

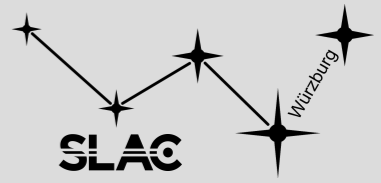
# High-energy variability of the gravitationally lensed blazar PKS 1830-211

Sarah Maria Wagner

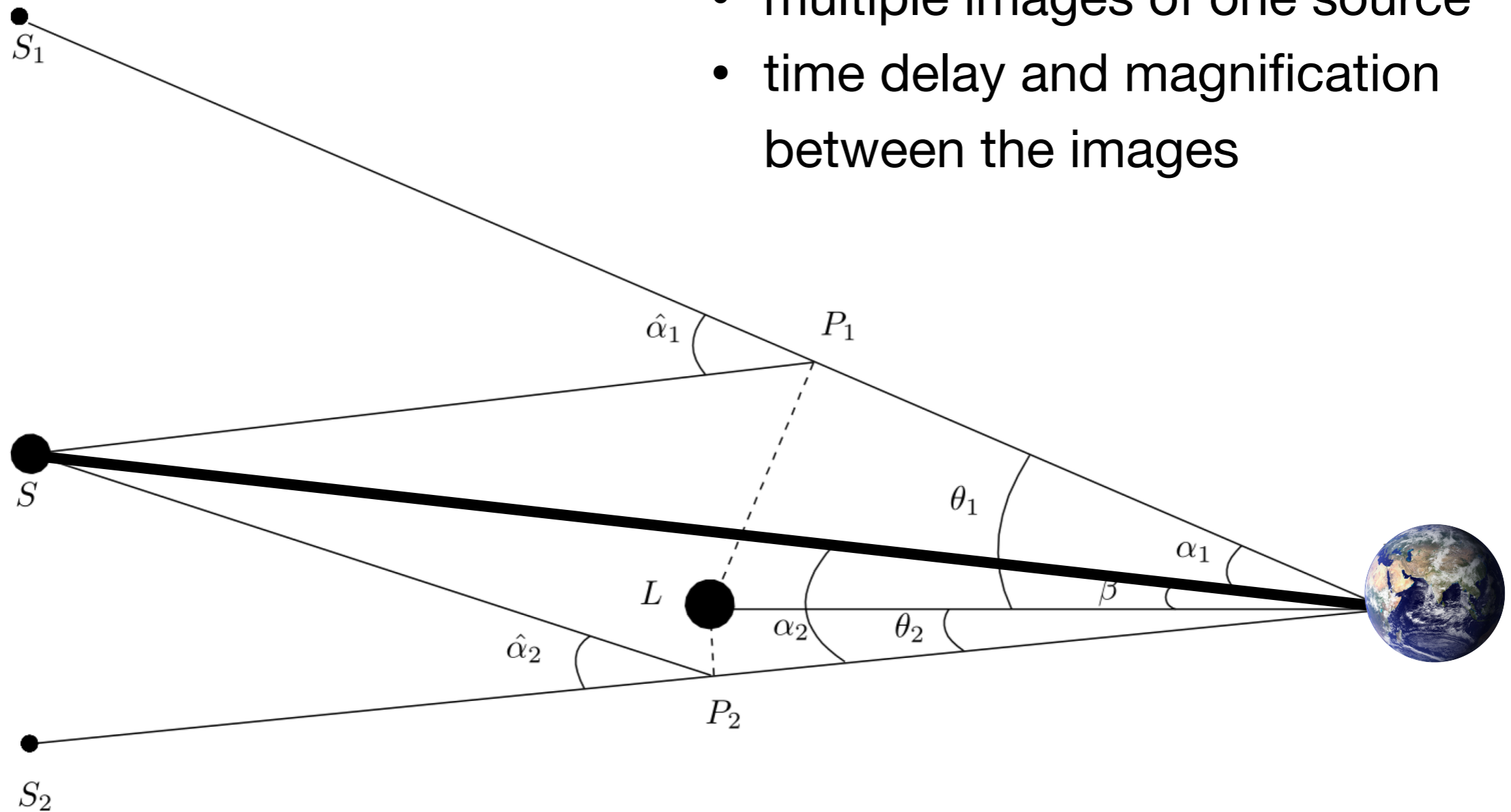
Andrea Gokus, Greg Madejski, Krzysztof Nalewajko, Jeff Scargle  
on behalf of the Fermi-LAT Collaboration



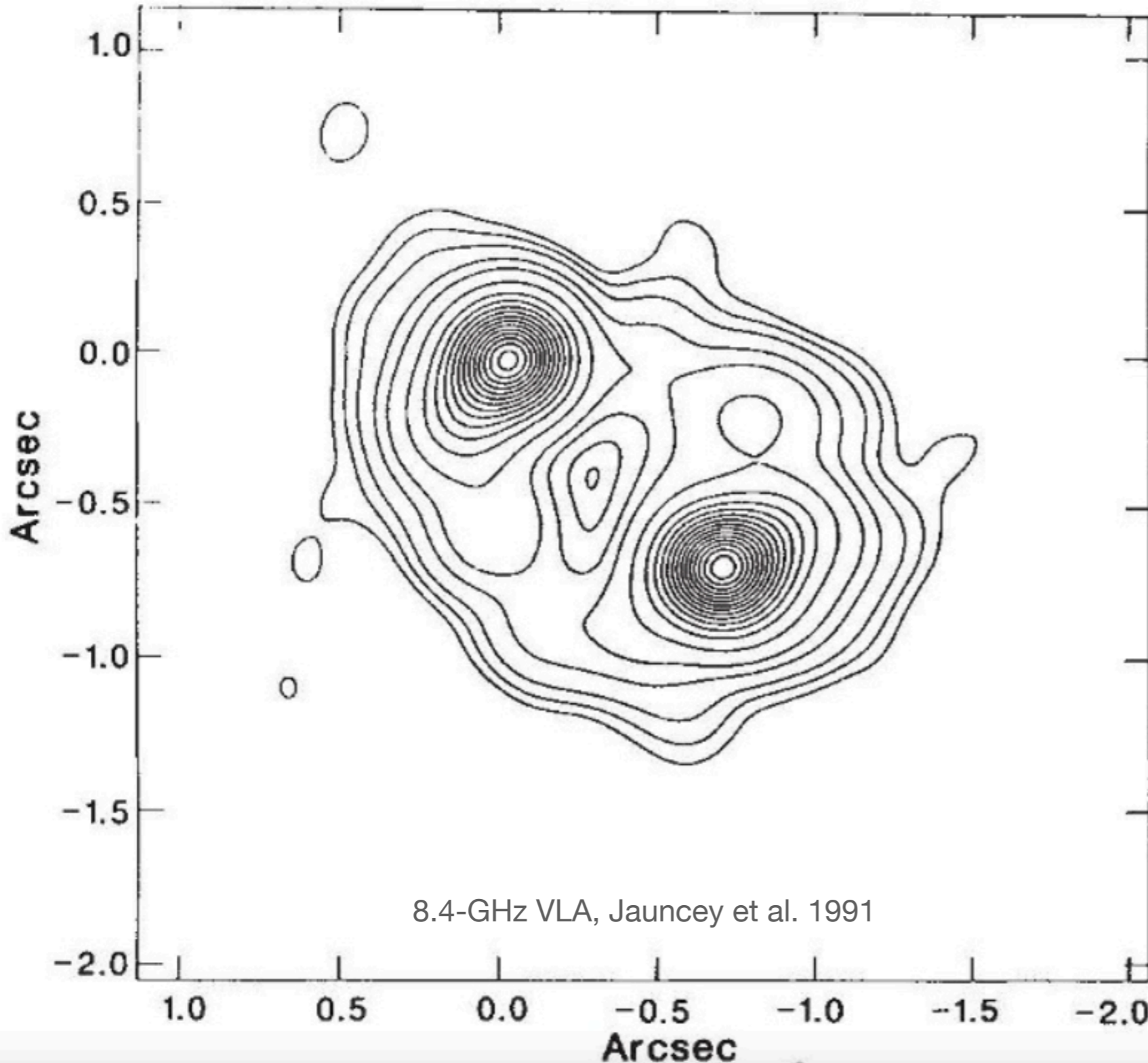
# Gravitational Lensing



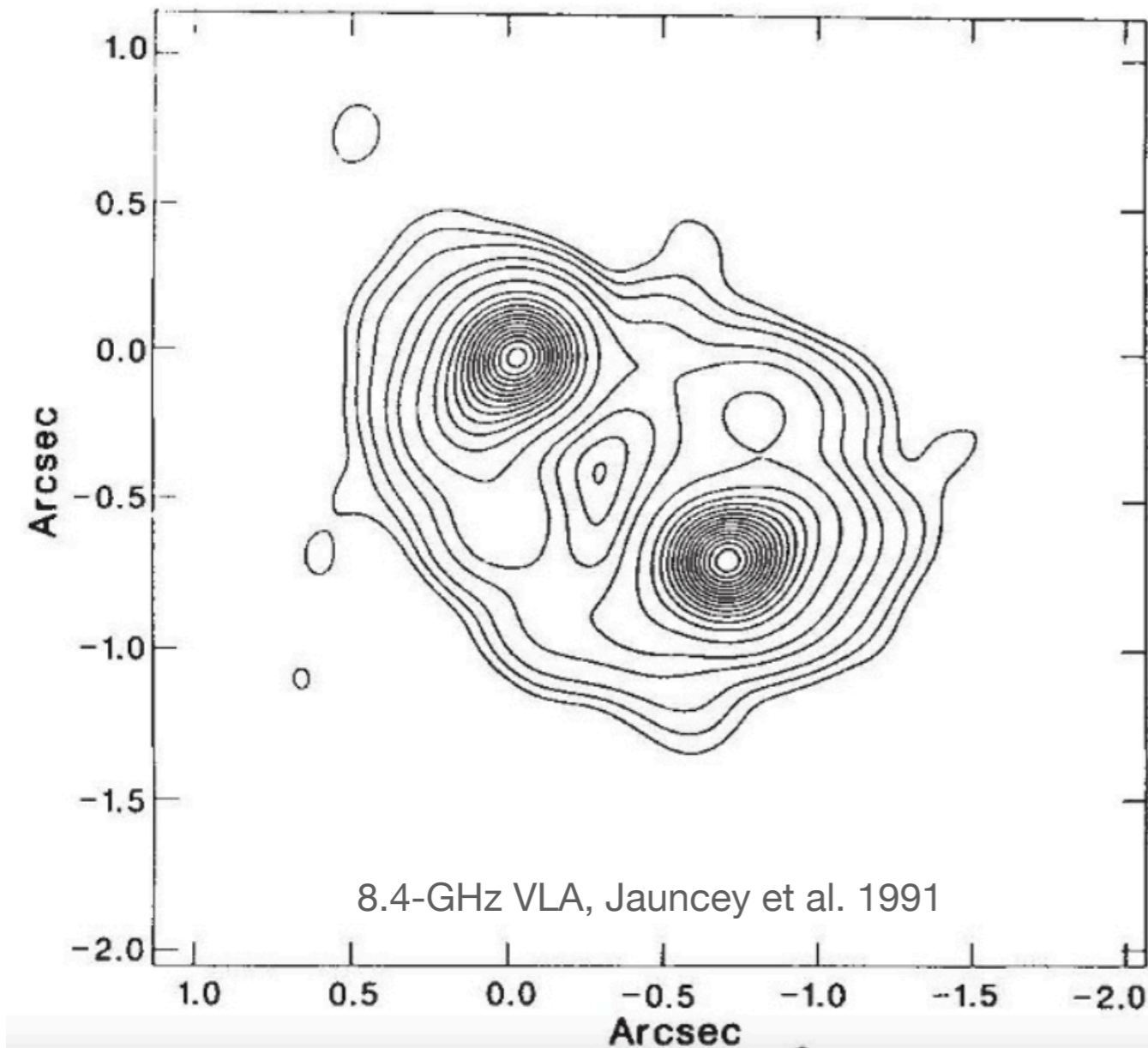
- only two gamma-ray bright blazars that are gravitationally lensed
- multiple images of one source
- time delay and magnification between the images



<https://www.mdpi.com/2073-8994/9/10/202>



- FSRQ
- two images
- separated by  $\sim 1$  arcsec
- Lovell et al. (1998) for radio core:
  - time delay:  $26^{+4}_{-5}$



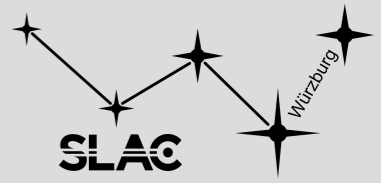
in case of not resolving two images:

$$y(t) = x(t) + a x(t - t_0)$$

magnification ratio  $a$  and delay  $t_0$   
= lens observables

light curve is a superposition of source intrinsic light curve  $x(t)$  and delayed, magnified copy of itself.

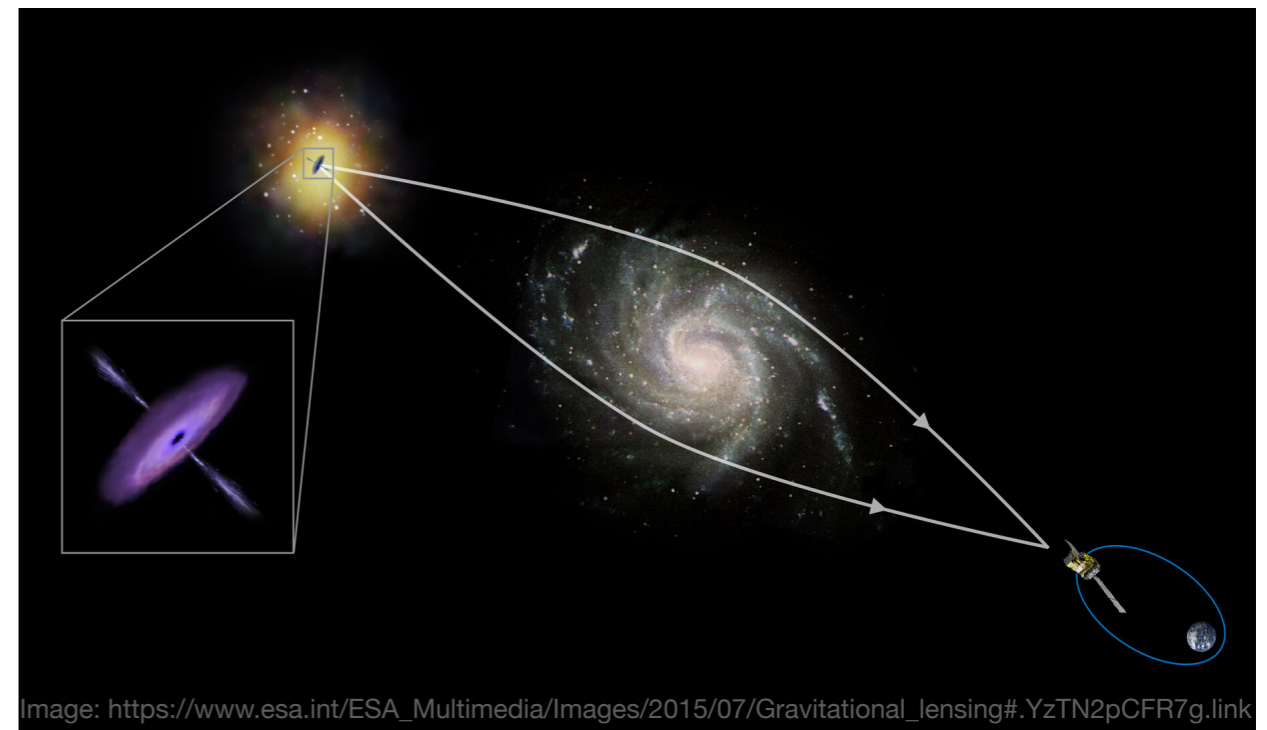
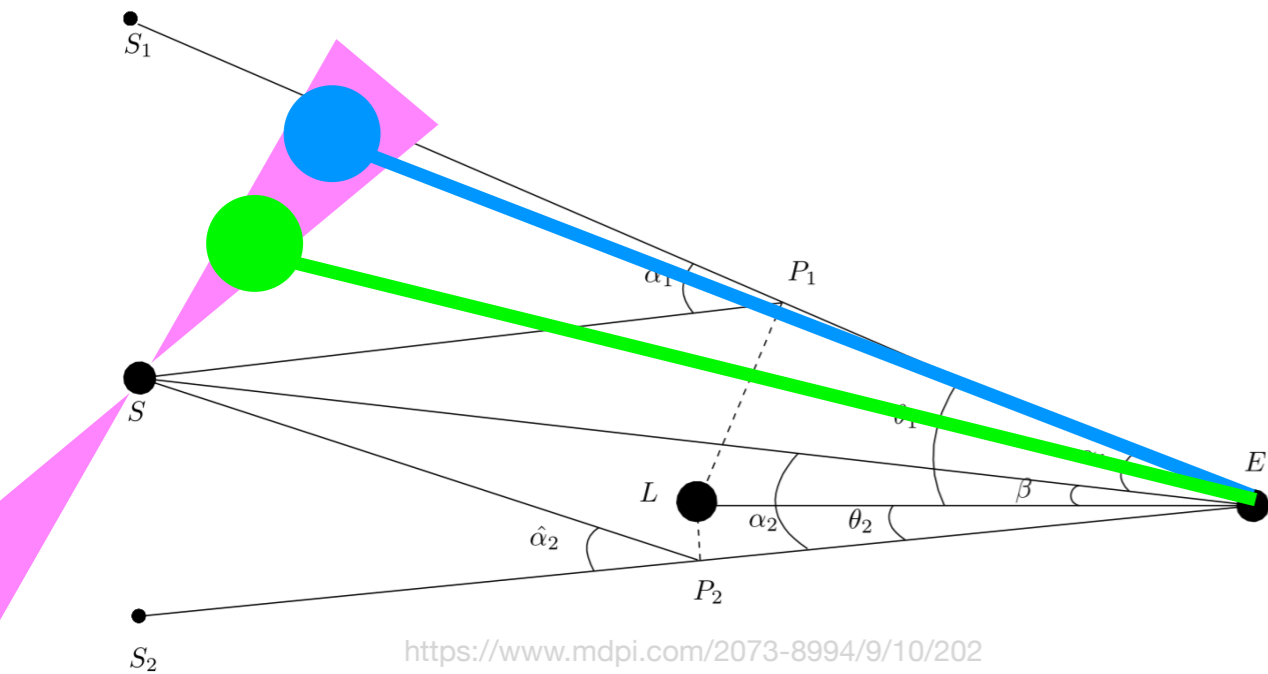
# Why care about delay?



It depends upon...

... geometry of emission region

... universe that light propagates through



constrain jet geometry

determine Hubble constant

Self correlated signal would show peak in ACF

Definition:

$$R_y(\tau) = \mathbf{E}[y(t) y(t + \tau)] = \int_{-\infty}^{+\infty} y(t) y(t + \tau) dt = \int_{-\infty}^{+\infty} |Y(s)|^2 e^{i2\pi st} ds$$

Auto-corr Theorem:

BUT: unevenly sampled measurements over a finite observation period

Discrete Correlation Function (DCF)

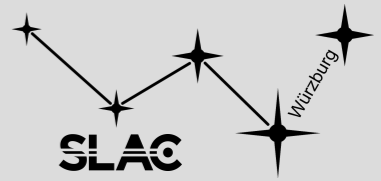
Edelson & Krolik (1988)

similar: zDCF, structure function

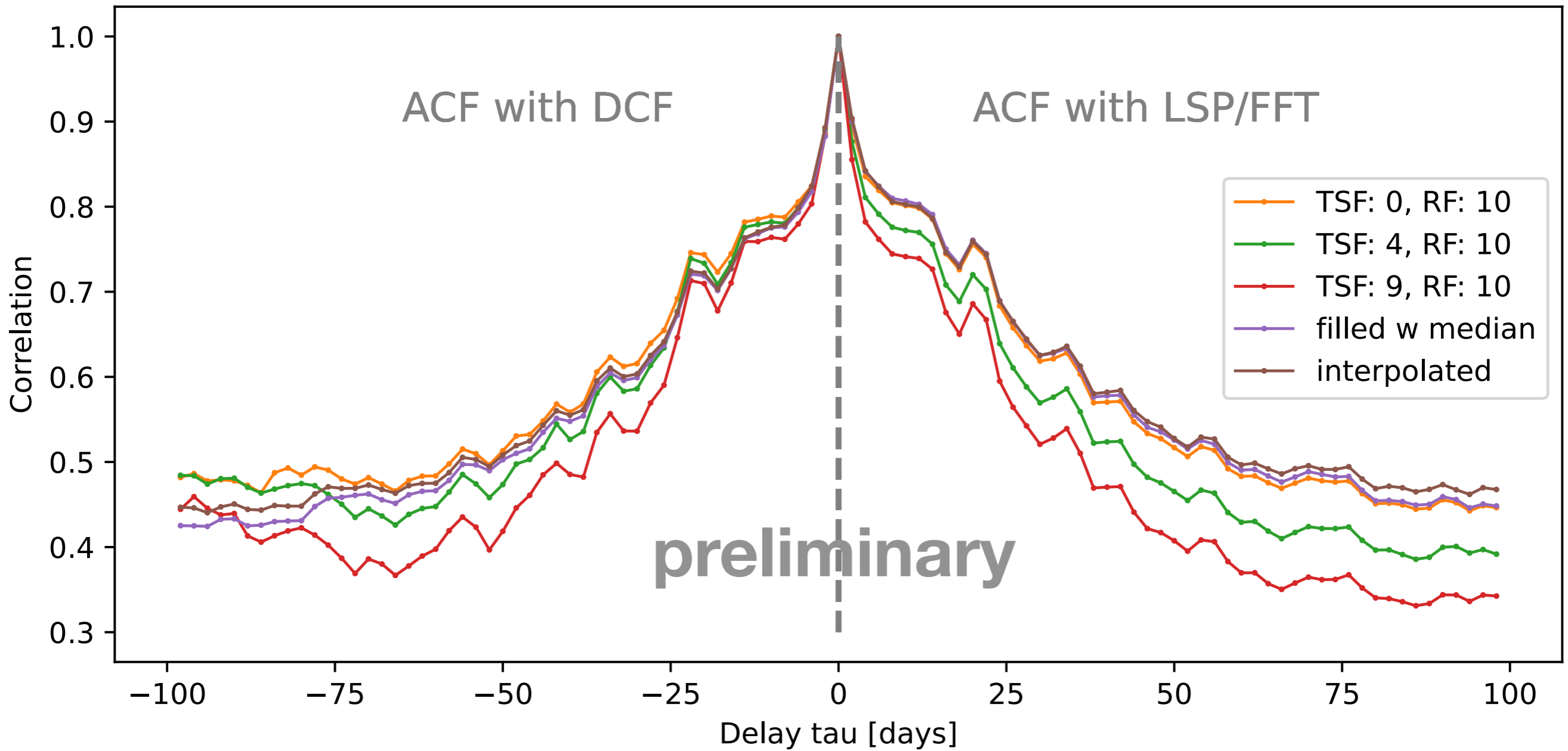
Lomb-Scargle Periodogram (LSP)

Scargle et al (1982)

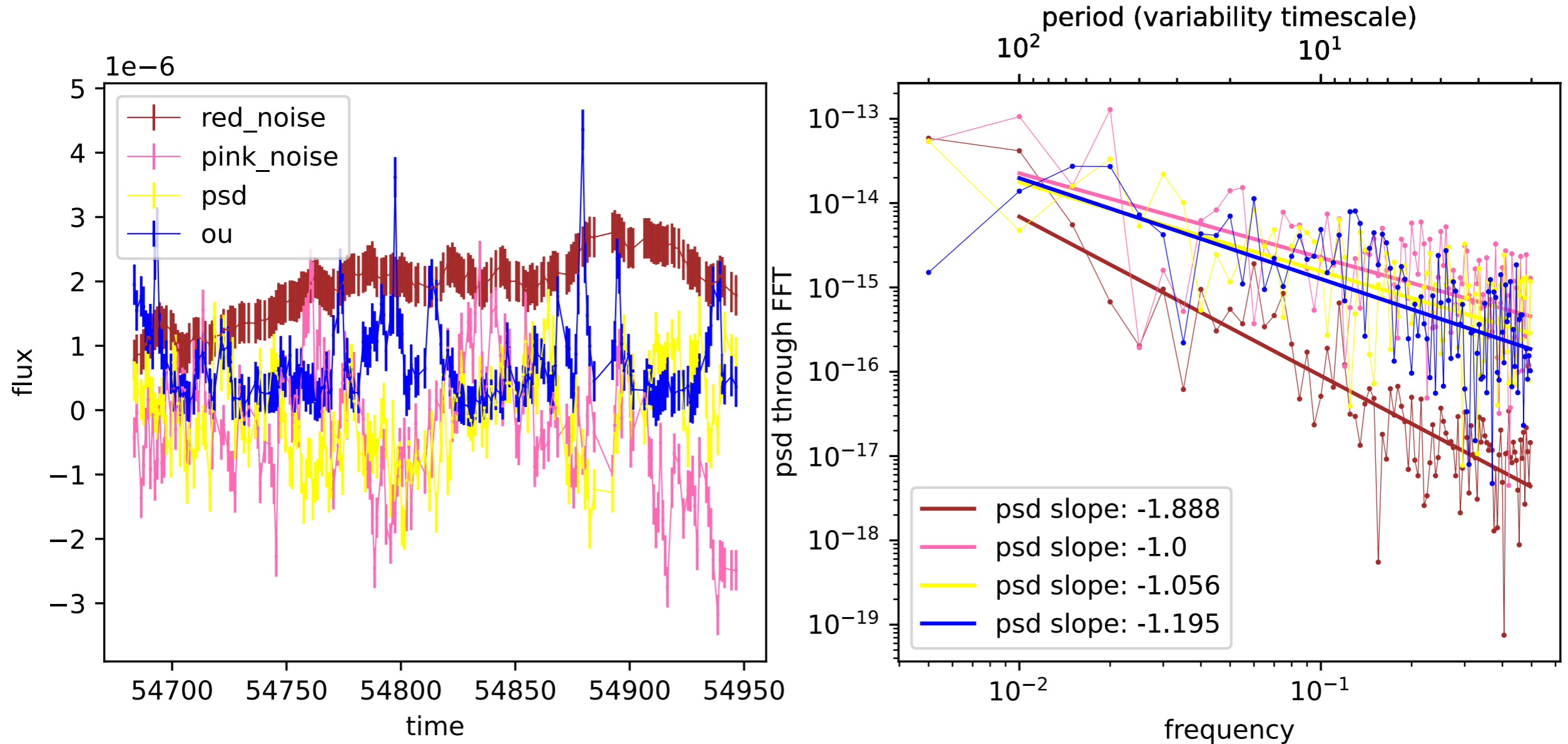
# ACF of PKS 1830-211



$$R_y(\tau) = \mathbf{E}[y(t) y(t + \tau)] = \int_{-\infty}^{+\infty} y(t) y(t + \tau) dt = \int_{-\infty}^{+\infty} |Y(s)|^2 e^{i2\pi st} ds$$



Colored noise has characteristic slope in Power Spectral Density (PSD)



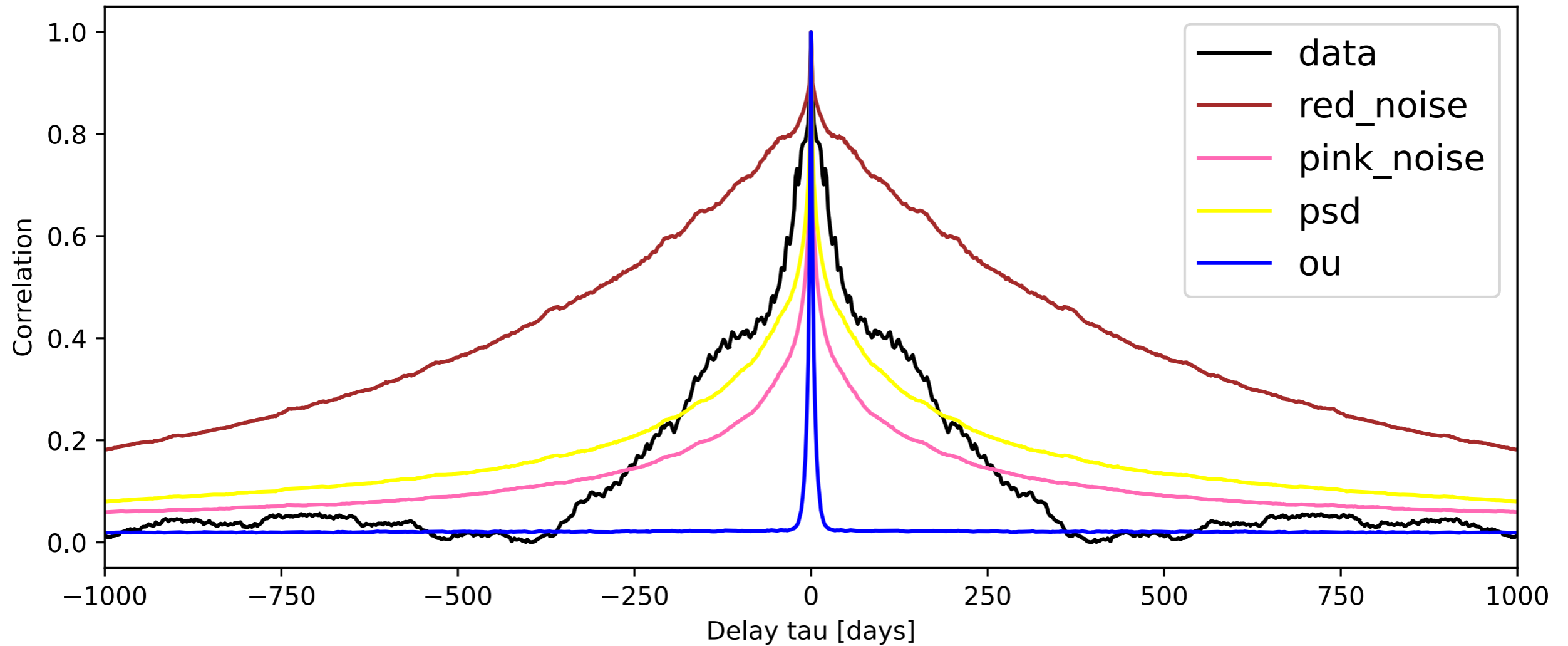
Autocorr Theorem:

also ACF will have characteristic shape



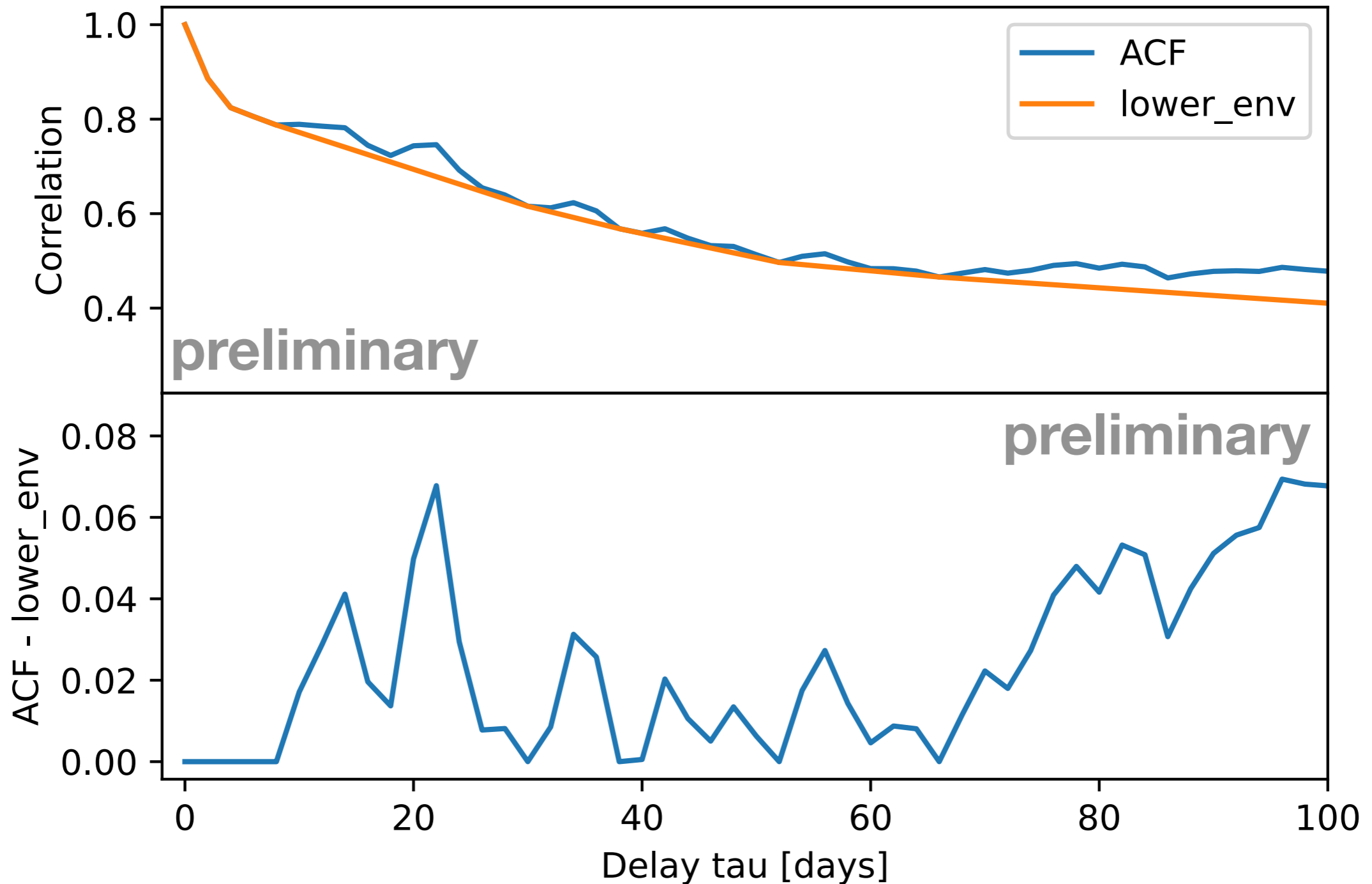
Colored noise has characteristic shape in ACF!

averaged ACFs

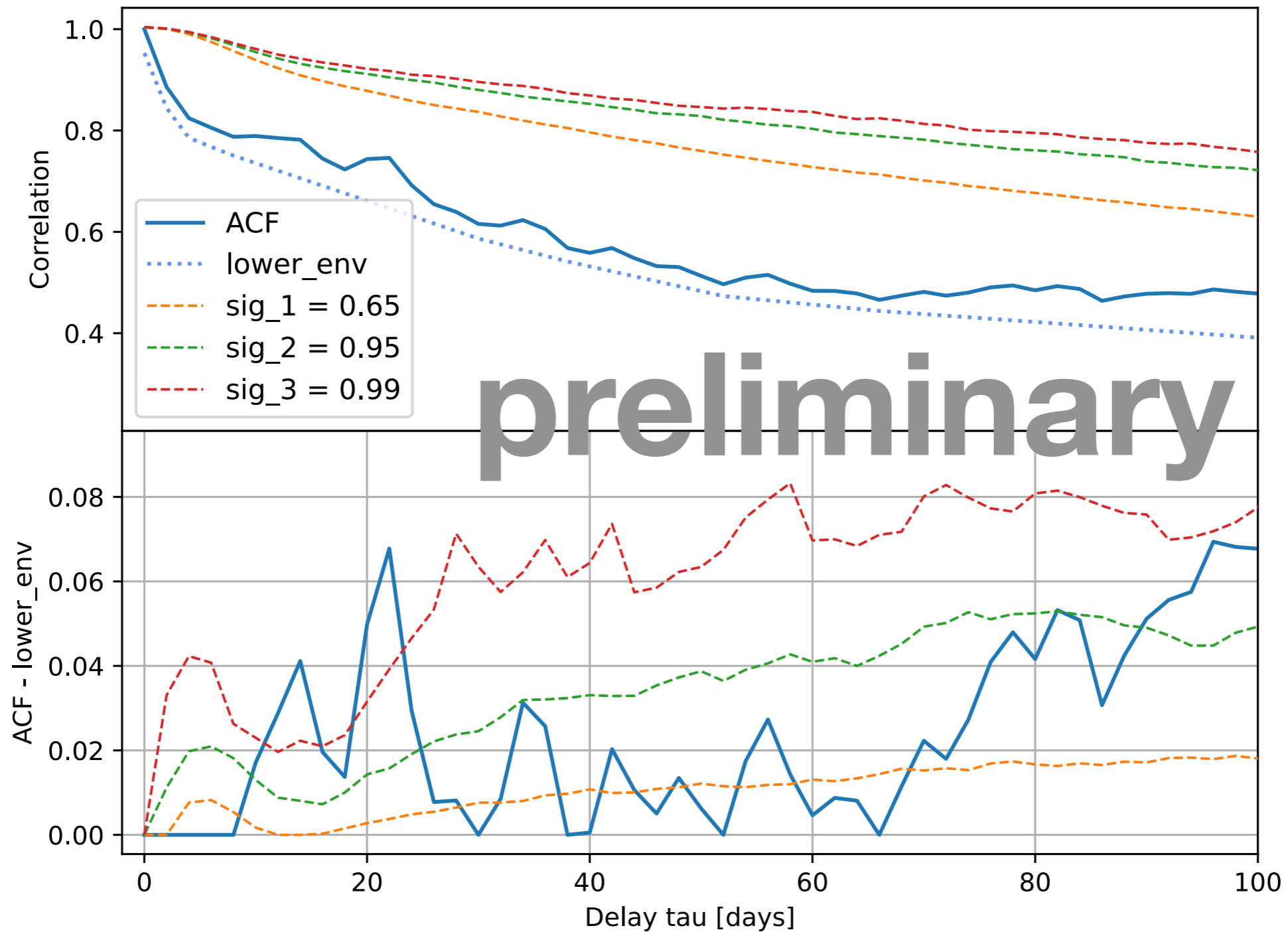


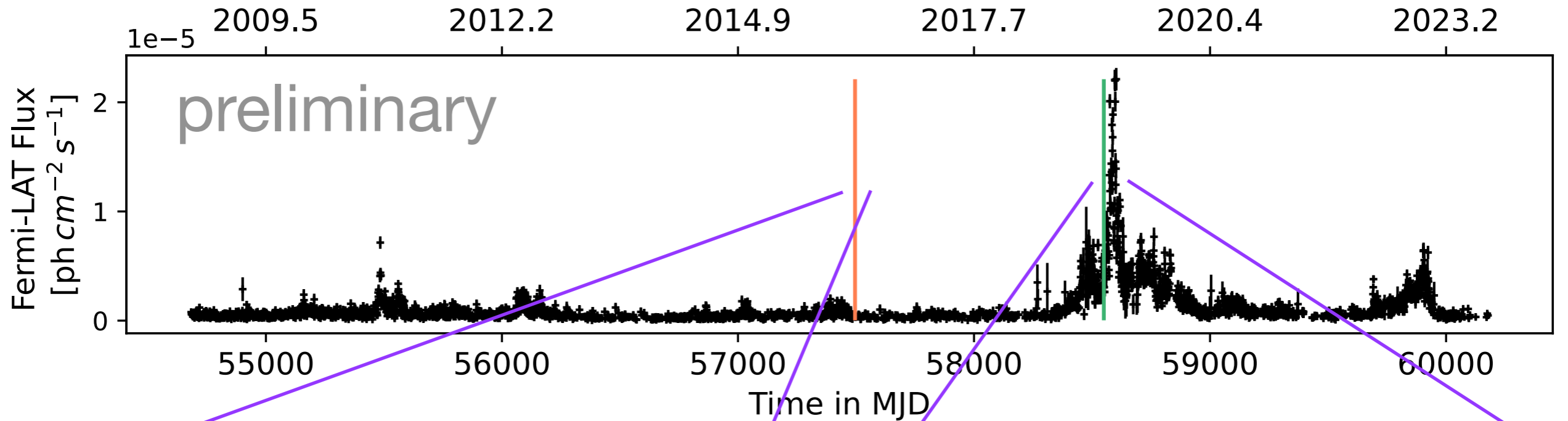
we are interested in excess over colored noise

Subtract noise contribution with mathematical description of envelope



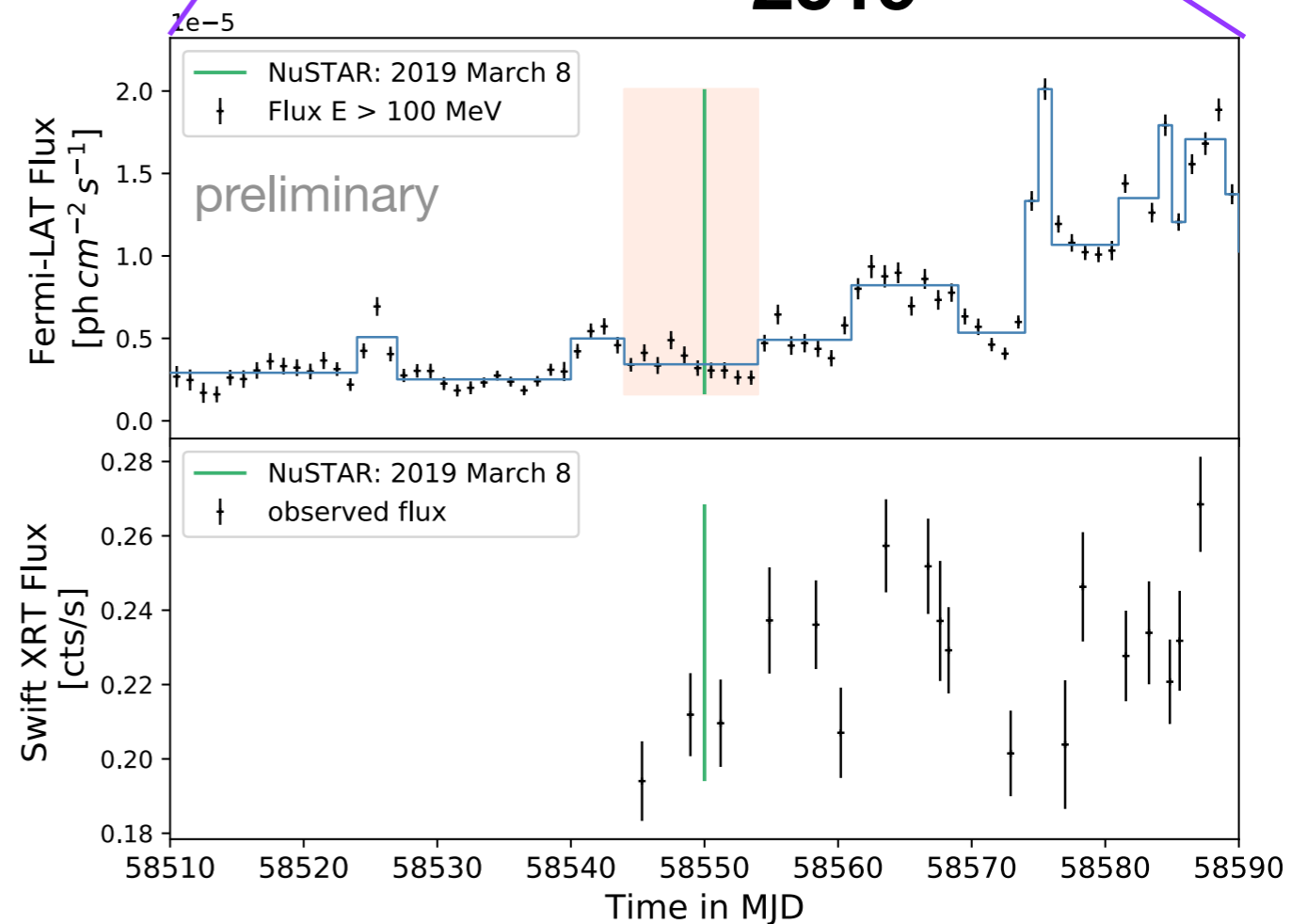
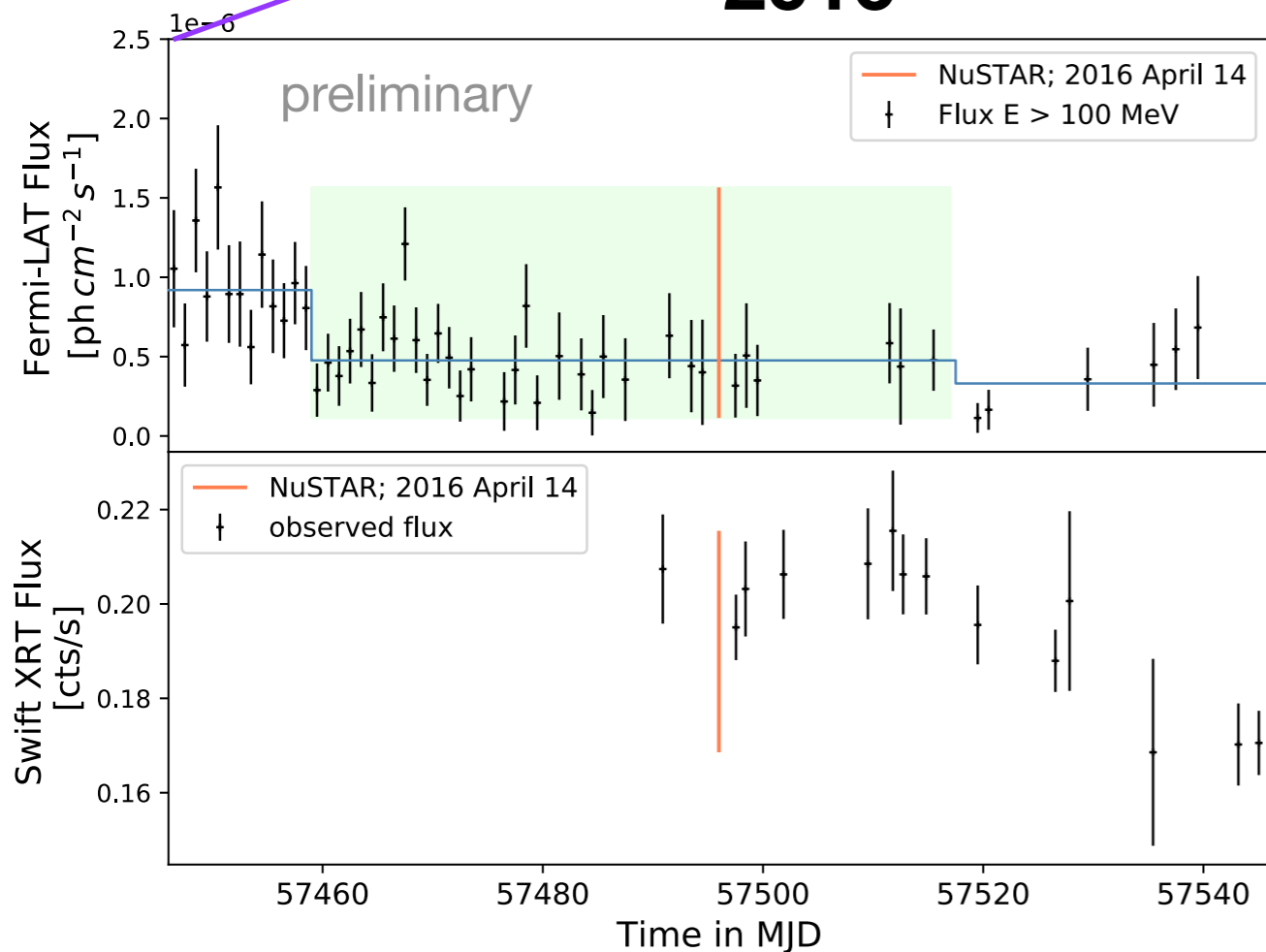
Determine significance with simulated light curves



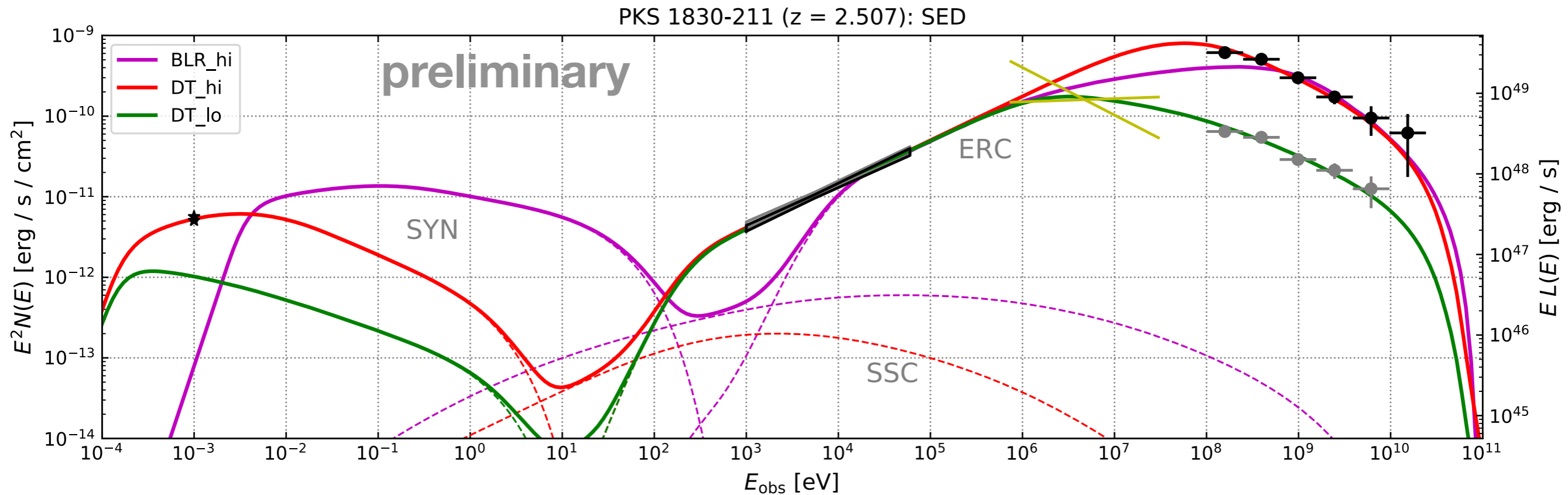


**2016**

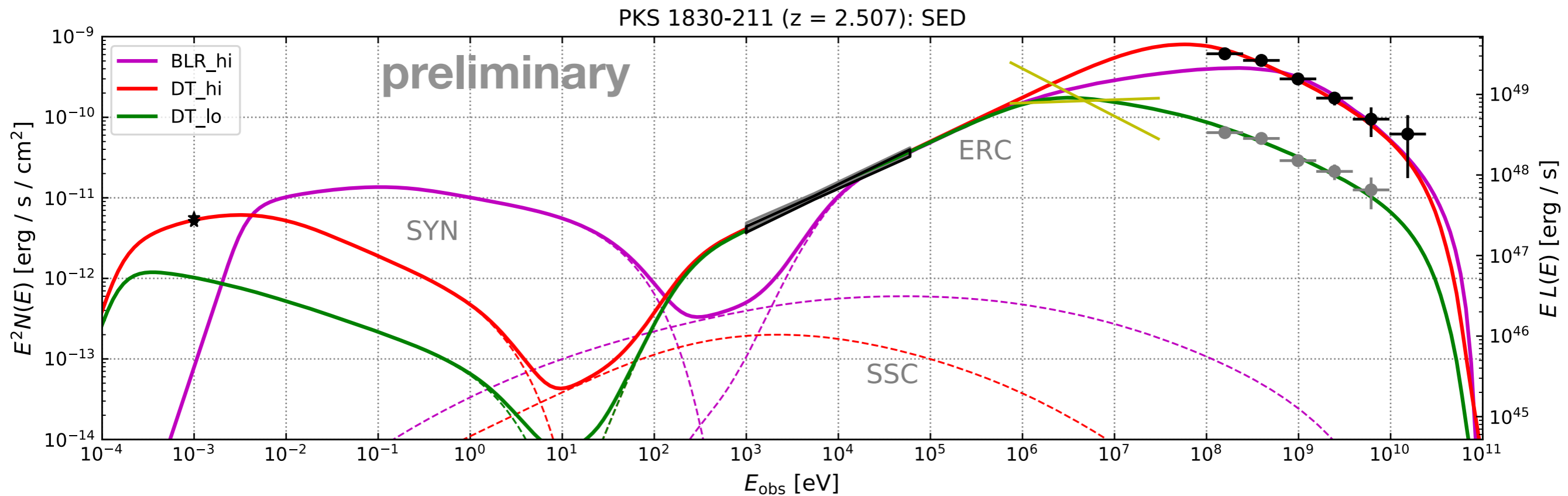
**2019**



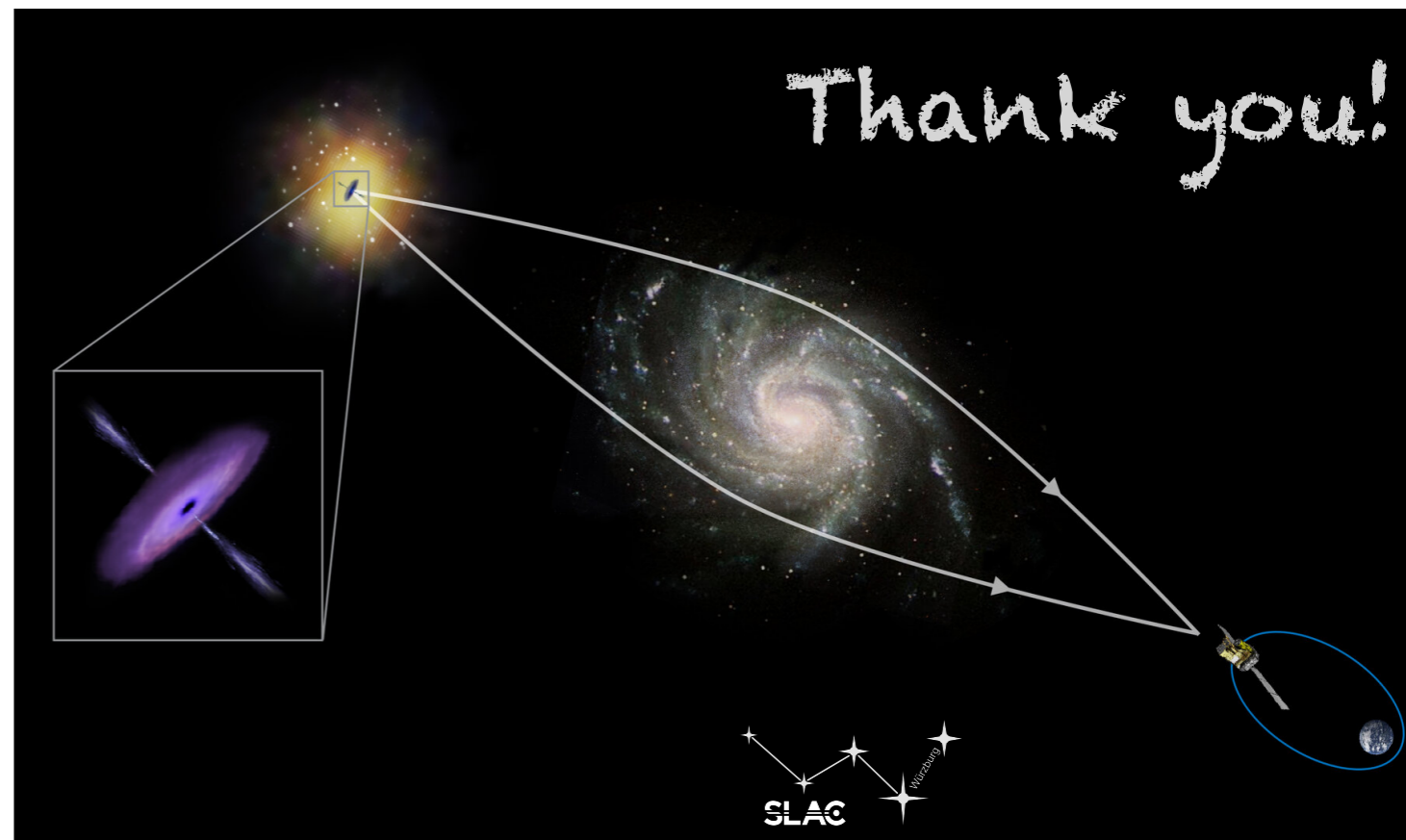
- non-thermal leptonic emission (BLAZAR, Moderski et al. 2013)
- spherical emission zone moving along conical jet
- inject energetic particles following a broken power-law distribution
- integrate emission (SYN, SSC, ERC\_BLR, ERC\_DT) over injection distance



- significant SSC contribution is incompatible with differing amplitudes
- focus on single ERC component (typical for FSRQ) with two distance scales:
  - $r_{\text{BLR}}$  (magenta): cannot reproduce soft x-ray and gamma-rays
  - $r_{\text{DT\_hi}}$  (red): fits the high state data well
  - $r_{\text{DT\_lo}}$  (green): fits the low state data well (lower break in  $e_l$  distribution)



- consistent lag throughout the whole light curve in agreement with delay from old radio measurements
- SED can be modeled with single emission zone and external compton emission from the Torus
- soon to be published; currently in internal Fermi-LAT review



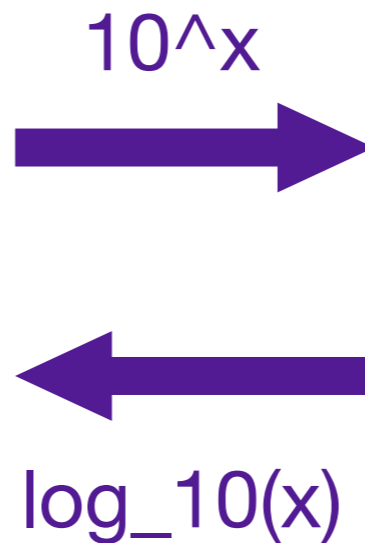
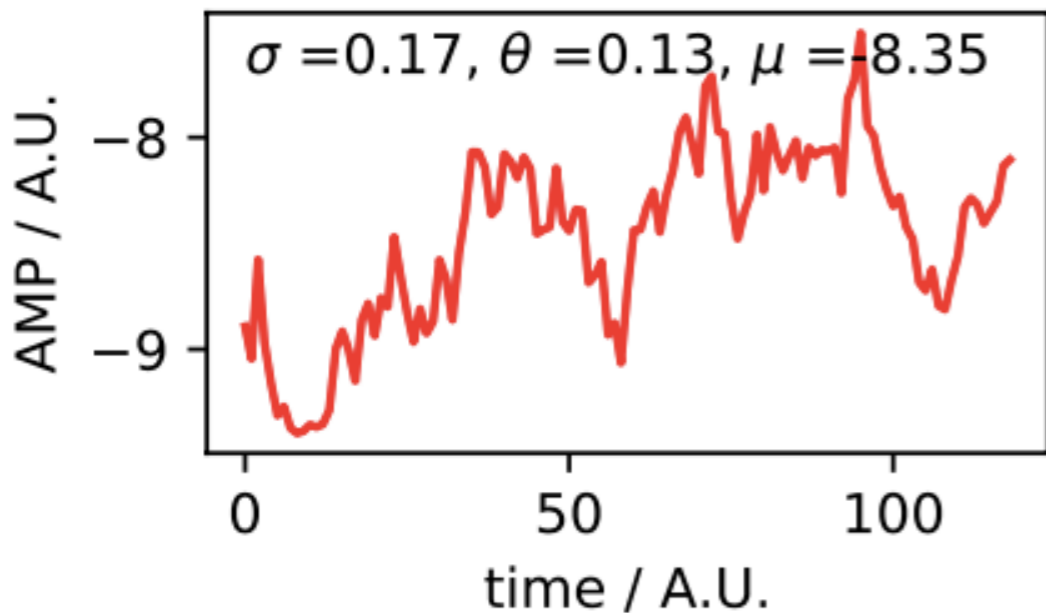
A&A 645, A62 (2021)  
<https://doi.org/10.1051/0004-6361/202039097>  
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**Astronomy  
&  
Astrophysics**

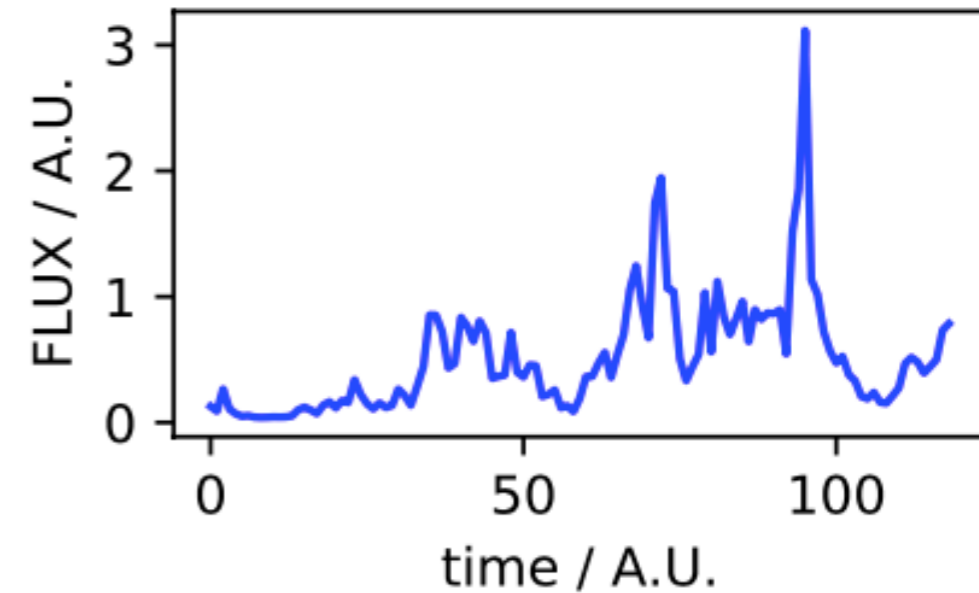
## Ornstein-Uhlenbeck parameter extraction from light curves of *Fermi*-LAT observed blazars

Paul R. Burd<sup>1</sup>, Luca Kohlhepp<sup>1</sup>, Sarah M. Wagner<sup>1</sup>, Karl Mannheim<sup>1</sup>, Sara Buson<sup>1</sup>, and Jeffrey D. Scargle<sup>2</sup>

OU time series



OU LC



Monthly binned *Fermi*-LAT LCs show characteristic OU parameters..  
physical interpretation?



## Fokker-Planck equation

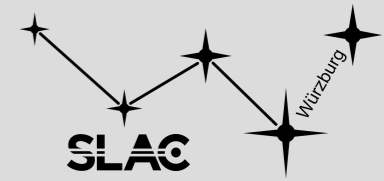
$$\frac{\partial f(t, \mathbf{x})}{\partial t} = - \sum_{i=1}^N \frac{\partial}{\partial x_i} \left( A_i(t, \mathbf{x}) f(t, \mathbf{x}) \right) + \sum_{i=1}^N \sum_{j=1}^N \frac{\partial^2}{\partial x_i \partial x_j} \left( \frac{1}{2} \sum_{k=1}^N B_{i,k}(t, \mathbf{x}) B_{j,k}(t, \mathbf{x}) \right)$$

is equivalent to (Arnold 1973)

$$\frac{d\mathbf{X}_{t,i}}{dt} = A_i(t, \mathbf{X}_t) + \sum_{j=1}^N B_{i,j}(t, \mathbf{X}_t) \frac{dW_\tau}{d\tau}$$

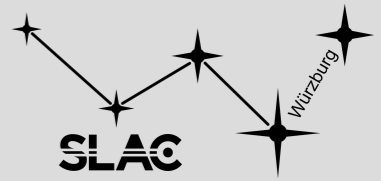
a system of Stochastic Differential Equations (SDEs)

# SED modeling

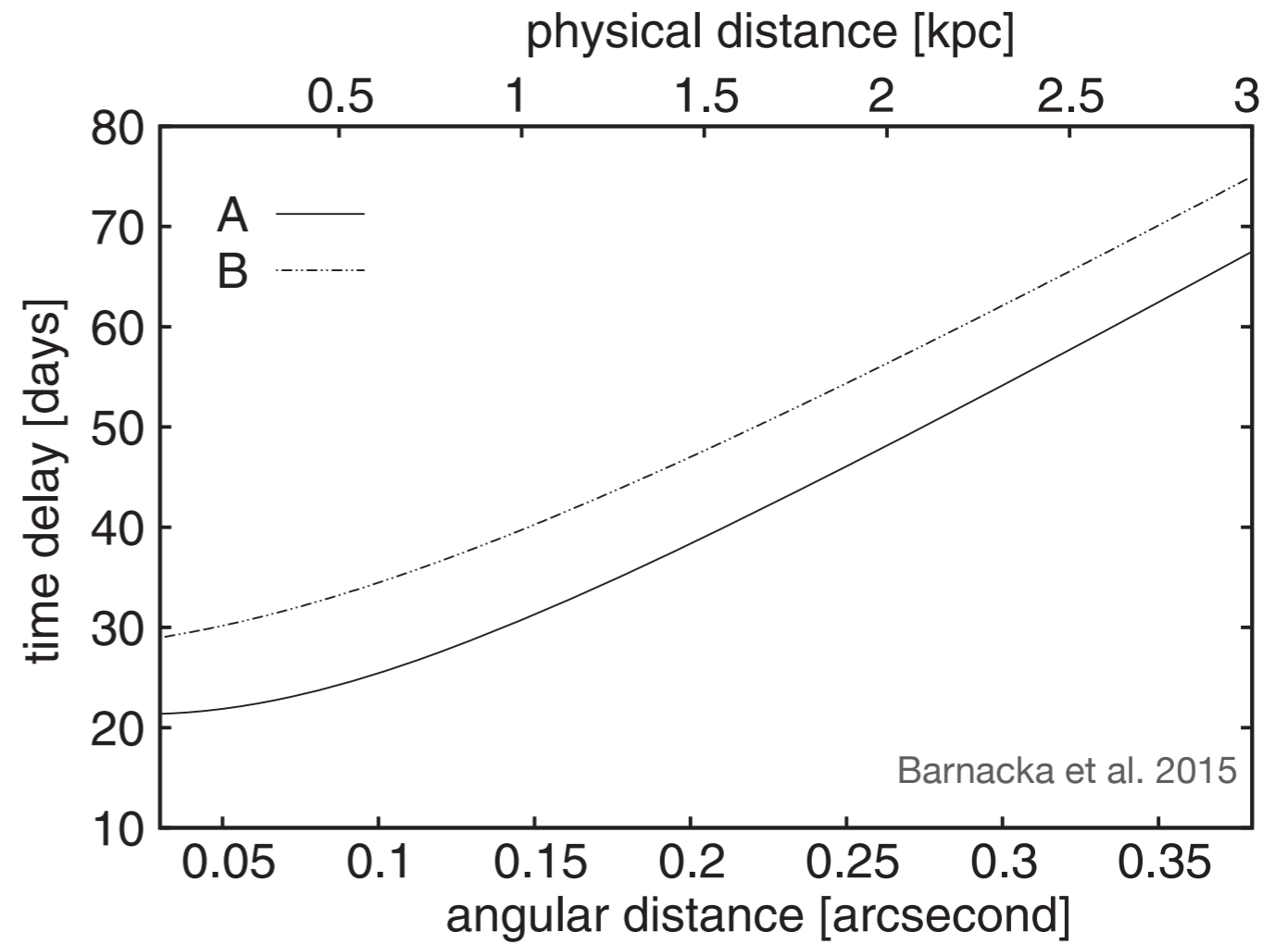
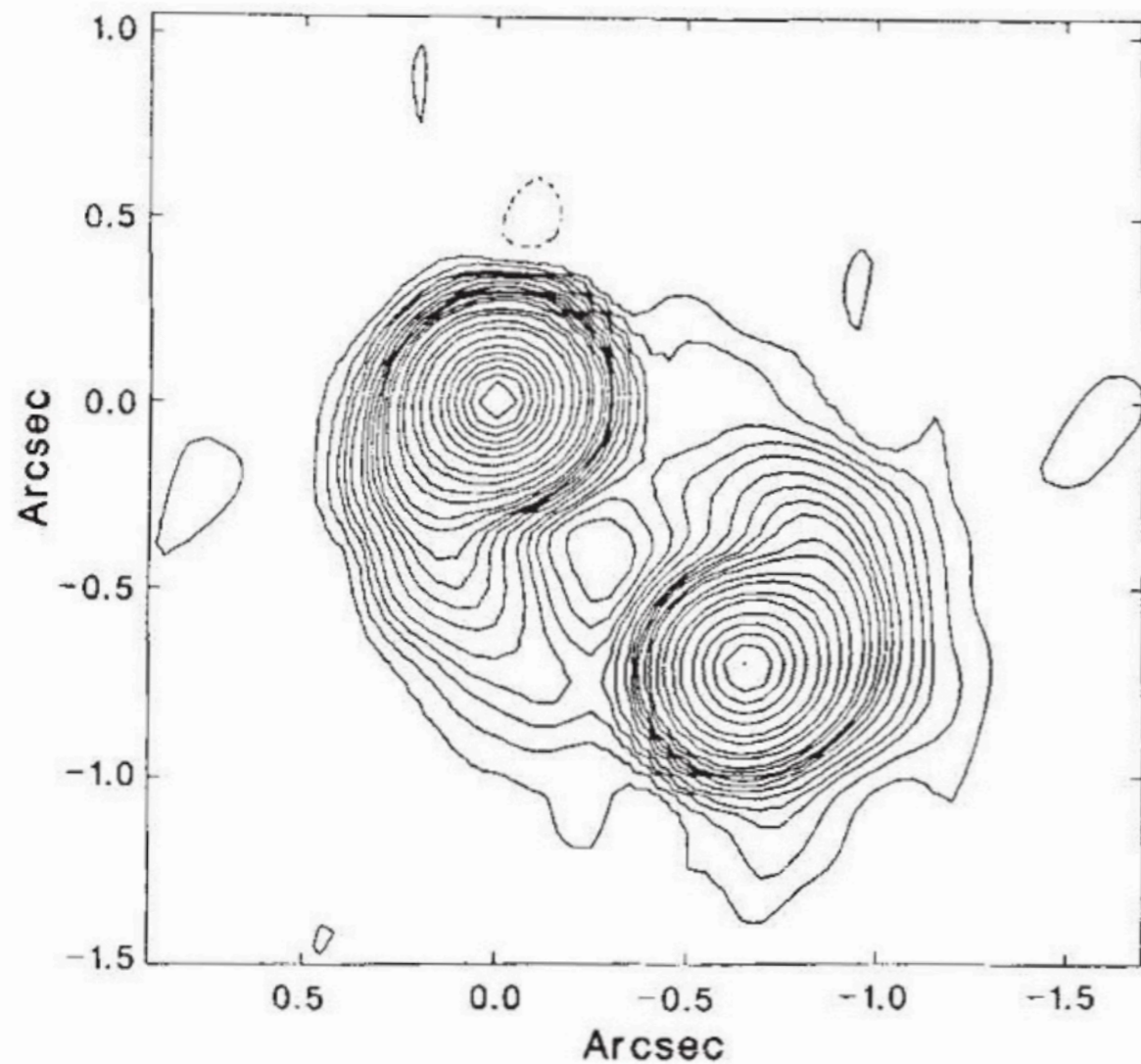


		BLR_hi			DT_hi		DT_lo	
		Model 1	Model 1a	Model 2	Model 2a	Model 3	Model 4	Model 5
pc / cm	3,086E+18							
magnification	mu	1	10	1	10	10	10	10
distance	r [pc]	0,084	0,084	3,338	3,338	0,324	3,338	0,528
dominant soft photons		BEL	BEL	IR	IR	BEL	IR	IR (*)
Lorentz factor	Gamma	30	30	30	30	20	30	30
jet half-opening angle	theta_j	0,0333	0,0333	0,0333	0,0333	0,05	0,0333	0,0333
viewing angle	theta_obs	0,0333	0,0333	0,0333	0,0333	0,05	0,0333	0,0333
magnetic field	B [G]	0,7	2,25	0,017	0,037	0,093	0,037	0,027
electron energy distribution	gamma_min	1	1	1	1	3	1	1
	gamma_br	580	580	900	900	320	115	300
	gamma_max	1,0E+4	1,0E+4	1,5E+4	1,5E+4	1,0E+4	1,5E+4	1,5E+4
	p_1	1,85	1,85	1,9	1,9	1,9	1,9	1,9
	p_2	3,3	3,2	3,3	3,3	3,1	3,1	3,3
electron jet power	log10 L_e [erg/s]	46,4	45,4	47,4	46,4	46,5	46,2	46,9
proton jet power (no pairs)	log10 L_p [erg/s]	48,9	47,9	49,7	48,7	48,5	48,7	49,3
magnetic jet power	log10 L_B [erg/s]	44,1	45,1	44,1	44,7	43,5	44,7	42,9
radiation jet power	log10 L_r [erg/s]	46,4	45,4	46,5	45,5	45,8	45,0	45,5
fits X-rays		no	no	yes	yes	no	yes	yes

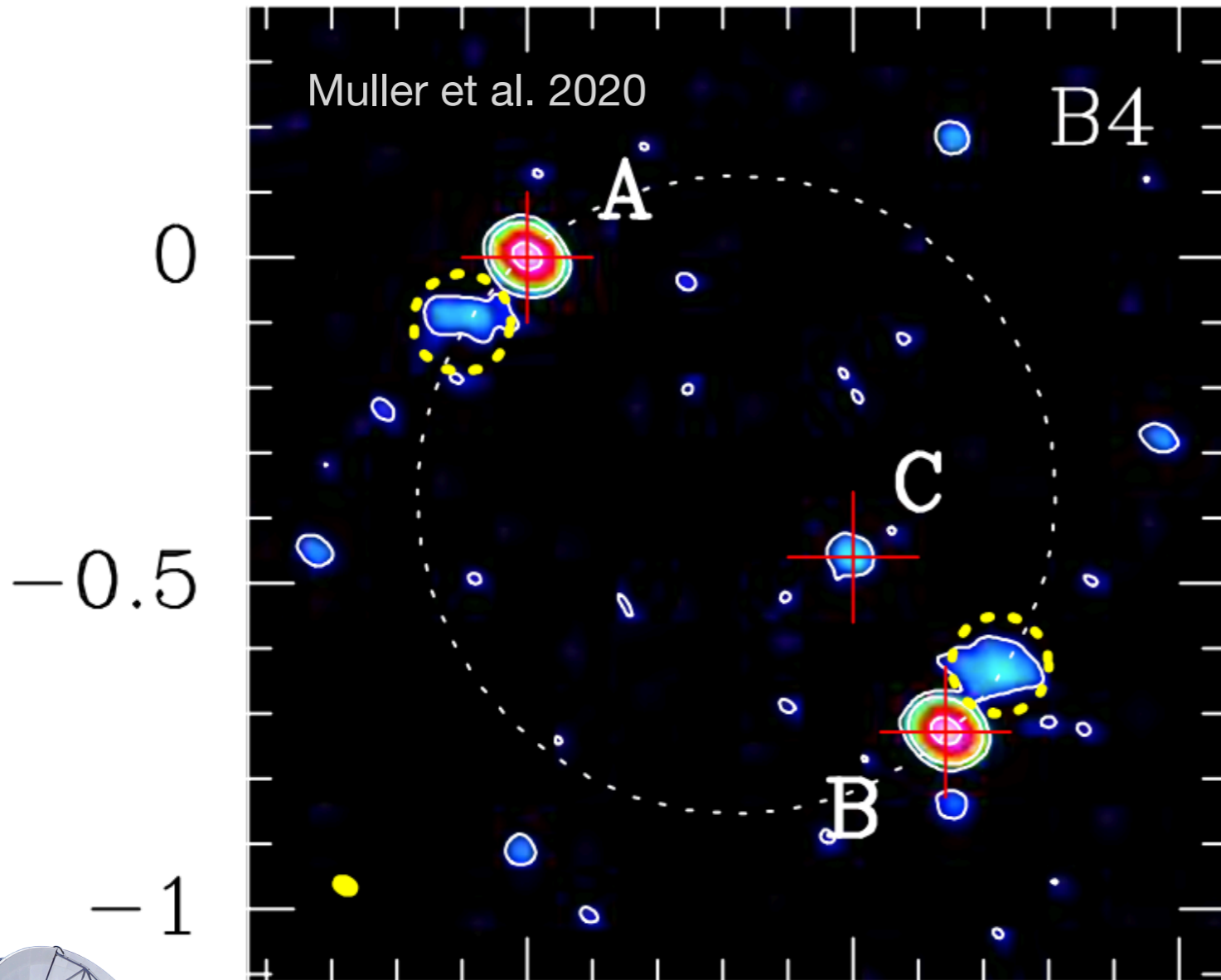
# Delay and Jet



8.4-GHz observation with VLA, Jauncey et al. 1991



Dec. offset (arcsec)



- FSRQ
- relatively close to galactic plane
- gravitationally lensed
  - two images (A & B) with core (red cross) and faint extension (yellow circle)
  - separated by  $\sim 1$  arcsec
  - much fainter third image (C) neglected here



ALMA

R.A. offset (arcsec)

## Time delay in Fermi-LAT LC of PKS 1830-211

**(A)**

Peak  
distances

**19.75 - 26.25**

**(B)**

Auto  
correlation

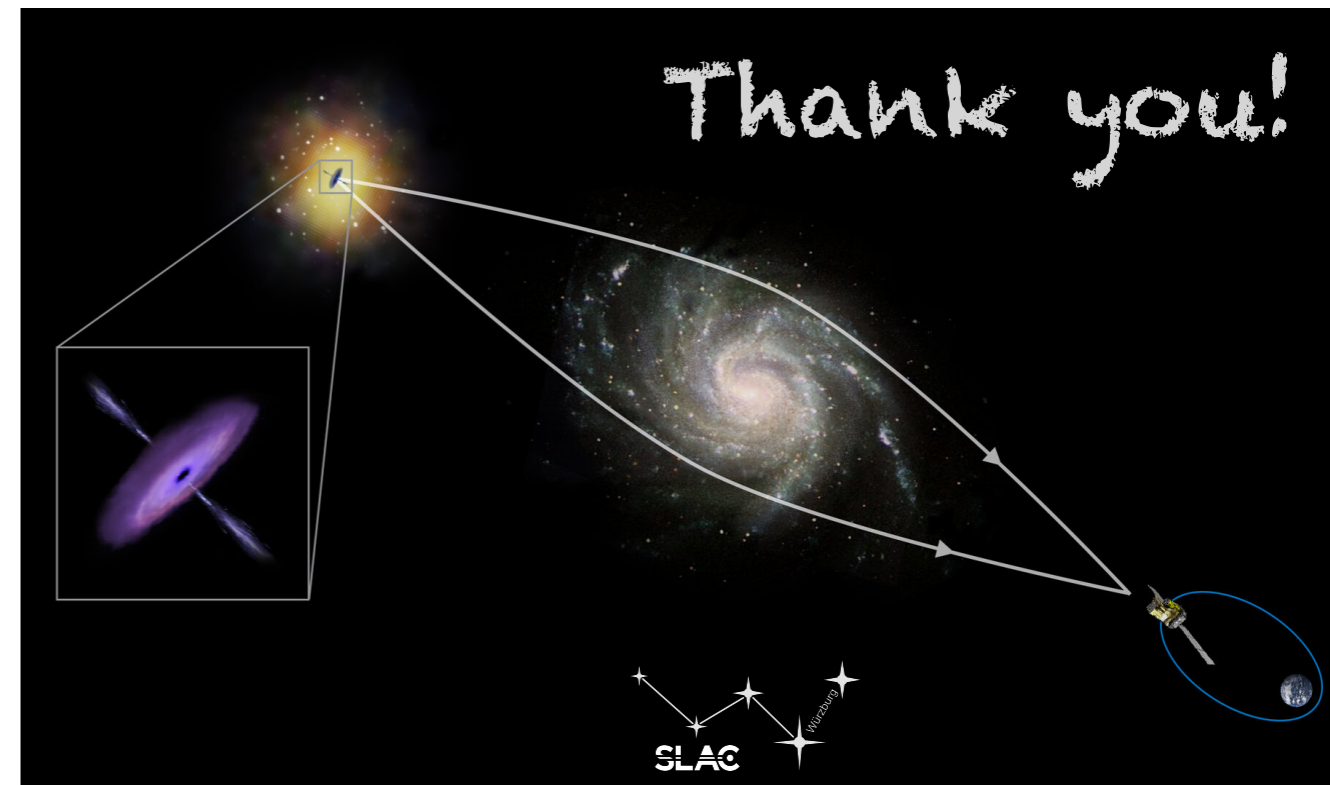
**21.96 +/- 0.30**

**(C)**

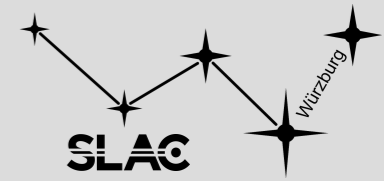
Metric  
optimization

**22.38 +/- 5.66**

- consistent lag throughout the whole light curve in agreement with radio
- currently in internal Fermi-LAT review

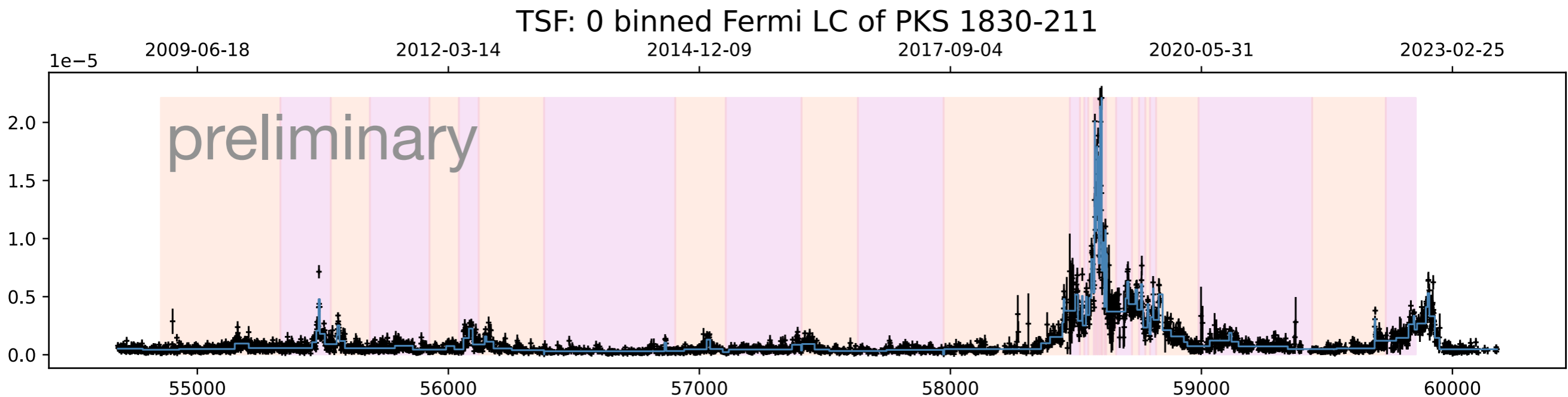


# A) Peak distances

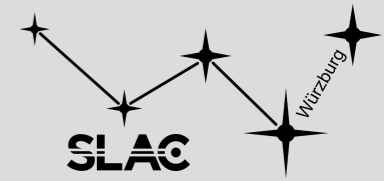


Delay induced by gravitational lensing imprinted in structure of light curve?

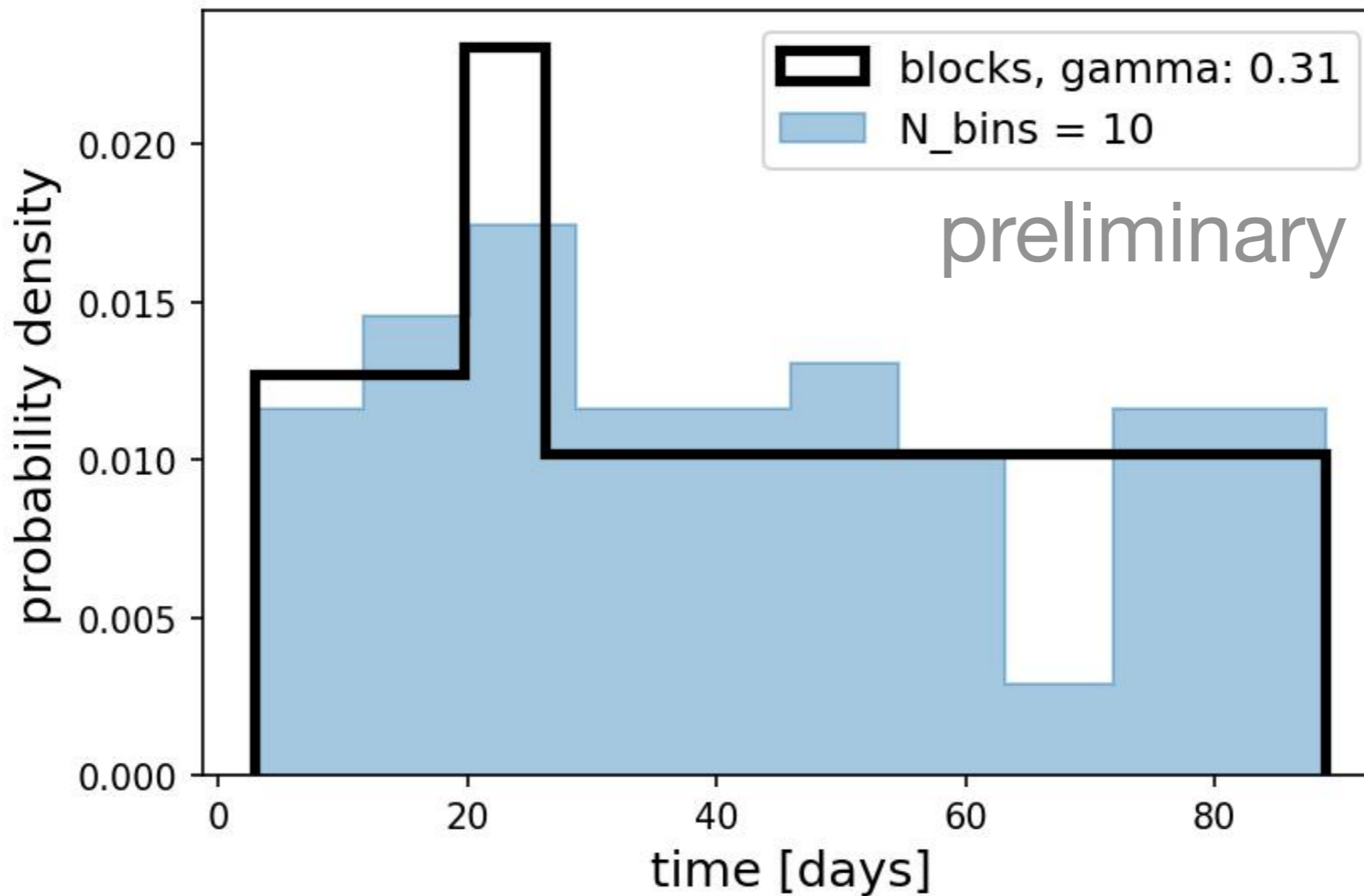
- ➔ apply Bayesian block and HOP analysis (Wagner et al. 2022)
- ➔ detection of 33 flares (“hopjects”)
- ➔ distribution of distances between all peaks



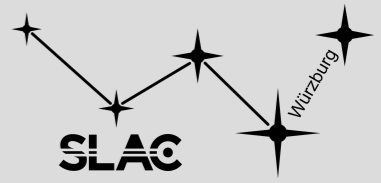
# A) Peak distances



Peak distances < 90d in regular (blue) and Bayesian binning (black), total: 80



**significantly higher probability for distance to lay between 19.75 and 26.25 days**



We know behavior of light curve based on lensing

$$y(t) = x(t) + a x(t - t_0) \xleftrightarrow{FT} Y(s) = X(s)(1 + a e^{-i2\pi t_0 s})$$

➔ solve for intrinsic light curve

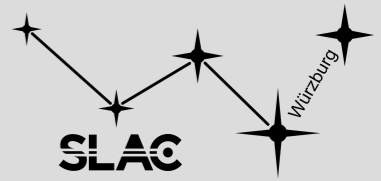
$$x(t) = IFT \left[ \frac{FT[y(t)]}{1 + a e^{-i\omega t_0}} \right]$$

➔ fit for lens observables

- define a metric  $M$  to judge whether  $x(t)$  is a “good” intrinsic light curve
- find values for lens observables  $a, t_0$  that optimize metric

$$\text{Estimated}(a, t_0) = \text{argmin } M[x(t|a, t_0)]$$

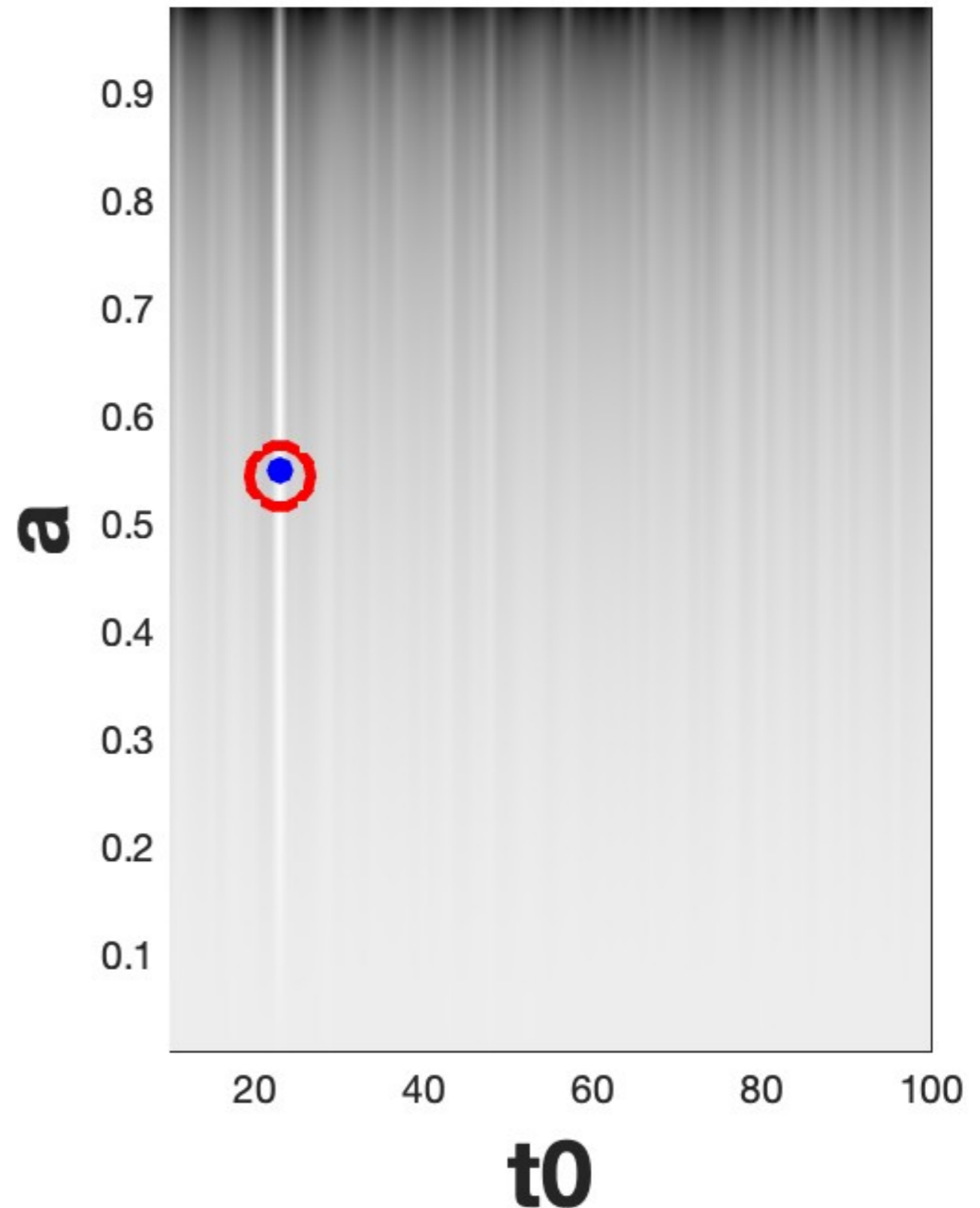




Many properties could be utilized as metric. One example:  
 → Variance of intrinsic light curve

$$M[x(t)] = \text{var}(x(t))$$

Figure to the right:  
 test case for noise-free simulated data.  
 Known parameter values: blue dot,  
 estimated values (minimum of variance  
 of  $x(t)$ ): red circle



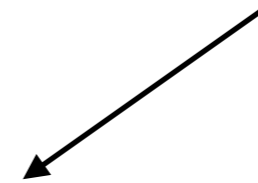
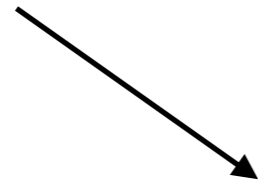
Estimate uncertainty with bootstrap method = mimic sampling process  
not possible for flux itself so use photon arrival times

assume flux is proportional  
to number of photons

$$F = C N_{\text{photons}}$$

assume photons follow  
a Poisson distribution

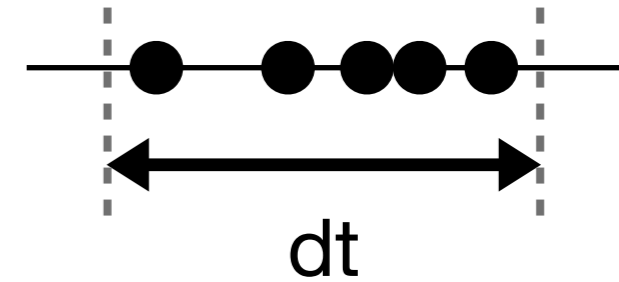
$$\sigma(N_{\text{photons}}) = \sqrt{N_{\text{photons}}}$$



Convert fluxes into time series of photon counts:

$$\mathbf{P}_t = \mathbf{F}_t \frac{\text{median}(\mathbf{F}_t)}{\text{median}(\mathbf{err}_t^2)}$$

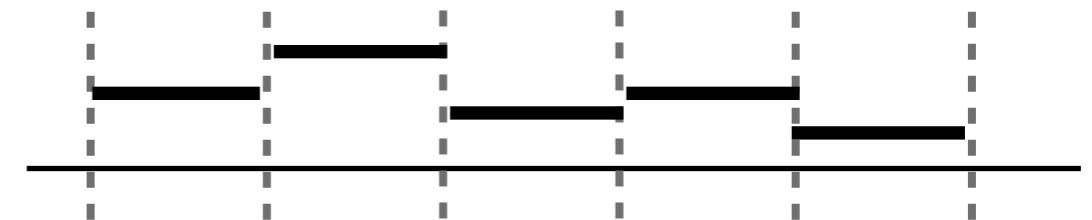
1. For each LC bin with flux  $F$  and width  $dt$   $\rightarrow$  generate  $P$  random, uniformly distributed arrival times



2. Set of all photon arrival times can be bootstrapped: draw random sample with replacement

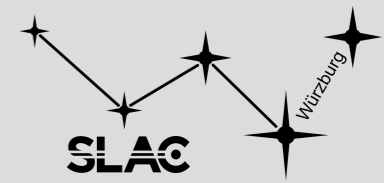


3. Histogram of this sample corresponds to randomized LC

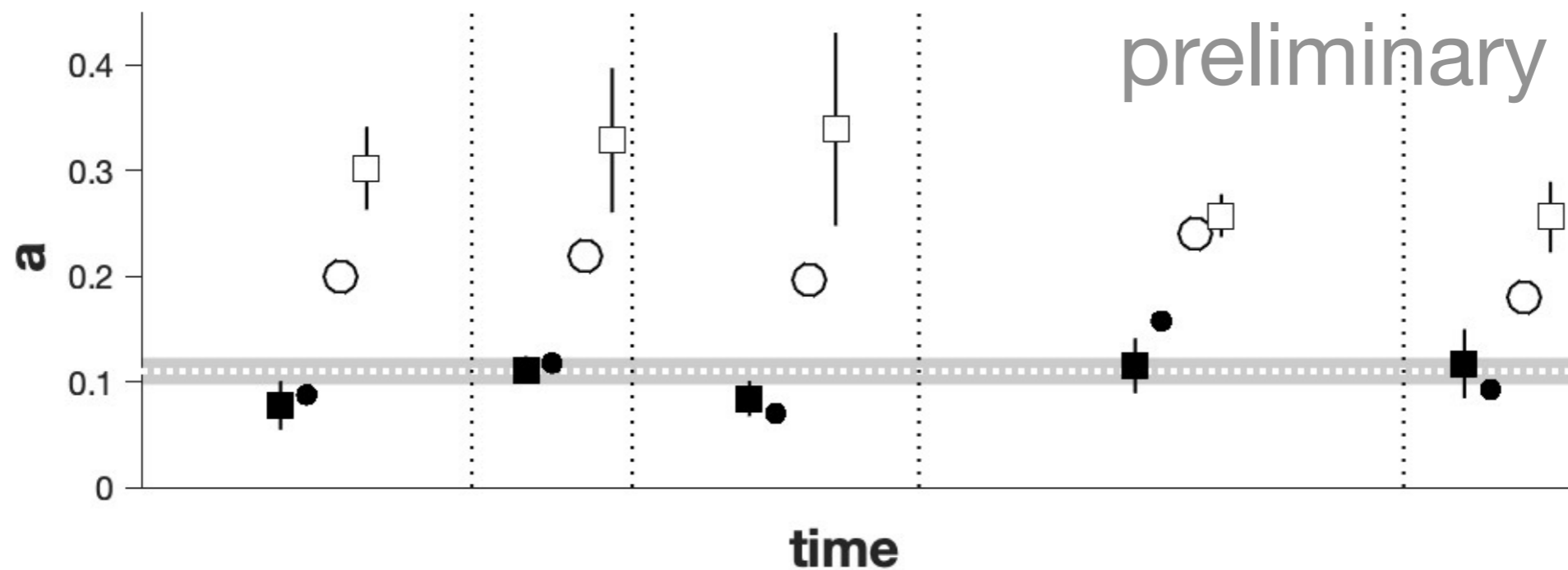
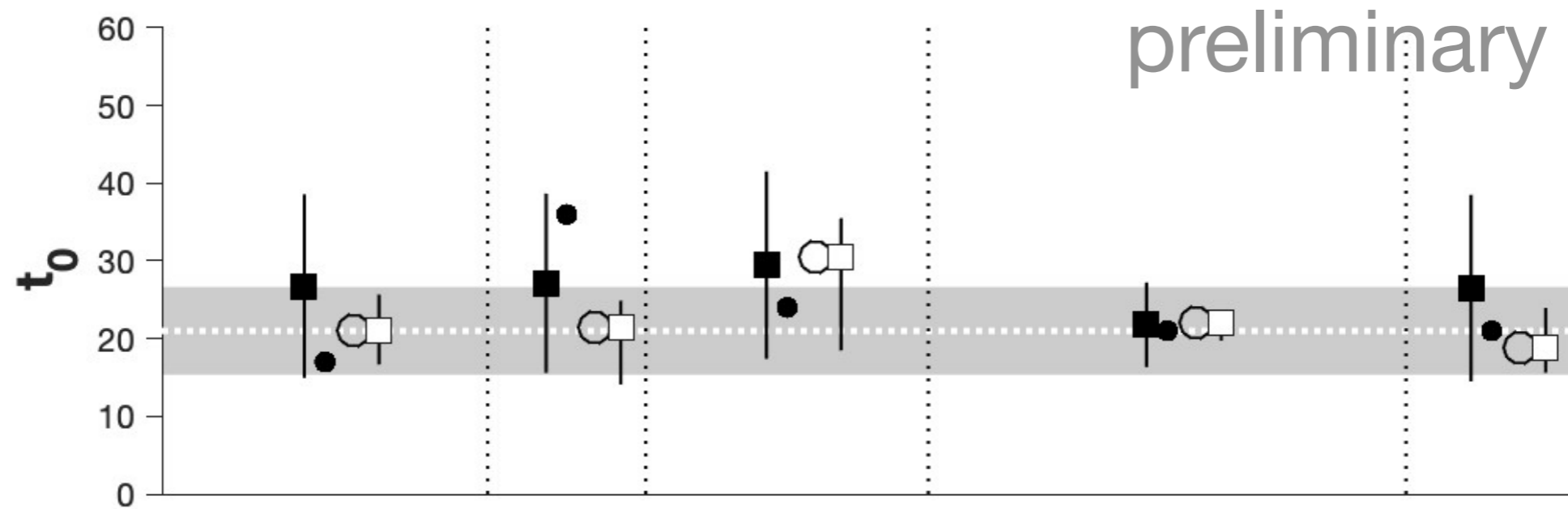


4. Run analysis with many randomized LCs and compute mean and standard deviation of best fit values for lens observables

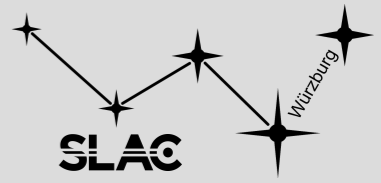
# Overall results



solid circles are the metric optimized estimates; solid squares and lines are the bootstrap means and variances. Open symbols at similarly for the autocorrelation-based estimates using Equation



Reference	Delay [d]	Magn.	Range	Data (binning)	Method
van Ommen et al. (1995)	$44 \pm 9$	$1.31 \pm 0.02$	1990 Jun - 1991 Jul	VLA at 8 and 15 GHz	Assume lensed images each consist of core, knot and contribution from Einstein-ring. Determine flux ratio between those components to derive time delay and magnification ratio.
Lovell et al. (1998)	$26^{+4}_{-5}$	$1.52 \pm 0.05$	1997 Jan - 1998 Jul	ATCA at 8.6 GHz	Dispersion analysis method with flux density light curve of compact component observed in each image.
Wiklind & Combes (2001)	$24^{+5}_{-4}$	not stated	1996 - 2001	SEST 15 m telescope	Dispersion analysis method with flux of compact component in each image estimated through molecular absorption features.
Barnacka et al. (2011)	$27.1 \pm 0.6$	magn	2008 Aug 4 - 2010 Oct 13	<i>Fermi</i> -LAT (2d, 1d, 23h)	double power spectrum
Abdo et al. (2015)	none	magn	2008 Aug 4 - 2011 Jul 25	<i>Fermi</i> -LAT (2d, 7d)	auto-correlation
	none	magn	2010 Oct 2 - 2011 Mar 1	<i>Fermi</i> -LAT (12h)	(a) auto-correlation: peak at $(19 \pm 1)$ d (b) continuous wavelet transform: no well-resolved peak
Barnacka et al. (2015)	$23 \pm 0.5$	magn	2010 Aug 12 - 2011 Feb 28	<i>Fermi</i> -LAT (1d)	divided 7d binned LC into 4 flares and used (a) auto-correlation (b) double power spectrum (c) maximum peak $\Rightarrow$ delay depends on range of LC!
	$19.7 \pm 1.2$	magn	2012 May 3 - 2012 Sep 30		
	none	magn	$\approx$ 2014 Jul 28		
	none	magn	$\approx$ 2015 Jan 8		
Neronov et al. (2015)	$21^{+4}_{-5}$ & $76^{+25}_{-15}$	$3.1 \pm 0.5$	2008 Aug - 2014 Sept	<i>Fermi</i> -LAT (2d)	structure function and reproduction of Abdo et al. (2015) as well as Lovell et al. (1998)
Abhir et al. (2021)	none	magn	2018 Oct 9 - 2019 Nov 13	<i>Fermi</i> -LAT (6h, 12h, 1d, 5d)	auto-correlation (peaks in DCF by eye)



Consider all measurement pairs  $a_i$  and  $b_i$  from the two time series and compute

$$UDCF_{i,j} = \frac{(a_i - \bar{a})(b_j - \bar{b})}{\sqrt{(\sigma_a^2 - e_a^2)(\sigma_b^2 - e_b^2)}} \quad \begin{array}{l} \text{detrend} \\ \text{normalize} \end{array}$$

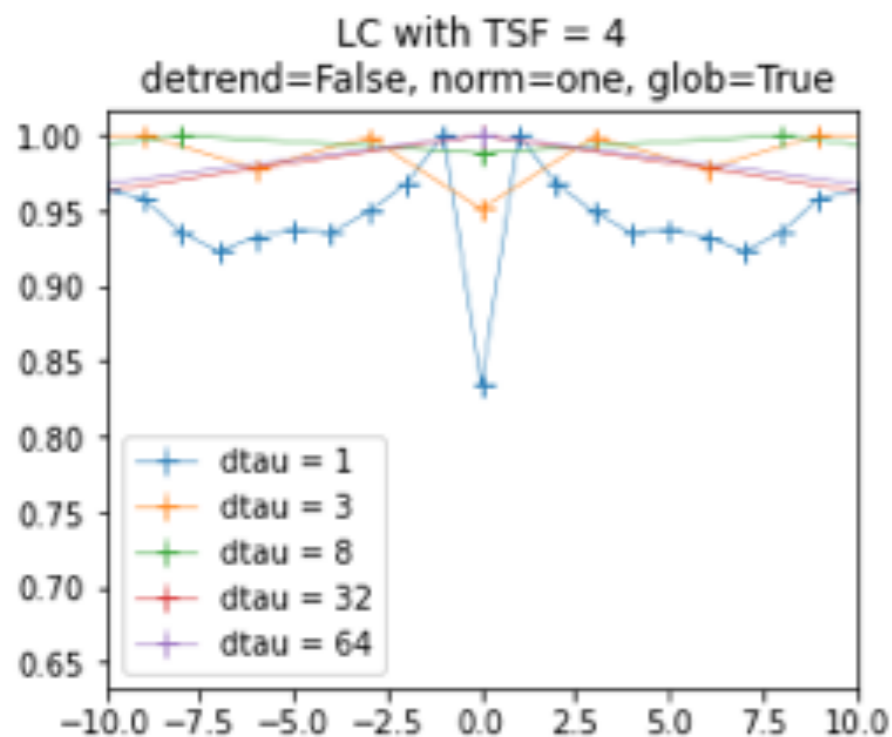
as well as the time shift between the corresponding times:  $\Delta t_{i,j} = t_j - t_i$

To compute DCF, average over all UDCF values within a chosen bin  $\Delta \tau$

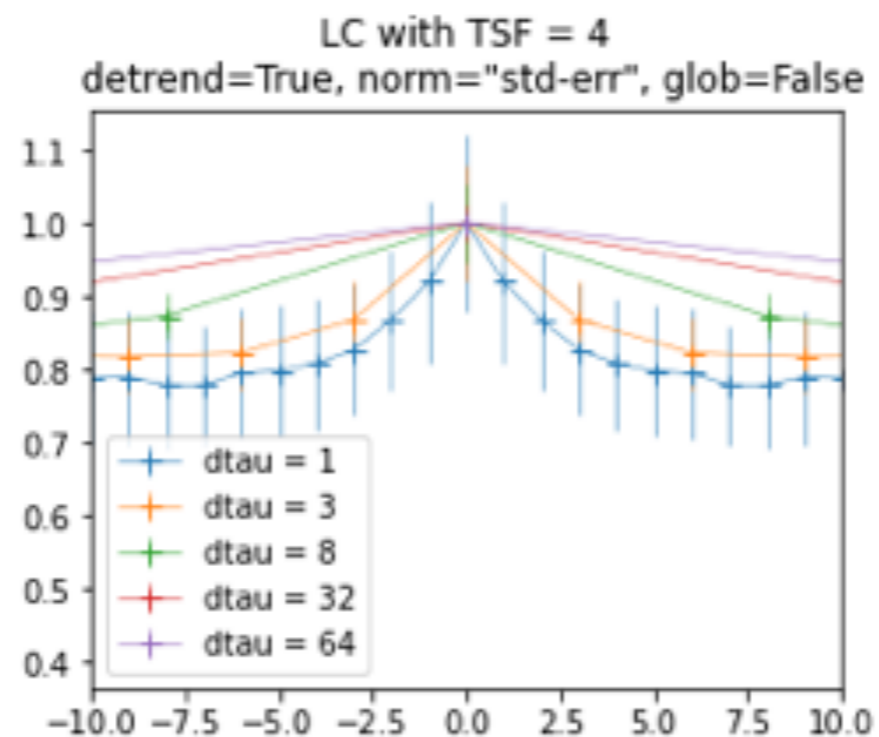
This can be done over the whole light curve or a certain lag range.

# Discrete Correlation Function

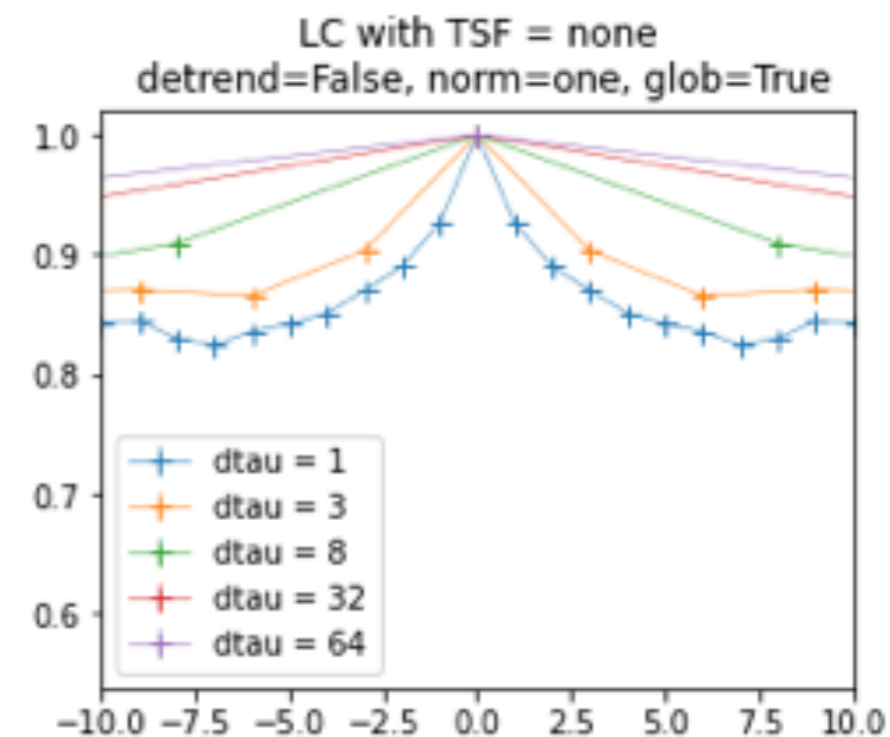
Bias of DCF can be minimized either by  
—> not applying a TS filter or  
—> detrending and normalizing the DCF



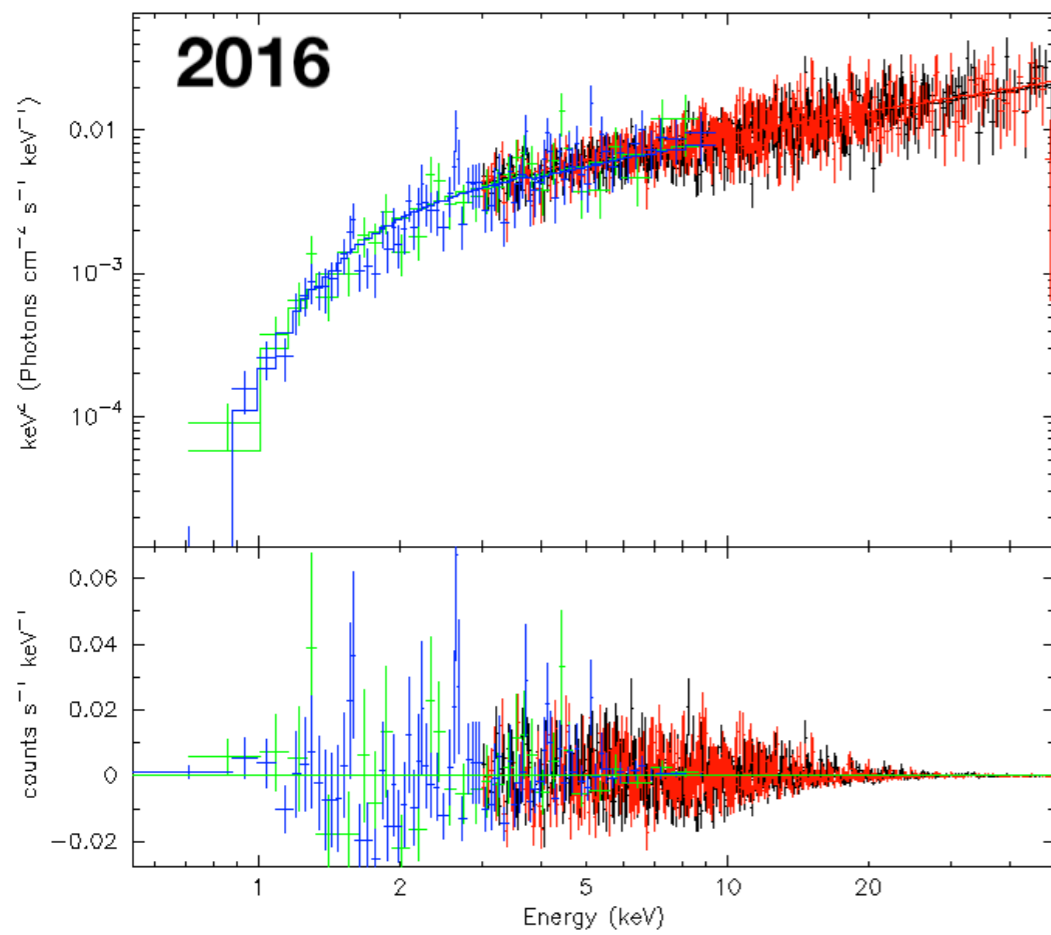
biased  
eg dip at center due  
to TS filter



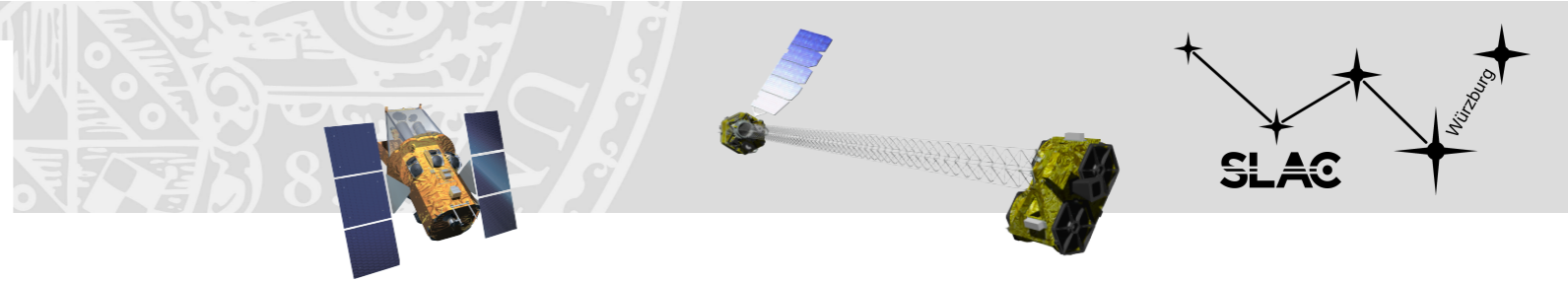
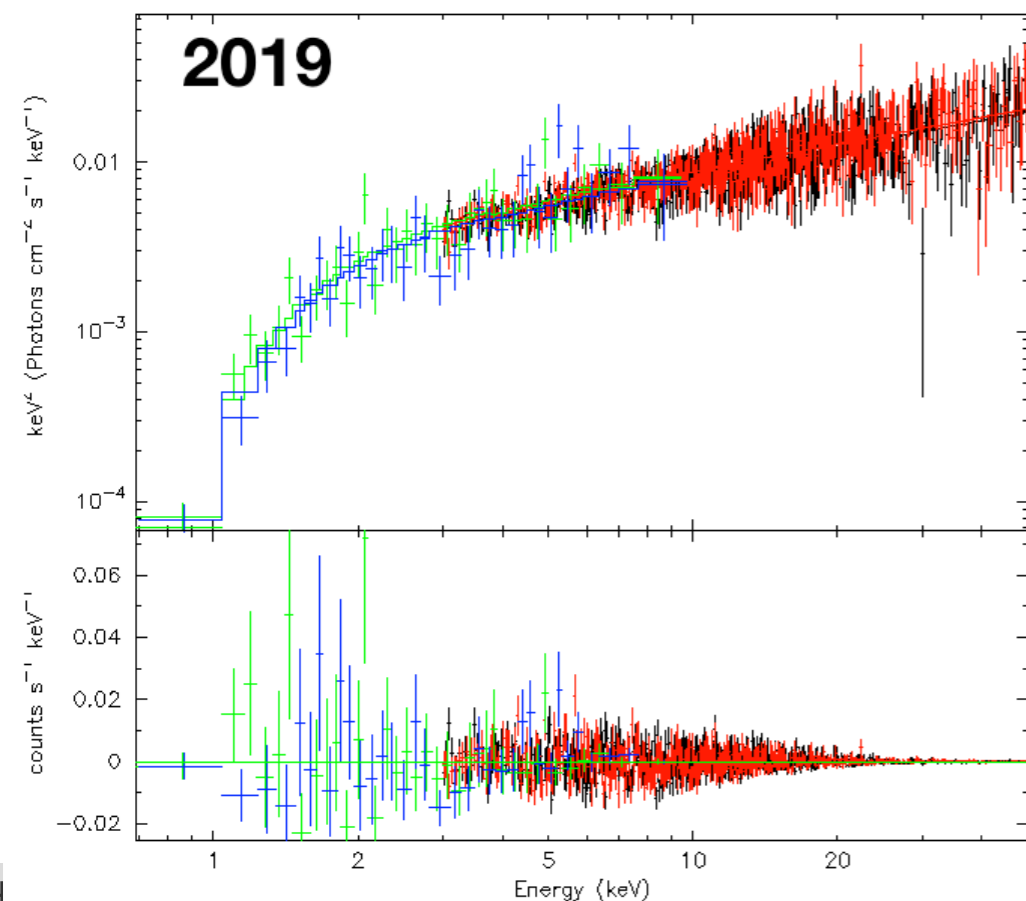
not biased  
(to be discussed)



not biased  
(to be discussed)



Unfolded Spectrum



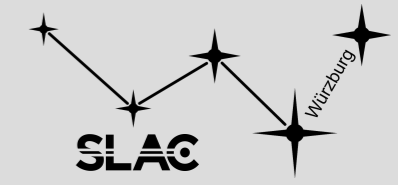
# X-ray Spectral Analysis

- Systematically smaller power-law indices for independent Swift XRT analysis
- Swift XRT data is heavily absorbed!
- NuSTAR data is crucial to determine underlying continuum
- Joint analysis to adequately fit spectral properties:  
power-law index  $\sim 1.4$

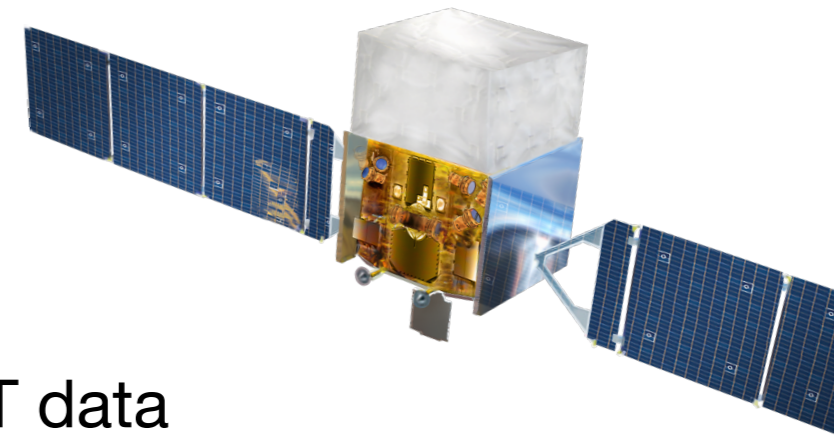
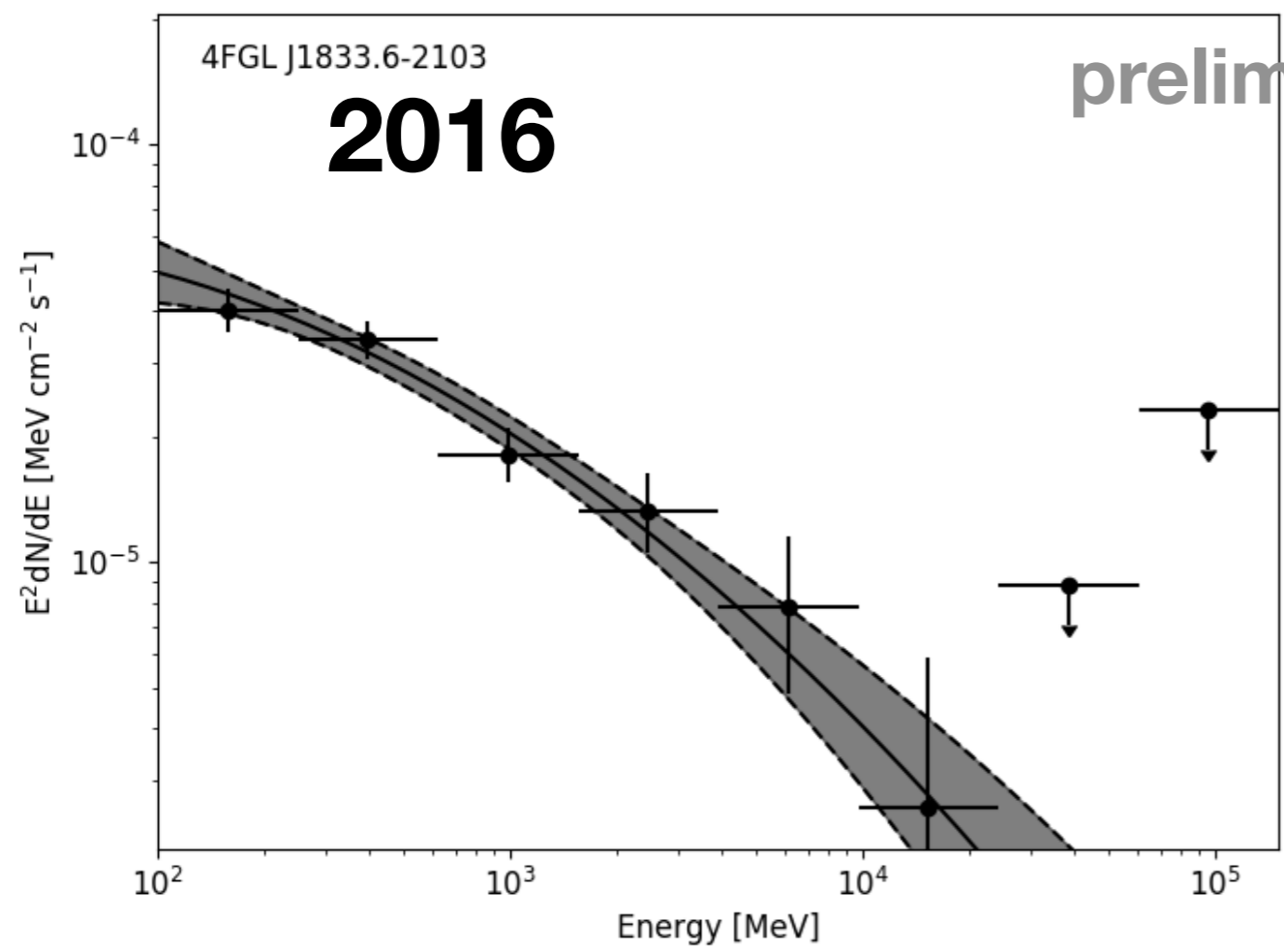


preliminary

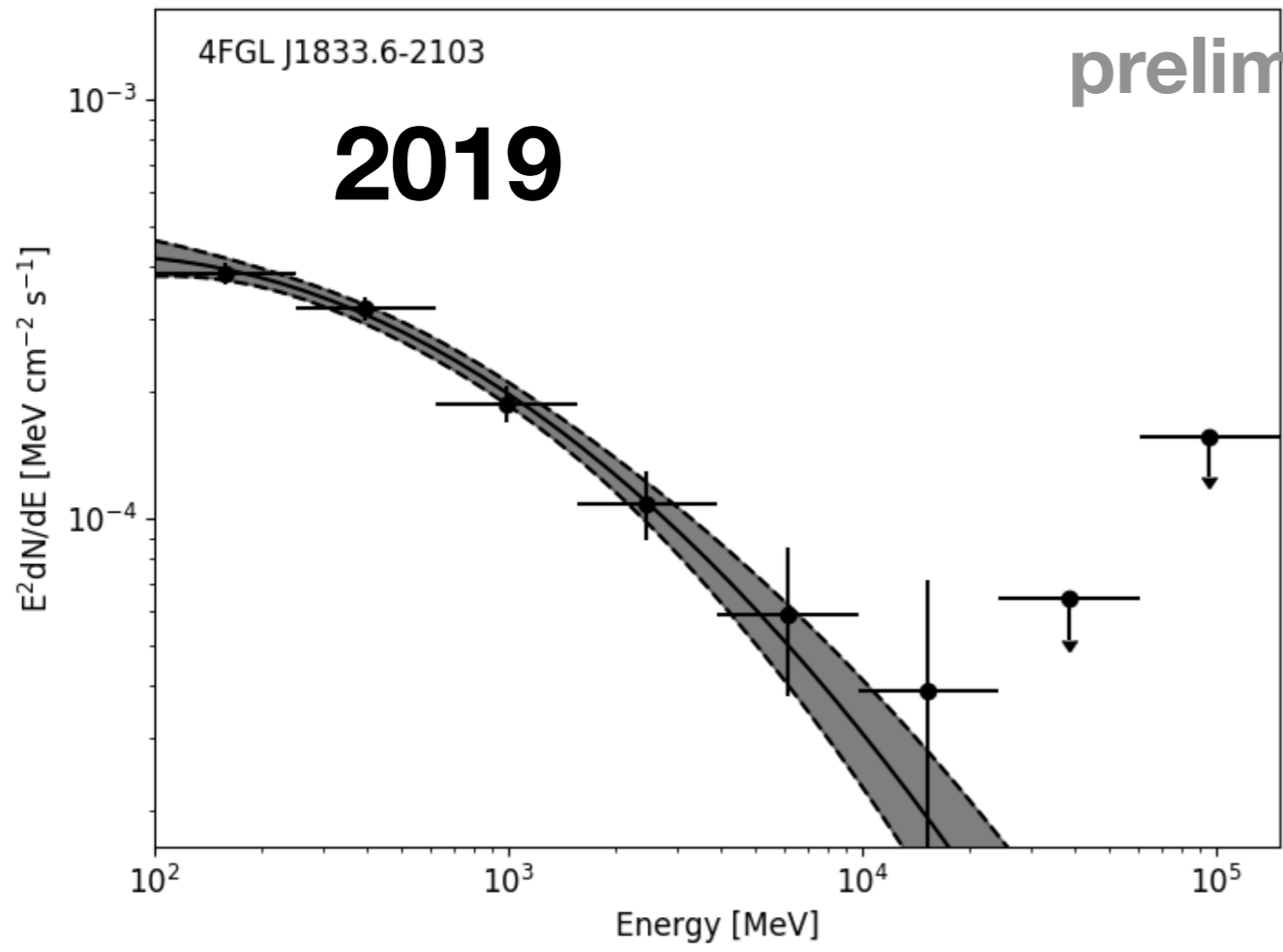
# Gamma-ray



# Spectral Analysis

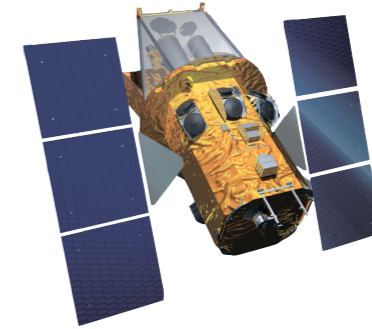
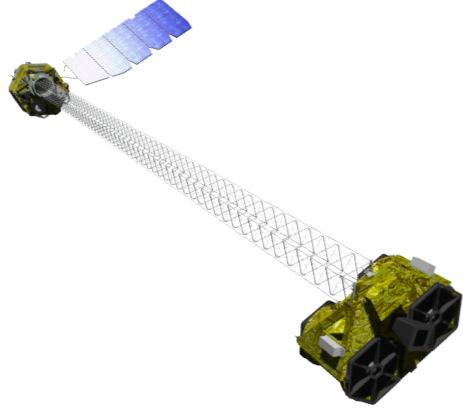


Fermi-LAT data



preliminary

- Note order of magnitude difference on y-axis
- amplitude of gamma-ray variability appears much larger than x-ray variability



Simultaneous fitting of:

NuSTAR FPMA + NuSTAR FPMB + Swift XRT (before) + Swift XRT (after)

with

- 1) absorbed power-law:  $tbabs * powerlaw$
- 2) double absorbed power-law:  $ztbabs * tbabs * powerlaw$
- 3) absorbed log-parabola:  $tbabs * logpar$

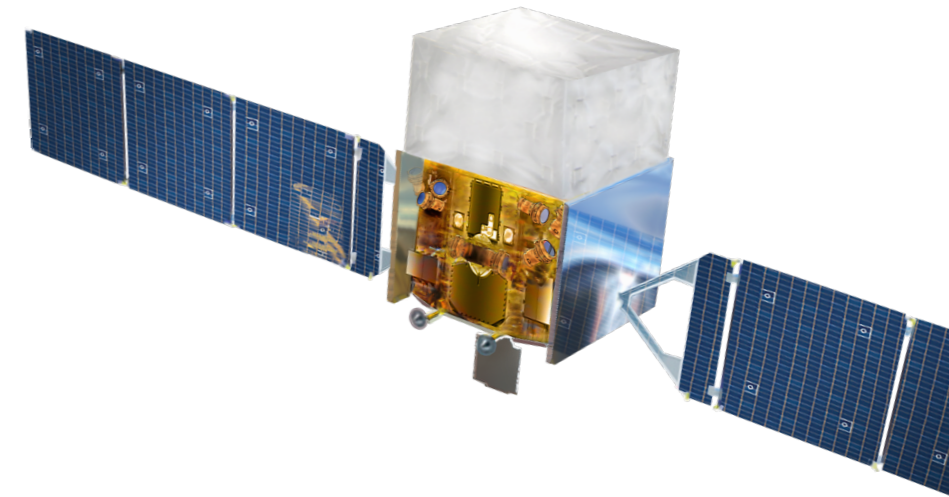
and

- $n_H$  either free or fixed to Galactic value:  $n_H = 0.18e22$
- normalization free to vary (calibration between instruments)
- for  $tbabs$ :  $z_{lens} = 0.88$

## Standard Analysis for spectra:

- FermiTools 1.2.23 & fermipy 0.20.0
- Energy range: 100 MeV – 300 GeV
- Zmax: 90
- Event class: 128
- Event type: 3
- Filter: `DATA_QUAL > 0 & LAT_CONFIG == 1`
- T in MET: 479433604 – 484444804 (2016);  
573177605 – 574041605 (2019)
- ROI: 10 deg
- Galactic diffusion: `gll_iem_v07.fits`
- Isotropic diffusion: `iso_P8_R3_SOURCE_V2_v1.txt`
- Catalog: `gll_psc_v26.xml`

analogously for light curves over the full observation period



# High-energy variability of the gravitationally lensed blazar PKS 1830-211

