DOF = 724

--
TERM: BLACK BODY

AMPLITUDE	4.020E-05 +/-	6.02E-06 P/S-CM2-KEV
KT	46.58 +/-	1.89 KEV

TERM: TOTAL TEST SYNCHROTRON

AMPLITUDE	33.46 +/-	0.913 P/S-CM2-KEV
ENERGY CRIT	31.25 +/-	3.87 KEV
ETA	3.000 +/-	0.00
PL INDEX	4.554 +/-	0.356

==> CASTOR C-STAT = 900.14, DOF = 725

TERM: BAND'S GRB, EPEAK

AMPLITUDE	0.2760 +/-	0.0263 P/S-CM2-KEV
EPEAK	443.6 +/-	42.2 KEV
ALPHA	-0.6760 +/-	0.0551
BETA	-2.355 +/-	0.0737

TERM: BLACK BODY

AMPLITUDE	0.0002532 +/-	4.84E-05 P/S-CM2-KEV
KT	29.76 +/-	2.02 KEV

==> CASTOR C-STAT = 858.46, DOF = 724

--
TERM: BLACK BODY

AMPLITUDE	0.0001957 +/-	3.29E-05 P/S-CM2-KEV
KT	33.69 +/-	1.39 KEV

TERM: TOTAL TEST SYNCHROTRON

AMPLITUDE	45.86 +/-	1.07 P/S-CM2-KEV
ENERGY CRIT	21.59 +/-	2.21 KEV
ETA	3.000 +/-	0.00
PL INDEX	3.893 +/-	0.203

==> CASTOR C-STAT = 865.87, DOF = 725