

Polarimetry of γ -Rays Converting to e^+e^- Pairs with Silicon-Pixel-Based Telescopes

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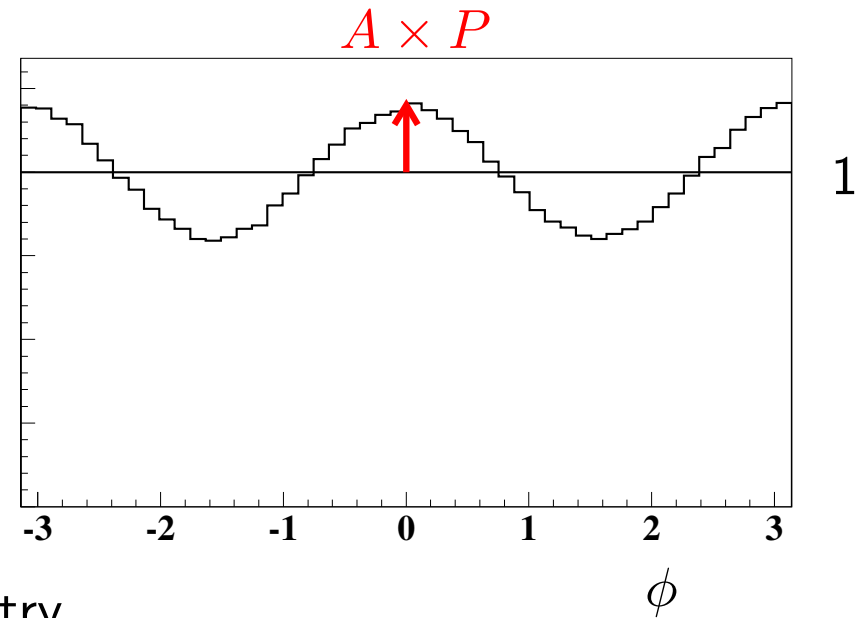
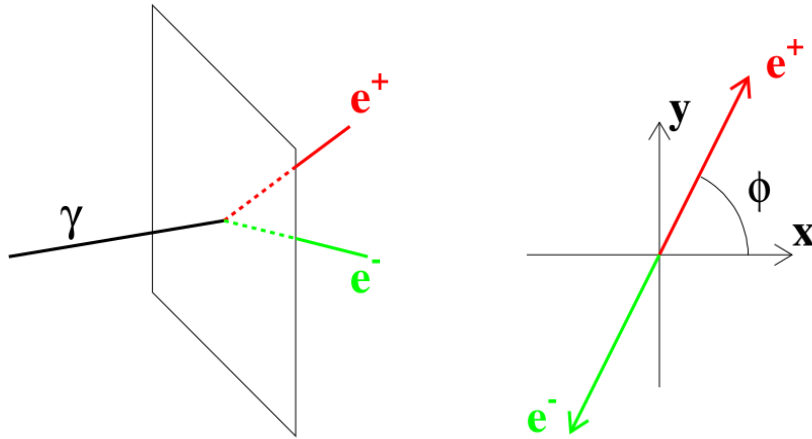


MeV γ -Ray Polarimetry: Science Goals

- Main targets: bright sources, deciphering emission mechanism
 - Blazars:
leptonic synchrotron self-Compton (SSC) or **hadronic** (proton-synchrotron)
Zhang and Böttcher, *Astrophys.J.* 774, 18 (2013)
 - Pulsars: Tagging the onset of Curvature Radiation (CR)
Harding and Kalapotharakos, *Astrophys. J.* 840 73 (2017)
- Further away (pending on statistics)
 - LIV search (Lorentz-invariance violation), induced dilution of the GRB polarization signal during propagation
F. Kislak, arXiv:1907.06514 [astro-ph.HE],
 - Axion search,
ALPs (Axion-like particles)
A. Rubbia and A. S. Sakharov, *Astropart. Phys.* **29** (2008) 20
G. Galanti, *Universe* **10** (2024) 312

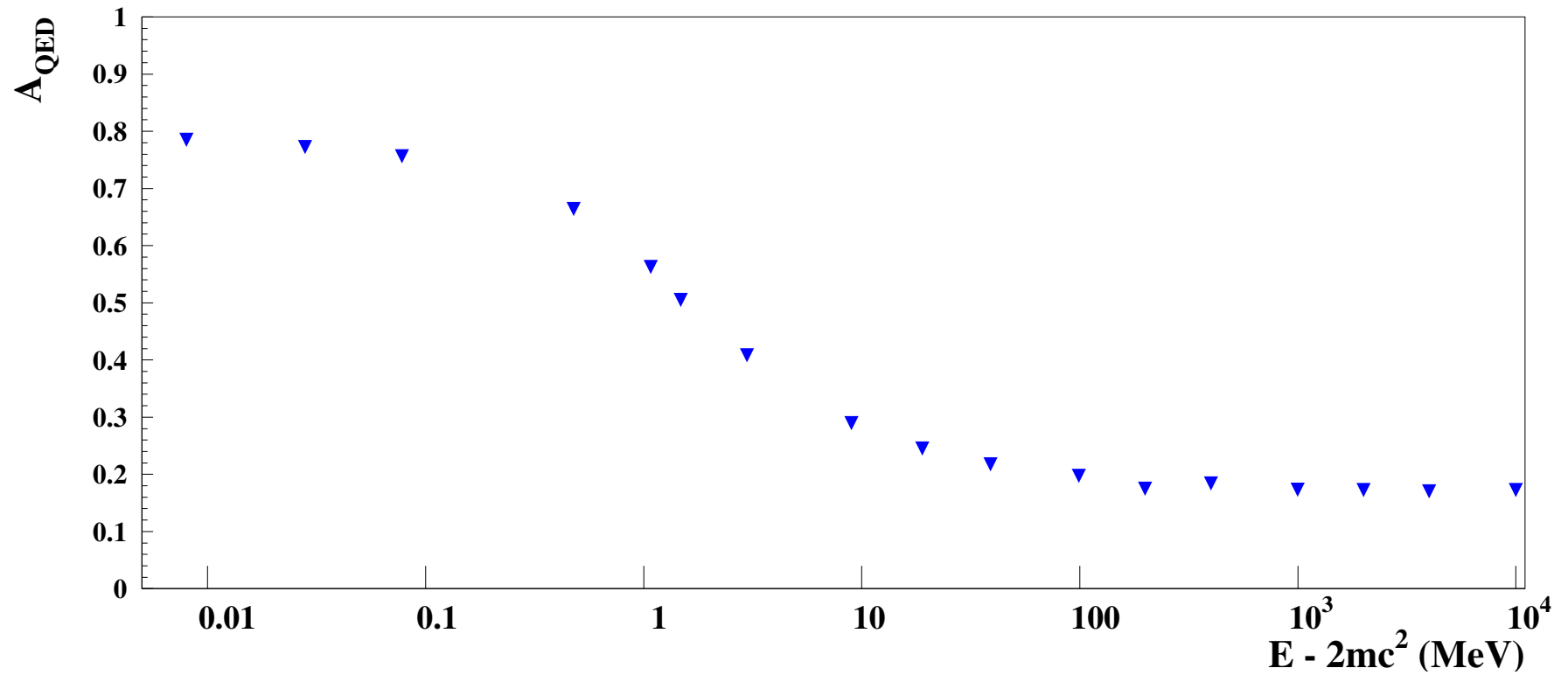
Polarimetry

$$\frac{d\Gamma}{d\phi} \propto (1 + AP \cos [2(\phi - \phi_0)]),$$



- P source linear polarisation fraction
- A γ -ray conversion polarization asymmetry
- ϕ event azimuthal angle
- ϕ_0 source polarization angle.

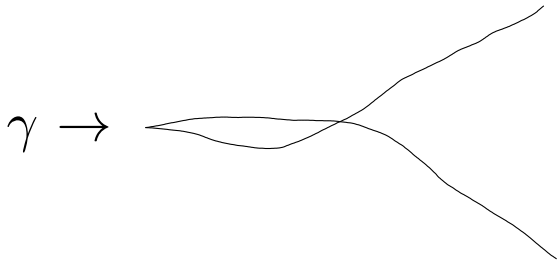
QED Polarization asymmetry



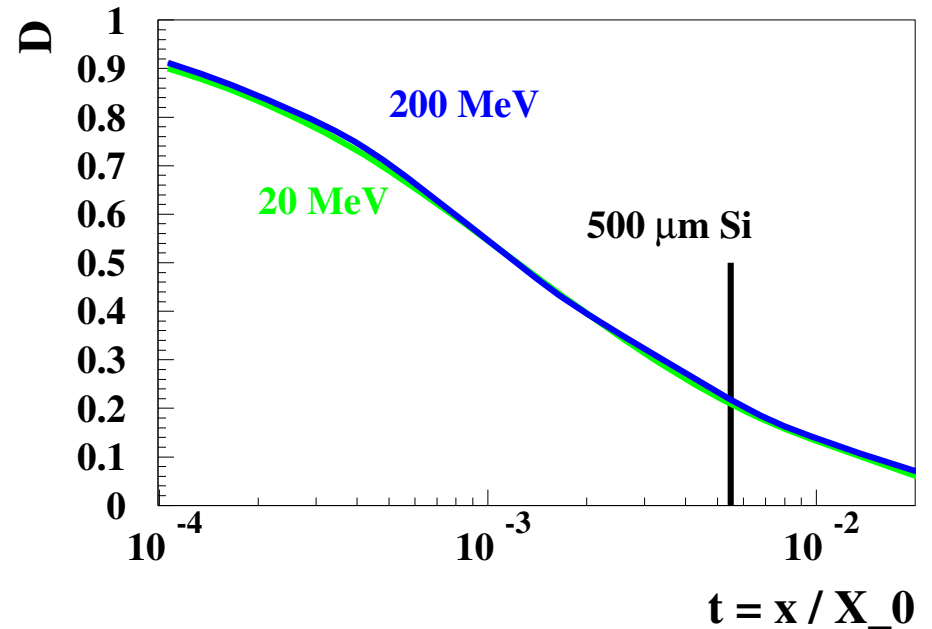
Close to 0.2 in energy range within reach

Polarimetry with pairs: e^+ and e^- Multiple Scattering

Simulated γ -ray conversion
In homogeneous medium



$$D = A/A_{\text{QED}}$$

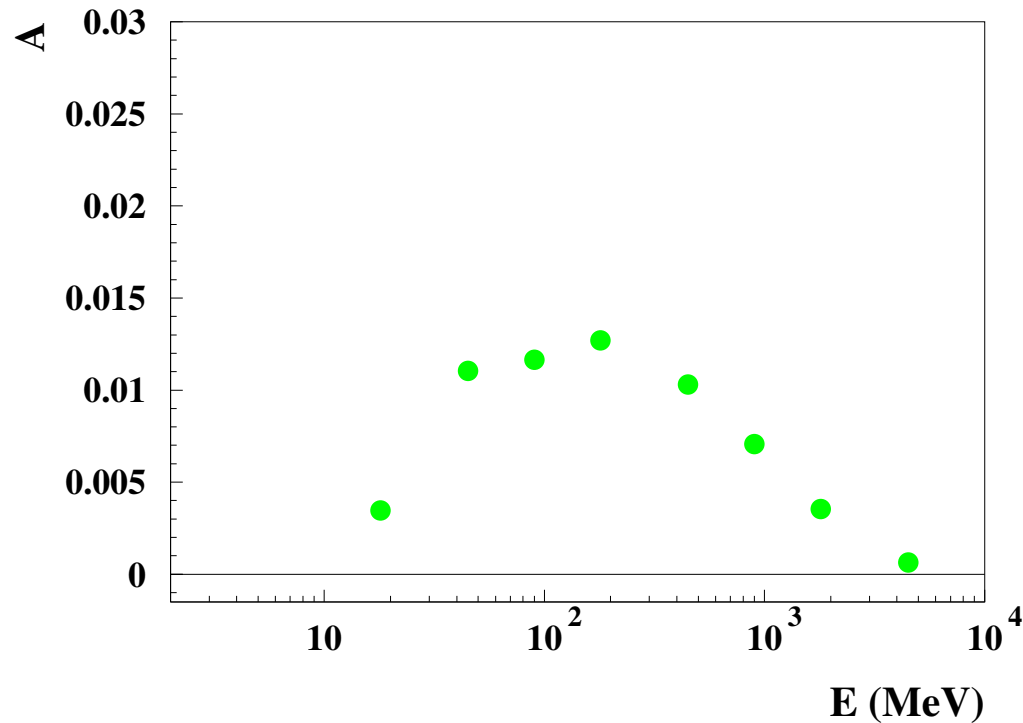


Adapted from D. Bernard, Nucl. Instrum. Meth. A 729 (2013) 765

Dilution, D , as a function of pathlength after conversion, normalized to radiation length, t

Most polarimetry information lost before leptons exited conversion wafer

Performance of Silicon Strip detectors: The Fermi-LAT



- Effective asymmetry peaks at $A \approx 0.0125$ for ≈ 200 MeV
- A dilution factor A/A_{QED} of a factor of 0.07
- Expected $\sigma_{\text{P}} \approx 0.15$ on bright source, $1.5 \times 10^{-3} \text{MeV cm}^{-2} \text{s}^{-1} / E^2$, exposure $\epsilon \approx 2 \times 10^{11} \text{cm}^2 \text{s}$

D. Bernard, Fermi Symposium 2022 and Nucl. Instrum. Meth. A **1042** (2022) 167462 (Fig. 21)

Estimate confirmed with full *Fermi*-LAT study (Vela, 15 years), A. Laviron+ PoS ICRC2023 (2023) 721 and [Talk at this Symposium](#)

Strips \rightarrow *Pixels*

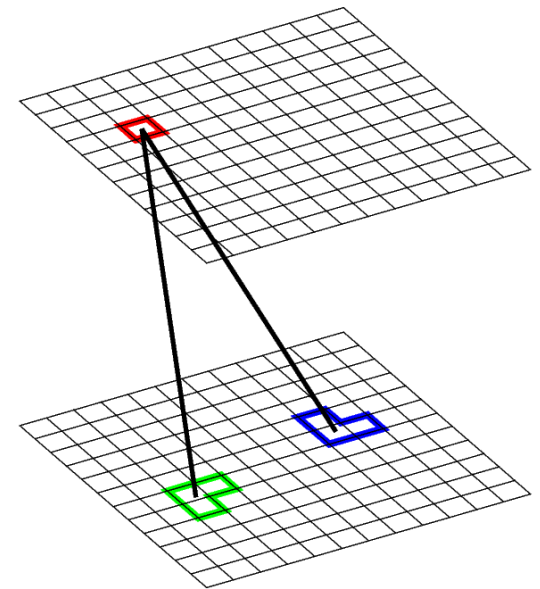
	<i>Fermi</i> -LAT	AMEGO-X
Layer	2 single-sided SSD	Pixels
Converter ?	Tungsten foils	All Si (no Tungsten foils)
e Si Thickness (μm) per layer	$2 \times 400 = 800$	500
p Pitch / size (μm)	228	500
d Layer spacing (cm)	3.3	1.0

Analysis

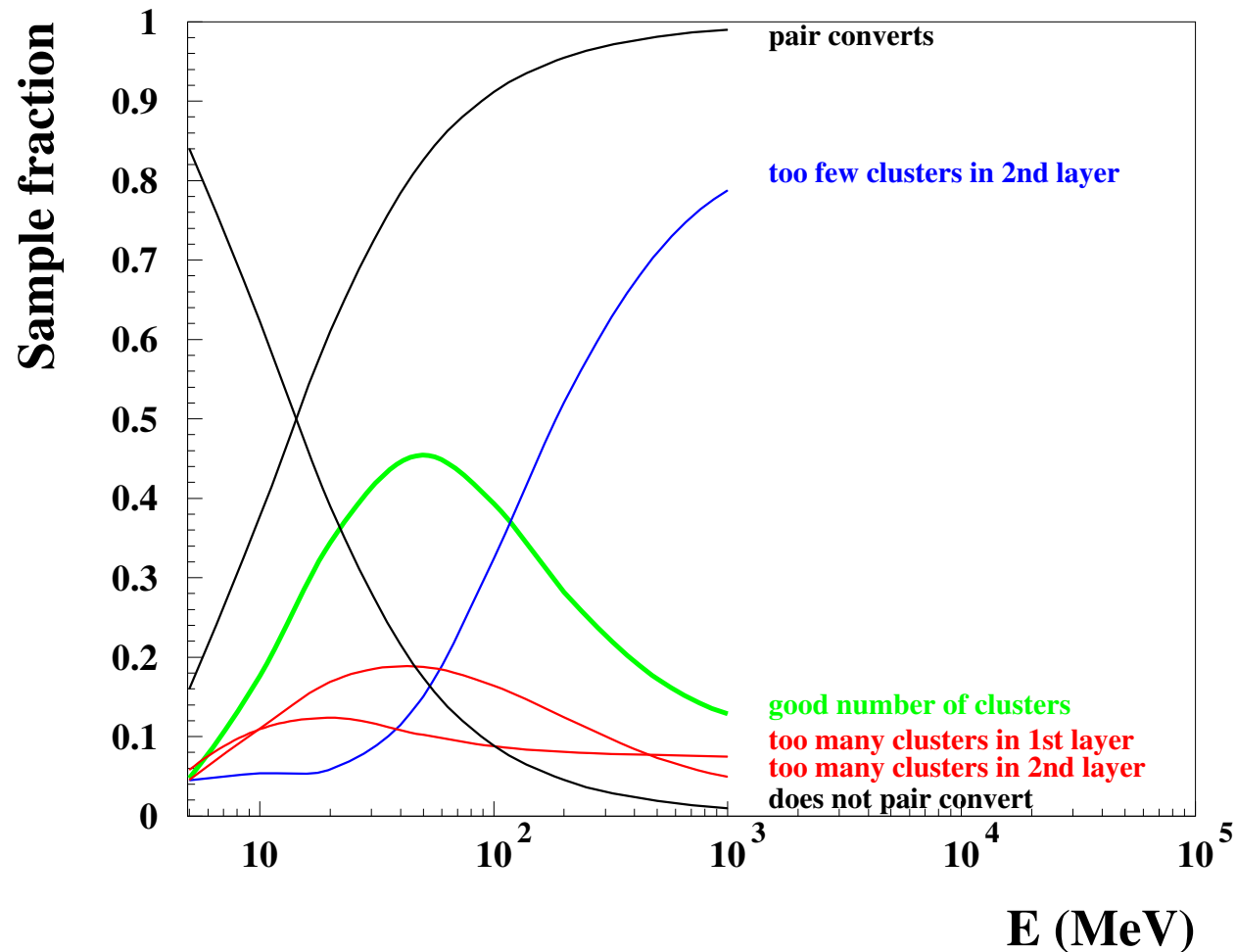
- Pair conversions selected (Compton rejected) based on MC information
- No additional trigger emulation
- **Track reconstruction based on information in conversion layer + next layer**

As in my previous [D. Bernard, Nucl. Instrum. Meth. A **1042** \(2022\) 167462](#)

- Pixels with > 0 deposited energy recorded.
- Recorded pixels with a side in common clustered
- **Exact number of clusters required**
 - 1 in conversion layer
 - 2 in next layer
- Track directions reconstructed from (geometric) cluster barycenters
- Event azimuthal angle computed from track azimuthal angles



Event Fractions

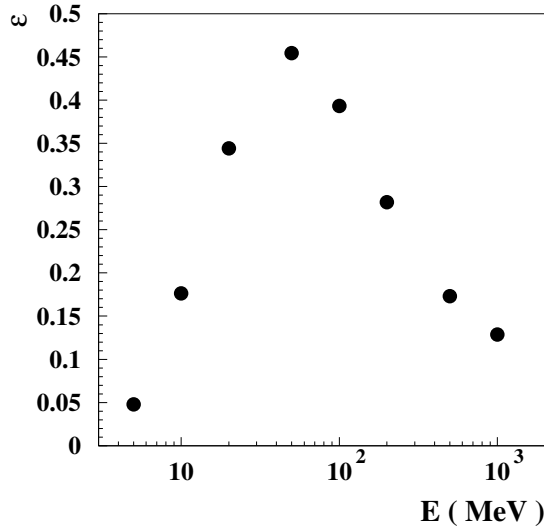


- Selection efficiency peaks at $\approx 45\%$ for $E \approx 50$ MeV
- Drops at low energies due to Compton scattering prior to conversion
- Drops at high energies due to both tracks create same cluster in next layer

Results

Selection efficiency

ϵ



Polarization asymmetry

A

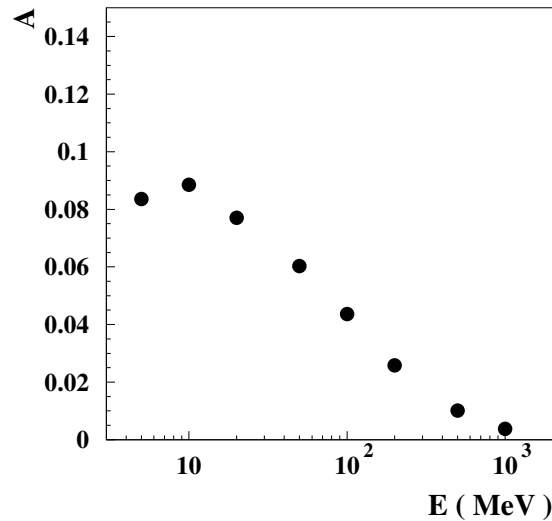
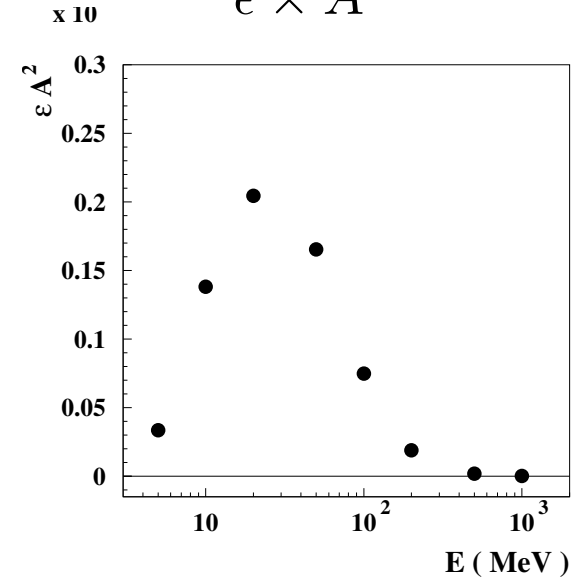


Figure of Merit

$\epsilon \times A^2$



- A plateaus at ≈ 0.09 at low energies, dilution factor $D = A/A_{\text{QED}} \approx 1/3$
- Figure of merit peaks for $E \approx 20$ MeV (sizable between 10 – 100 MeV)

Energy-Integrated Performance

Energy bins, E_k , events weighted with weight A_k , \Rightarrow

$$\sigma_P = \sqrt{\frac{2}{\sum_k A_k^2 N_k}} \quad N_k = \frac{\eta \epsilon_k F_0 \Delta E_k H(E_k) T m}{E_k^2},$$

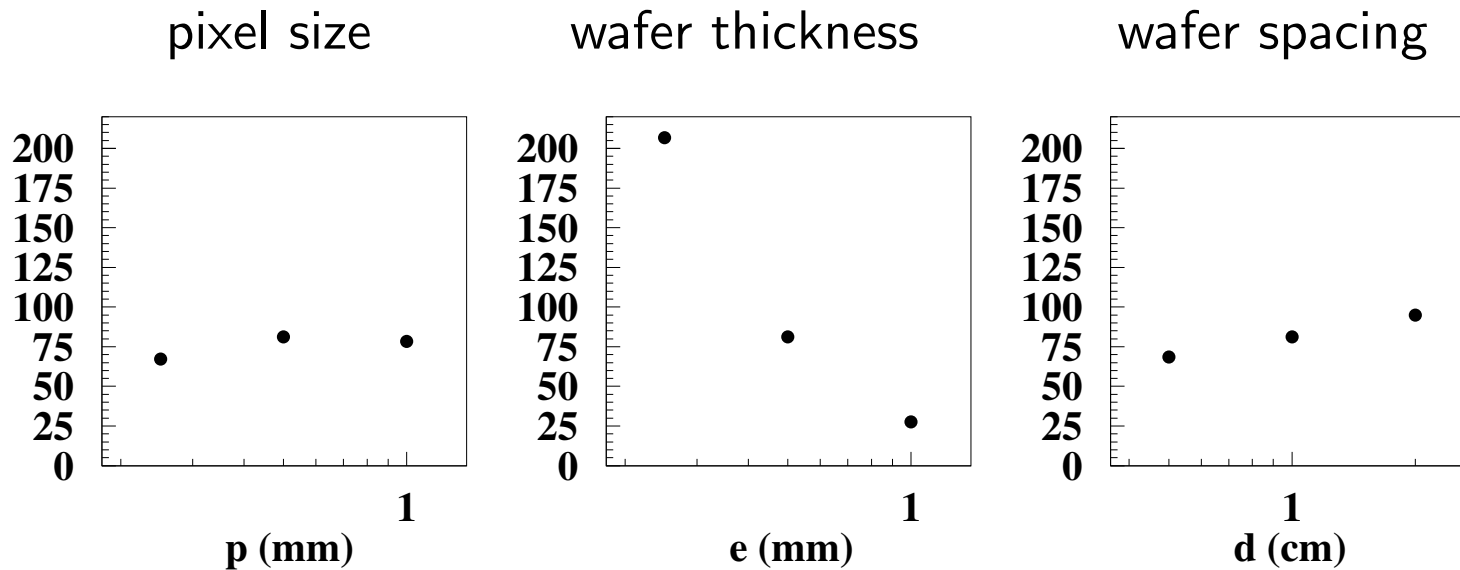
- Differential flux F_0/E^2 , $F_0 = 10^{-3} \text{ MeV}/(\text{cm}^2\text{s})$,
- m detector silicon mass (g), T duration (s)
- $H(E_k)$ total photon attenuation (cm^2/g) at photon energy E_k [NIST XCOM data base](#)
(i.e. effective area per unit mass)
- ΔE_k width of energy bin k , ϵ_k selection efficiency,
- Exposure factor $\eta = (1 - \cos(\theta_{\text{cut}}))/2 \approx 0.375$.

Energy-integrated figure of merit, $\sum_k A_k^2 N_k / (T m) = 81.(\text{year} \cdot \text{kg})^{-1}$,

For a 5 year, 30 kg AMEGO-X mission, $\sigma_P \approx 0.013$ within reach.

Energy-Integrated Performance: Variation with Detector Parameters

Energy-integrated figure of merit, $\sum_k A_k^2 N_k / (T m)$



- Driving parameter of the overall performance is clearly wafer thickness e .
(Total silicon mass kept constant)

Conclusion

- Performance of Silicon-pixel based pair polarimeter estimated with simple model
- Main performance driving parameter, wafer thickness
- Excellent prospects for the brightest sources of the MeV gamma-ray sky.

$$\sigma_P = \begin{array}{ll} 0.15 & (\text{LAT} \quad 15 \text{ years}) \\ 0.013 & (\text{AMEGO-X} \quad 5 \text{ years}) \end{array}$$

On a bright Crab-like source.

Back-up slides

Deciphering Emission Mechanism in Blazars with γ -Ray Polarimetry

- Blazars: active galactic nuclei (AGN) with one jet pointing (almost) to us

leptonic synchrotron self-Compton (SSC)

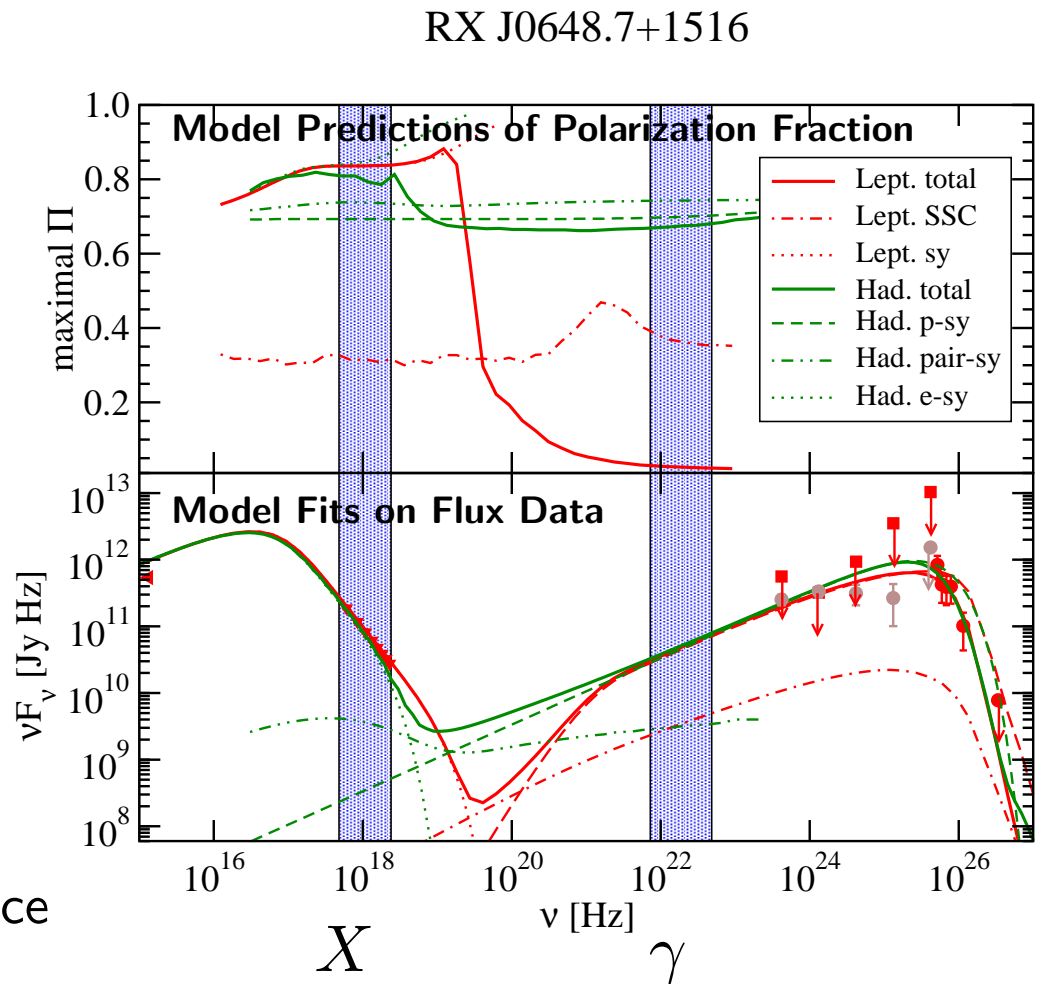
or

hadronic (proton-synchrotron) ?

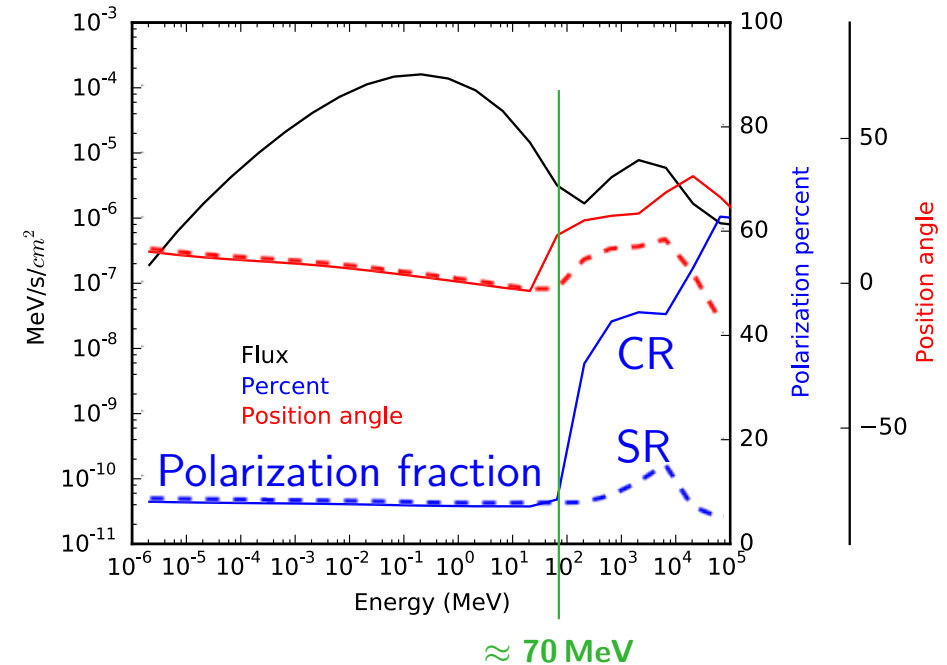
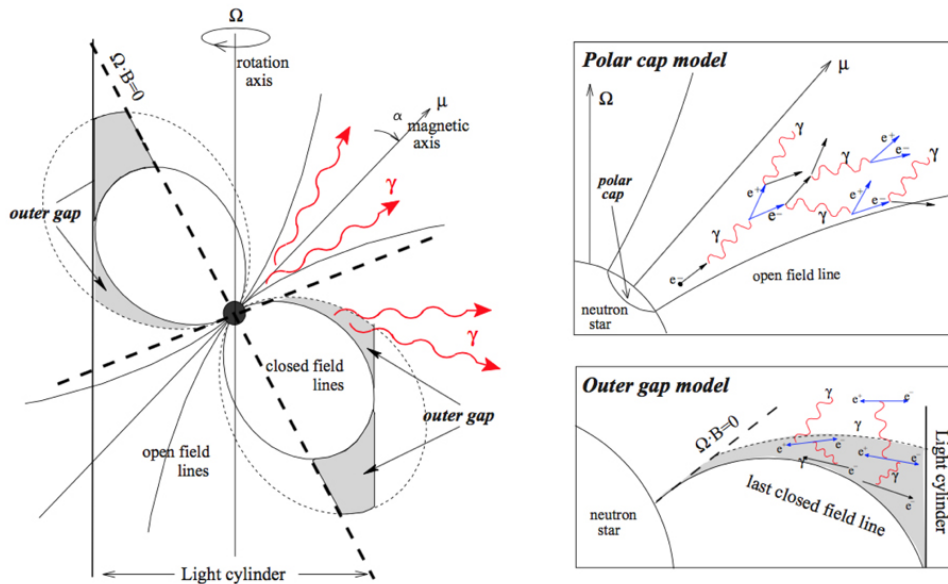
- high-frequency-peaked BL Lac
- X band: 2 -10 keV
- γ band: 30 - 200 MeV
- SED's indistinguishable, but
 - X-ray: $P_{\text{lept}} \approx P_{\text{hadr}}$
 - γ -ray: $P_{\text{lept}} \ll P_{\text{hadr}}$

Zhang and Böttcher, *Astrophys.J.* 774, 18 (2013)

“Maximal” Π : assumes no \vec{B} turbulence



Tagging the (Curvature Radiation CR – Synchrotron Radiation SR) Transition in Rotation-Powered Pulsars



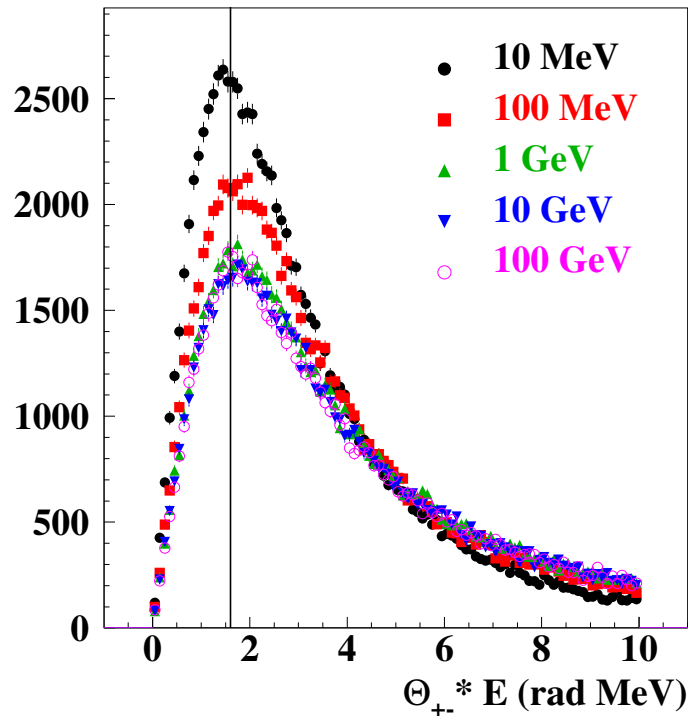
Polar-cap model of Crab-like pulsar

- MeV component is SR from pairs
- GeV component is either CR (solid line) or SR (dashed line)

Harding and Kalapotharakos, *Astrophys. J.* 840 73 (2017)

Pair Opening Angle: $1/E$ Scaling

(pair opening angle) \times (photon energy)



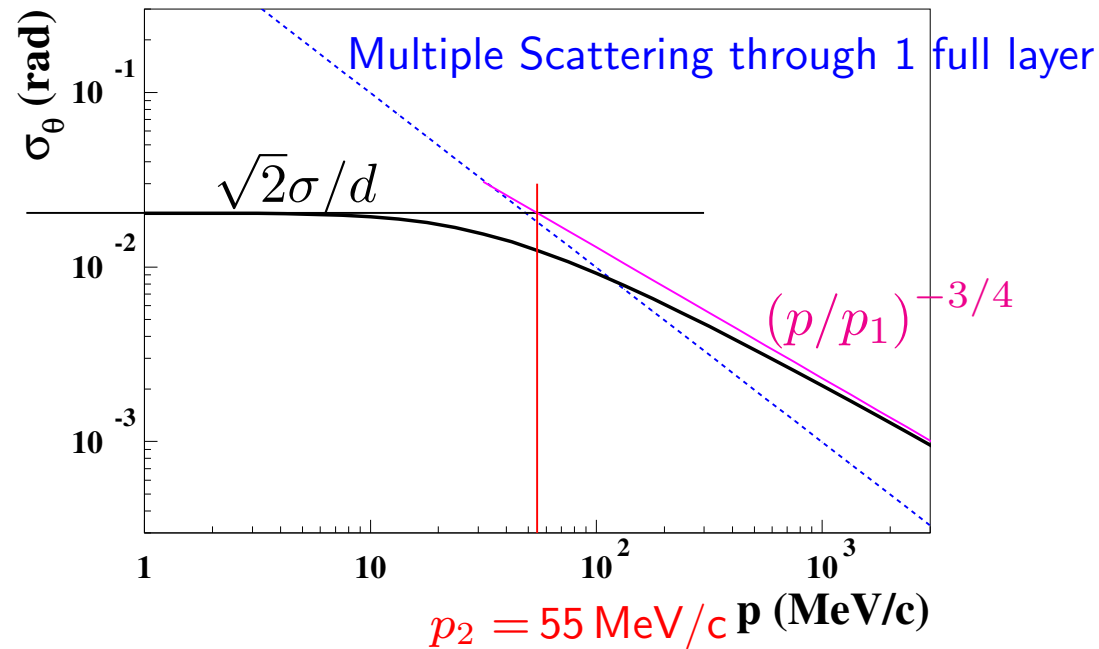
Vertical line: high-energy asymptotic most probable value

$$\frac{1.6 \text{ rad} \cdot \text{MeV}}{E}$$

H. Olsen, Phys. Rev. 131 (1963) 406

D. Bernard, Nucl. Instrum. Meth. A **899** (2018) 85

Tracking: Single-Track Polar-Angle Resolution



Curve, angular resolution of optimal (Kalman filter) tracking, eq. (1) of [arXiv:1902.07910](https://arxiv.org/abs/1902.07910)

- for conversion at the very bottom of a layer,
- an asymptotically large number of planes, and
- dE/dx energy loss neglected

A two-layer measurement is close to optimal at low track p (low photon E)

Optimal Sample Combination

$$\frac{d\Gamma}{d\phi} \propto (1 + AP \cos 2\phi), \quad \Rightarrow \quad P = \sum_i^N w_i / (A \times N) \quad \text{with weight } w_i \equiv 2 \cos 2\phi_i$$

K samples. Weight each with inverse variance, $P = \left(\sum_k \frac{P_k}{V_k} \right) / \left(\sum_k \frac{1}{V_k} \right)$, with $\frac{1}{V_k} = \frac{N_k A_k^2}{2}$
 (eg. [D. J. Shahar Open J. Stat. 2017, 7, 216.](#))

$$\text{So, } P = \sum_k \sum_i^{N_k} w'_{i,k} \quad \text{with} \quad w'_{i,k} = \frac{A_k w_{i,k}}{\sum_l N_l A_l^2}, \quad \text{precision } \sigma_P = \sqrt{\frac{2}{\sum_k N_k A_k^2}}$$

Weight each event by the average asymmetry of the sample to which it belongs.

Figure of merit of sample k , $N_k A_k^2$, of total sample, $\sum_k N_k A_k^2 = N \sum_k \epsilon_k A_k^2$.

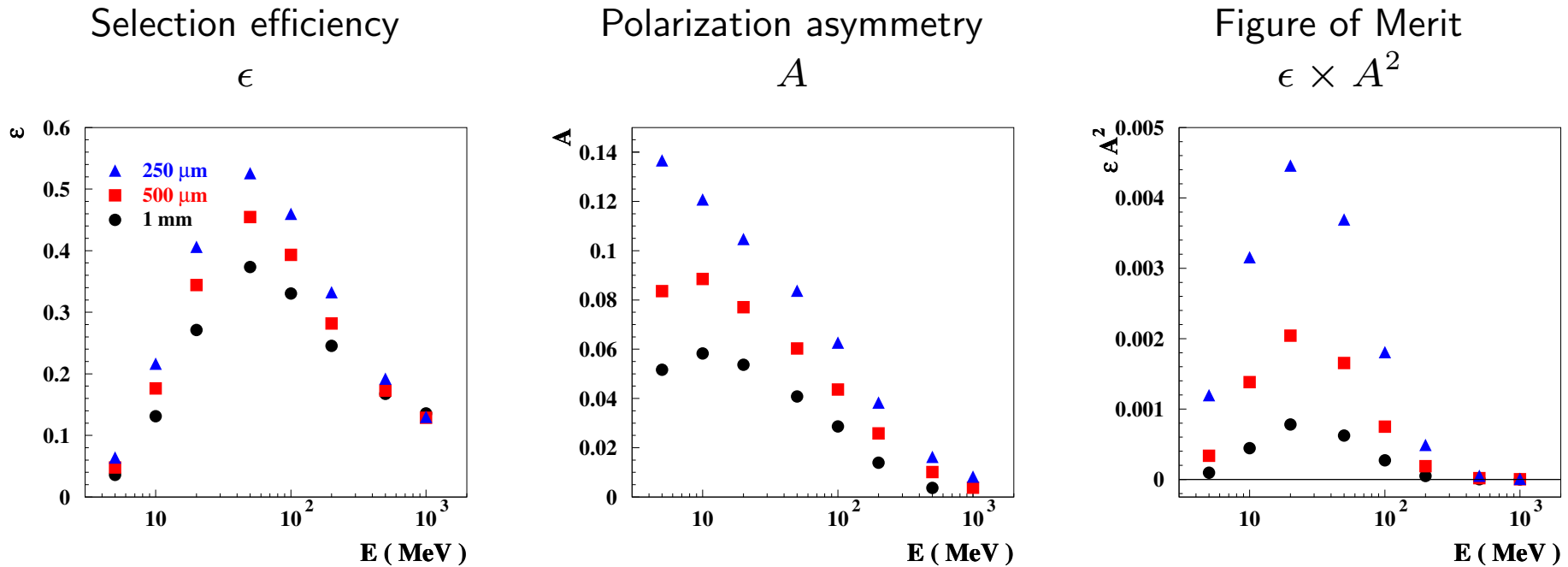
Method

ASAP: As Simple As Possible

- Target
 - “Infinite” number of “infinite” Si planes, $z < 0$
 - ⇒ All photons convert, (thin detector, effective area \propto silicon mass)
 - Dead material neglected
- Point-like source,
- Isotropic exposure map with $\cos \theta > 0.25$ cut (approx $\theta < 75^\circ$)
- Assume the telescope provides γ sample associated with known
 - γ direction (exactly, that of the source) and
 - γ energy
- Electromagnetic physics simulation EGS5, version 1.0.5, [H. Hirayama et al., SLAC-R-730, 2005](#)
- No background

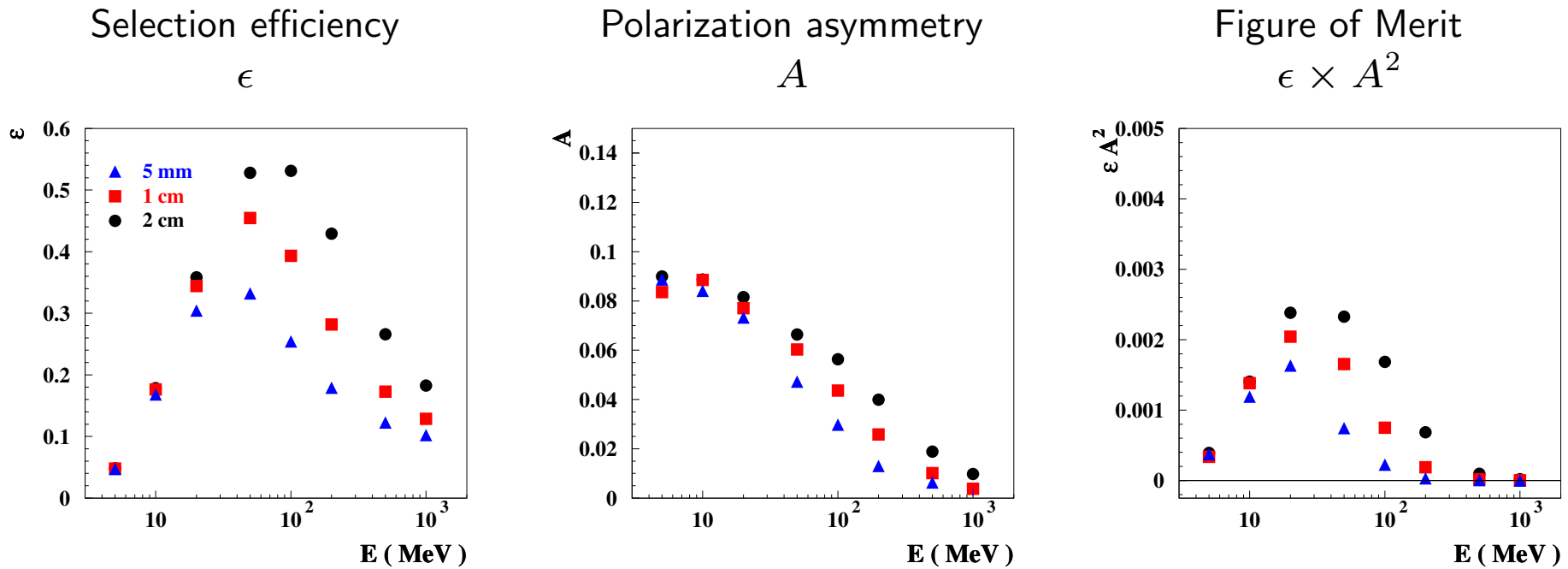
Wafer Thickness e Variation

Number of incident photons, therefore effective area, therefore Si mass, kept unchanged



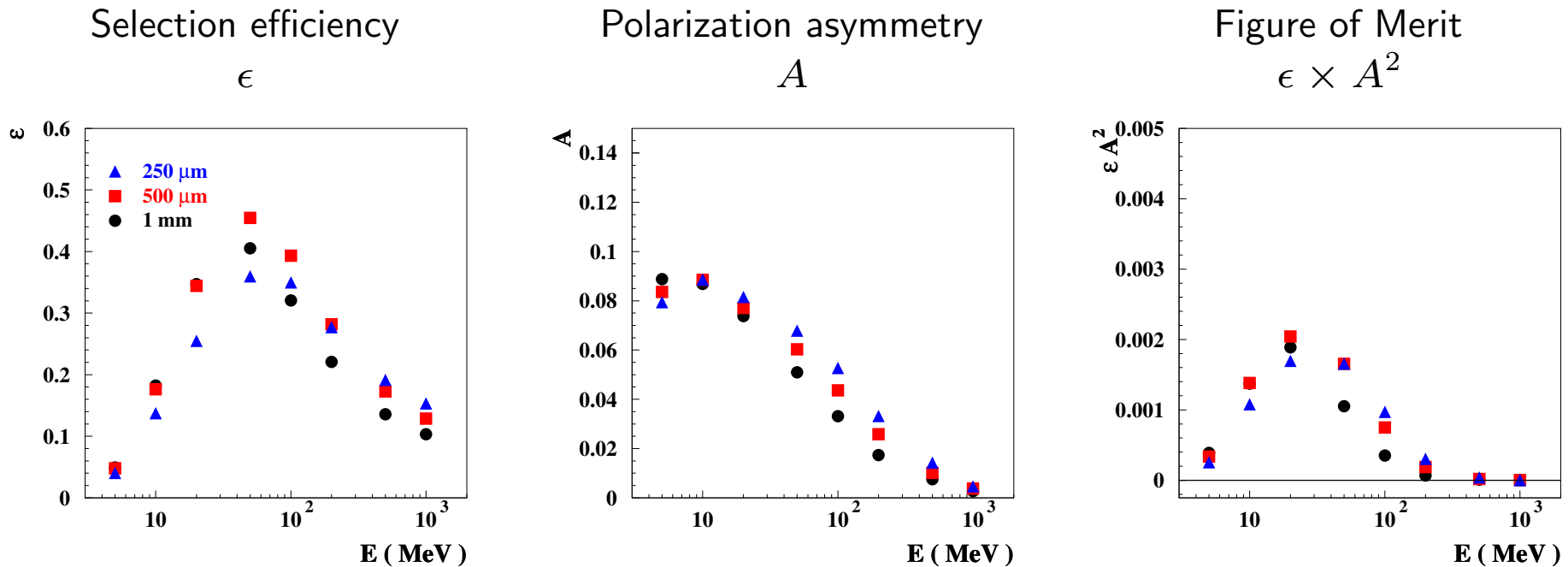
- ϵ decreases mildly with increasing e (increase of the fraction of events with too large a number of clusters in the 2nd layer)
- A decreases with increasing e due to multiple scattering

Layer Spacing d Variation



- Increasing the wafer spacing obviously improves the selection efficiency at high energies (better separation of small opening angles)
- A barely affected, except at high energy

Pixel Size p Variation



- Smaller pixels improves mildly ϵ at high energy (better separation of small opening angles)
- Smaller pixels degrades mildly ϵ at low energy (larger fraction of events with too many clusters in the 2nd wafer).
- A barely affected (the additional contribution of the pixel size to the ϕ angular resolution not the dominant factor) except at high energy