The $E_{p,i} - E_{iso}$ correlation: cosmological use and reliability

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Why look for more cosmological probes?

- different distribution in redshift -> different sensibility to different cosmological parameters

\[ D_L = \frac{(1 + z)c}{H_o} | k |^{0.5} \times S \left\{ | k |^{0.5} \int_0^z \left[ k(1 + z)^2 + \Omega_M (1 + z')^3 + \Omega_\Lambda \right]^{0.5} dz' \right\} \]
Each cosmological probe is characterized by possible systematics

e.g SN Ia:

- different explosion mechanism and progenitor systems? May depend on z?
- light curve shape correction for the luminosity normalisation may depend on z
- signatures of evolution in the colours
- correction for dust extinction
- anomalous luminosity-color relation
- contaminations of the Hubble Diagram by no-standard SNe-Ia and/or bright SNe-Ibc (e.g. HNe)
If the “offset from the truth” is just 0.1 mag....

(slide by M. della Valle)
Recent results from SNLS (231 SNe Ia at $0.15 < z < 1.1$, Guy et al. 2010) compared to those of Astier et al. 2006 (44 low redshift SNe along with the 71 SNe from the SNLS first year sample)
Why investigating Gamma-Ray Bursts?

- all GRBs with measured redshift (~220, including a few short GRBs) lie at cosmological distances ($z = 0.033 – 8.2$) (except for the peculiar GRB980425, $z=0.0085$)

- isotropic luminosities and radiated energy are huge, can be detected up to very high $z$

- no dust extinction problems; $z$ distribution much beyond SN Ia but... GRBs are not standard candles (unfortunately)

Jakobsson et al., 2010

Amati, 2009
jet angles, derived from break time of optical afterglow light curve by assuming standard afterglow model, are of the order of few degrees

the collimation-corrected radiated energy spans the range $\sim 5 \times 10^{49} - 5 \times 10^{52}$ erg

$\Rightarrow$ more clustered but still not standard

\[ \theta = 0.09 \left( \frac{t_{\text{jet},d}}{1+z} \right)^{3/8} \left( \frac{n \eta_\gamma}{E_{\gamma, \text{iso,52}}} \right)^{1/8} \]

\[ E_\gamma = (1 - \cos \theta) E_{\gamma, \text{iso}}. \]
The $E_{p,i} - E_{iso}$ correlation

- GRB $\nu F\nu$ spectra typically show a peak at a characteristic photon energy $E_p$
- measured spectrum + measured redshift $\rightarrow$ intrinsic peak energy and radiated energy

\[ E_{p,i} = E_p \times (1 + z) \]

\[ E_{\gamma,iso} = \frac{4\pi D_i^2}{(1 + z)} \int_{1/(1+z)}^{10^4/(1+z)} E N(E) \, dE \text{ \text{erg}} \]

Amati (2009)
Amati et al. (A&A 2002): significant correlation between $E_{p,i}$ and $E_{iso}$ found based on a small sample of BeppoSAX GRBs with known redshift.
Ep,i – Eiso correlation for long GRBs with known redshift confirmed and extended by measurements of ALL other GRB detectors with spectral capabilities

120 long GRBs as of Oct. 2010

BeppoSAX GRBs
Ep\textsubscript{i} of Swift GRBs measured by Konus-WIND, Suzaku/WAM, Fermi/GBM and BAT (only when Ep inside or close to 15-150 keV and values provided by the Swift/BAT team (GCNs or Sakamoto et al. 2008).

Red points = Swift GRBs

Slope \sim 0.5

\sigma (\log Ep\textsubscript{i}) \sim 0.2

Gaussian distribution of data scatter
definite evidence that short GRBs DO NOT follow the $E_{p,i} - E_{iso}$ correlation: a tool to distinguish between short and long events and to get clues on their different nature (e.g., Amati 2006, Piranomonte et al. 2008, Ghirlanda et al. 2009)
3-parameters spectrum-energy correlations: prompting investigation of GRBs as cosmological probes

claims (2004): the $E_{p,i}-E_{iso}$ correlation becomes tighter when adding a third observable: the jet opening angle derived from the afterglow break time $t_b$, $(\theta_{jet} \rightarrow E_{\gamma} = [1-\cos(\theta_{jet})]E_{iso})$, (Ghirlanda et al. 2004) or directly $t_b$ (Liang & Zhang 2004)
Method (e.g., Ghirlanda et al, Firmani et al., Dai et al., Zhang et al.):

\[ E_{p,i} = E_{p,\text{obs}} (1 + z) , \quad t_{b,i} = t_b / (1 + z) \]

\[ E_{\gamma,iso} = \frac{4\pi D_i^2}{(1 + z)} \int_{1/1+z}^{10^4/1+z} E N(E) dE \text{ erg} \]

\[ D_i = D_i(z, H_0, \Omega_M, \Omega_{\Lambda}, \ldots) \]

fit the correlation and construct an Hubble diagram for each set of cosmological parameters -> derive c.l. contours based on chi-square
“Crisis” of 3-parameters spectrum-energy correlations

- lack of jet breaks in several Swift X-ray afterglow light curves, in some cases, evidence of achromatic break
- challenging evidences for Jet interpretation of break in afterglow light curves or due to present inadequate sampling of optical light curves w/r to X-ray ones and to lack of satisfactory modeling of jets?
➢ debate on Swift outliers to the Ep-Eγ correlation (including both GRB with no break and a few GRB with achromatic break)

➢ different conclusions based on light curve modeling and considering early or late break

Campana et al. 2007

Ghirlanda et al. 2007
the $E_p-E_\gamma$ slope and dispersion depends on the assumptions on the circum-burst environment density profile (ISM or wind)

Nava et al., A&A, 2005: ISM (left) and WIND (right)
Recent Fermi observations confirm the $E_{p,i}$ – $E_{iso}$ correlation and that the dispersion of the $E_p$ – $E_\gamma$ correlation is likely significantly larger than claimed in 2004-2005.

Amati 2010

McBreen et al. 2010
Growing number of outliers to the Ep-Eiso-tb correlation

Amati, Frontera, Guidorzi 2009

GRB 080916C

Urata et al. 2009

GRB071010B
claims (2006): the $E_{p,i}$-$E_{iso}$ correlation becomes tighter when adding a third observable: the “high signal time” $T_{0.45}$ (Firmani et al. 2006)

... but Rossi et al. (2008) and Schaefer et al. (2008), based on BeppoSAX and Swift GRBs, showed that the dispersion of the $L_p$-$E_p$-$T_{0.45}$ correlation is significantly higher than thought before and that the $E_{p,i}$-$L_p$-$iso$-$T_{0.45}$ correlation my be equivalent to the $E_{p,i}$-$E_{iso}$ correlation
Using the simple $E_{p,i}-E_{iso}$ correlation for cosmology

- Ep,i – Eiso vs. other spectrum-energy correlations

Diagram:

- Ep,i – Liso
  - Ep,i – Eiso
  - "Amati" 02
    - Eiso<->Liso
    - $E_{iso}<->L_{iso}$
    - $E_{iso}<->L_{p,iso}$
  - Ep,i – Eiso-tb
  - "Liang-Zhang" 05

- Ep,i – Lp,iso
  - Ep,i – Lp,iso-T0.45
  - "Firmani" 06

- Ep,i – Eγ
  - "Ghirlanda" 04
  - $tb, opt + jet model$

- Ep,i – Eiso
  - $tb, opt$

- Ep,i – Lp,iso
  - $T0.45$
Eiso is the GRB brightness indicator with less systematic uncertainties

Liso is affected by the often uncertain GRB duration (e.g., long tails of Swift GRBs);

Lp,iso is affected by the lack of or poor knowledge of spectral shape of the peak emission (the time average spectrum is often used) and by the subjective choice and inhomogeneity in z of the peak time scale

addition of a third observable introduces further uncertainties (difficulties in measuring t_break, chromatic breaks, model assumptions, subjective choice of the energy band in which compute T_{0.45}, inhomogeneity on z of T_{0.45}) and substantially reduces the number of GRB that can be used (e.g., #E_{p,i} - E_{\gamma} \sim \frac{1}{4} #E_{p,i} - E_{iso})

recent evidences that dispersion of E_{p,i}-L_{p,iso}-T_{0.45} correlation is comparable to that of E_{p,i} - E_{iso} and evidences of outliers / higher dispersion of the E_p-E_{\gamma} and E_p-E_{iso}-t_b correlations
Amati et al. (2008): let’s make a step backward and focus on the Ep,i – Eiso correlation.
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does the extrinsic scatter of the $E_{p,i}$-$E_{iso}$ correlation vary with the cosmological parameters used to compute $E_{iso}$?

$$E_{\gamma, iso} = \frac{4\pi D_l^2}{(1+z)} \int_{1/1+z}^{10^{4}/1+z} E N(E) dE \ \text{erg}$$

$$D_l = D_l(z, H_0, \Omega_M, \Omega_\Lambda, ...)$$

Amati et al. 2008
a fraction of the extrinsic scatter of the $E_{p,i}$-$E_{iso}$ correlation is indeed due to the cosmological parameters used to compute $E_{iso}$

Evidence, independent on SN Ia or other cosmological probes, that, if we are in a flat $\Lambda$CDM universe, $\Omega_M$ is lower than 1

Amati et al. 2008
By using a maximum likelihood method the extrinsic scatter can be parametrized and quantified (e.g., D’Agostini 2005)

\[ L(m, c, \sigma_v; x, y) = \frac{1}{2} \sum \log (\sigma_v^2 + \sigma_{y_i}^2 + m^2 \sigma_{x_i}^2) + \frac{1}{2} \sum \frac{(y_i - m x_i - c)^2}{\sigma_v^2 + \sigma_{y_i}^2 + m^2 \sigma_{x_i}^2} \]

\( \Omega_M \) can be constrained to 0.04-0.43 (68%) and 0.02-0.71 (90%) for a flat \( \Lambda CDM \) universe (\( \Omega_M = 1 \) excluded at 99.9% c.l.)

significant constraints on both \( \Omega_M \) and \( \Omega_\Lambda \) expected from sample enrichment

Amati et al. 2008
analysis of the most updated sample of 120 GRBs shows significant improvements w/r to the sample of 70 GRBs of Amati et al. (2008)

this evidence supports the reliability and perspectives of the use of the Ep,i – Eiso correlation for the estimate of cosmological parameters

<table>
<thead>
<tr>
<th>Ωm (flat universe)</th>
<th>68%</th>
<th>90%</th>
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</thead>
<tbody>
<tr>
<td>70 GRBs (Amati 08)</td>
<td>0.04 – 0.43</td>
<td>0.02 – 0.71</td>
</tr>
<tr>
<td>120 GRBs (Amati 10)</td>
<td>0.06 – 0.34</td>
<td>0.03 – 0.54</td>
</tr>
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</table>
Calibrating the $E_{p,i} - E_{iso}$ correlation with SN Ia

- several authors (e.g., Kodama et al., 2008; Liang et al., 2008, Li et al. 2008, Tsutsui et al. 2009, Capozziello & Izzo 2010) calibrated the correlation at $z < 1.7$ by using the luminosity distance – redshift relation derived from SN Ia.

- The aim is to extend the SN Ia Hubble diagram up to redshift where the luminosity distance is more sensitive to dark energy properties and evolution.

- but with this method GRB are no more an independent cosmological probe.

![Graphs showing the relationship between redshift and luminosity distance, with annotations for different cosmological models and data sets.](image-url)
But… is the $E_p,i$ – $E_{iso}$ correlation “real”? 

- different GRB detectors are characterized by different detection and spectroscopy sensitivity as a function of GRB intensity and spectrum
- this may introduce relevant selection effects / biases in the observed $E_p,i$ – $E_{iso}$ and other correlations

Band 2008

Ghirlanda et al. 2008
Selection effects in the process leading to the redshift estimate are also likely to play a relevant role (e.g., Coward 2008).

Swift: reduction of selection effects in redshift → Swift GRBs expected to provide a robust test of the $E_{p,i} - E_{iso}$ correlation.
claims that a high fraction of BATSE events (without z) are inconsistent with the correlation (e.g. Nakar & Piran 2004, Band & Preece 2005, Kaneko et al. 2006, Goldstein et al. 2010)

but… is it plausible that we are measuring the redshift only for the very small fraction (10-15%) of GRBs that follow the Ep,i – Eiso correlation? This would imply unreliably huge selection effects in the sample of GRBs with known redshift

in addition: Ghirlanda et al. (2005), Bosnjak et al. (2005), Nava et al. (2008), Ghirlanda et al. (2009) showed that most BATSE GRBs with unknown redshift are potentially consistent with the correlation

Substantially different conclusions, but… data are data, it cannot be a matter of opinions!

tests have to take into account correctly the extrinsic scatter of the Ep,i – Eiso correlation
- method: unknown redshift -> convert the $E_{p,i} - E_{iso}$ correlation into an $E_{p,obs} -$ Fluence correlation

$$E_{\text{peak}}^{\text{obs}}(1 + z) = k \left( \frac{4\pi d_L^2 F}{1 + z} \right)^{\alpha} \rightarrow E_{\text{peak}}^{\text{obs}} = k F^{\alpha} f(z); \quad f(z) = \frac{(4\pi d_L^2)^{\alpha}}{(1 + z)^{1+\alpha}}$$

- the fit of the updated $E_{p,i} - E_{iso}$ GRB sample with the maximum-likelihood method accounting for extrinsic variance provides $a = 0.53$, $k = 102$, $\sigma = 0.19$

- for these values $f(z)$ maximizes for $z$ between 3 and 5
a simple exercise: consider BATSE fluences and spectra from Kaneko et al. 2006 (350 bright GRBs)

Ep,i-Eiso correlation re-fitted by computing Eiso from $25^*(1+z)$ to $2000^*(1+z)$ gives $K \sim 120$, $m \sim 0.53$, $\sigma(\log Ep,i) \sim 0.2$, $K_{\text{max,2}\sigma} \sim 250$

only a very small fraction of GRBs (and with large uncertainties on Ep) are below the $2\sigma$ limit !
Amati, Dichiara et al. (2010, in progress): consider fluences and spectra from the Goldstein et al. (2010) BATSE complete spectral catalog (on line data)

- considered long (777) and short (89) GRBs with fit with the Band-law and uncertainties on $E_p$ and fluence $< 40\%$

- most long GRBs are potentially consistent with the $E_{p,i} - E_{iso}$ correlation, most short GRBs are not
ALL long GRBs with 20% uncertainty on $E_p$ and fluence (525) are potentially consistent with the correlation.
ALL long GRBs with 20% uncertainty on Ep and fluence (525) are potentially consistent with the correlation.
in addition to the large uncertainties on \( E_p \) and fluences, biases in the estimates of \( E_p \) and fluence of weak hard events have also to be taken into account:

a) fits with cut-off power-law (COMP) tend to overestimate \( E_p \) because of the too steep slope above \( E_p \)

BATSE, sample of Goldstein et al. 2010  
BeppoSAX/GRBM (Guidorzi et al. 2010)
measure only the harder portion of the event: overestimate of $E_p$ and underestimate of the fluence
Butler et al. based on analysis Swift/BAT spectra with a Bayesian method assuming BATSE Ep distribution: 50% of Swift GRB are inconsistent with the pre-Swift Ep,i - Eiso correlation

BUT: comparison of Ep derived by them from BAT spectra using a Bayesian method and those MEASURED by Konus/Wind show that BAT cannot measure Ep > 200 keV (as expected, given its 15-150 keV passband)

MOREOVER: Ep values by Butler et al. NOT confirmed by official analysis by BAT team (Sakamoto et al. 2008) and joint analysis of BAT + KW (Sakamoto et al. 2009) of BAT + Suzaku/WAM (Krimm et al. 2009) spectra.
Ep,i of Swift GRBs measured by Konus-WIND, Suzaku/WAM, Fermi/GBM and BAT (only when Ep inside or close to 15-150 keV and values provided by the Swift/BAT team (GCNs or Sakamoto et al. 2008)): Swift GRBs are consistent with the Ep,i – Eiso correlation

- Red points = Swift GRBs
- Slope ~ 0.5
- $\sigma(\log Ep,i)$ ~ 0.2

Gaussian distribution of data scatter
Amati, Frontera & Guidorzi (2009): the normalization of the correlation varies only marginally using measures by individual instruments with different sensitivities and energy bands: -> no relevant selection effects
the $E_{p,i}$– $L_{iso}$ correlation holds also within a good fraction of GRBs (Liang et al. 2004, Firmani et al. 2008, Frontera et al. 2009, Ghirlanda et al. 2009): robust evidence for a physical origin and clues to explanation.
Conclusions and perspectives

- Given their huge radiated energies and redshift distribution extending from ~ 0.1 up to > 8, GRBs are potentially a very powerful cosmological probe, complementary to other probes (e.g., SN Ia, clusters, BAO).

- The Ep,i – Eiso correlation is one of the most robust (no firm evidence of significant selection / instrumental effects) and intriguing properties of GRBs and a promising tool for cosmological parameters.

- Analysis in the last years (>2008) provide already evidence, independent on, e.g., SN Ia, that if we live in a flat $\Lambda$CDM universe, $\Omega m$ is < 1 at >99.9% c.l. ($\chi^2$ minimizes at $\Omega m \sim 0.25$, consistent with “standard” cosmology).

- The simultaneous operation of Swift, Fermi/GBM, Konus-WIND is allowing an increase of the useful sample (z + Ep) at a rate of 15-20 GRB/year, providing an increasing accuracy in the estimate of cosmological parameters.

- Future GRB experiments (e.g., SVOM) and more investigations (statistical tools, simulations, calibration) will improve the significance and reliability of the results.
- a fraction of the extrinsic scatter of the $E_{p,i} - E_{iso}$ correlation is indeed due to the cosmological parameters used to compute $E_{iso}$

- Evidence, independent on SN Ia or other cosmological probes, that, if we are in a flat $\Lambda$CDM universe, $\Omega_M$ is lower than 1

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**Diagram:**

![Graph showing $\chi^2$ vs $\Omega_M$](image)

- Simple PL fit

*Amati et al. 2008 - 2010*
- final remark: X-ray redshift measurements are possible!

- a transient absorption edge at 3.8 keV was detected by BeppoSAX in the first 13 s of the prompt emission of GRB 990705 (Amati et al. Science, 2000)

- by interpreting this feature as a redshifted neutral iron edge a redshift of $0.86\pm0.17$ was estimated

- the redshift was later confirmed by optical spectroscopy of the host galaxy ($z = 0.842$)
END OF THE TALK